

$(\mathbb{E}_{A1 \rightarrow B1}[\omega1_ , Q1_] // \mathbb{E}_{A2 \rightarrow B2}[\omega2_ , Q2_]) / ; (B1^* === A2) :=$

Module [{ i, j, E1, F1, G1, E2, F2, G2, I, M = Table },

I = IdentityMatrix@Length@B1;

E1 = M[$\partial_{i,j} Q1$, {i, A1}, {j, B1}]; E2 = M[$\partial_{i,j} Q2$, {i, A2}, {j, B2}];

F1 = M[$\partial_{i,j} Q1$, {i, A1}, {j, A1}]; F2 = M[$\partial_{i,j} Q2$, {i, A2}, {j, A2}];

G1 = M[$\partial_{i,j} Q1$, {i, B1}, {j, B1}]; G2 = M[$\partial_{i,j} Q2$, {i, B2}, {j, B2}];

$\mathbb{E}_{A1 \rightarrow B2}$ [CF [$\omega1 \omega2 \text{Det} [I - F2.G1]^{1/2}$], CF@Plus [

If [$A1 === \{ \} \vee B2 === \{ \}$, θ , $A1.E1.Inverse [I - F2.G1].E2.B2$],

If [$A1 === \{ \}$, θ , $\frac{1}{2} A1.(F1 + E1.F2.Inverse [I - G1.F2].E1^T).A1$],

If [$B2 === \{ \}$, θ , $\frac{1}{2} B2.(G2 + E2^T.G1.Inverse [I - F2.G1].E2).B2$]]]]]