

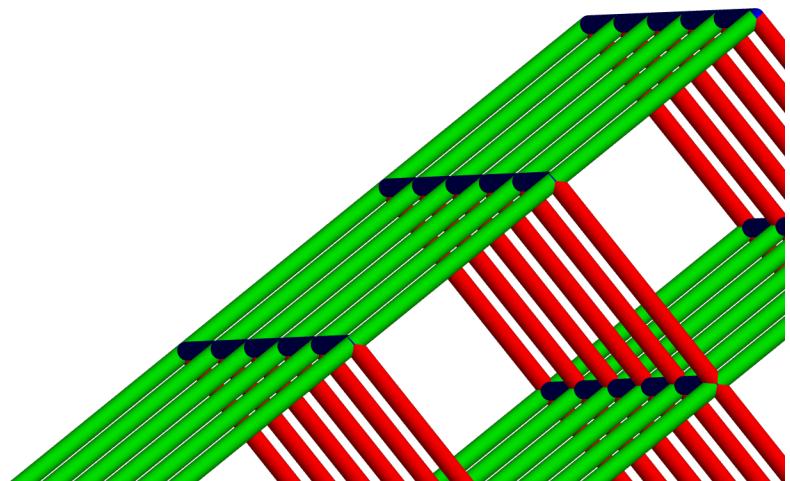
```
In[1]:= SetDirectory["C:\\drorbn\\AcademicPensieve\\Talks\\Fields-2011"]
```

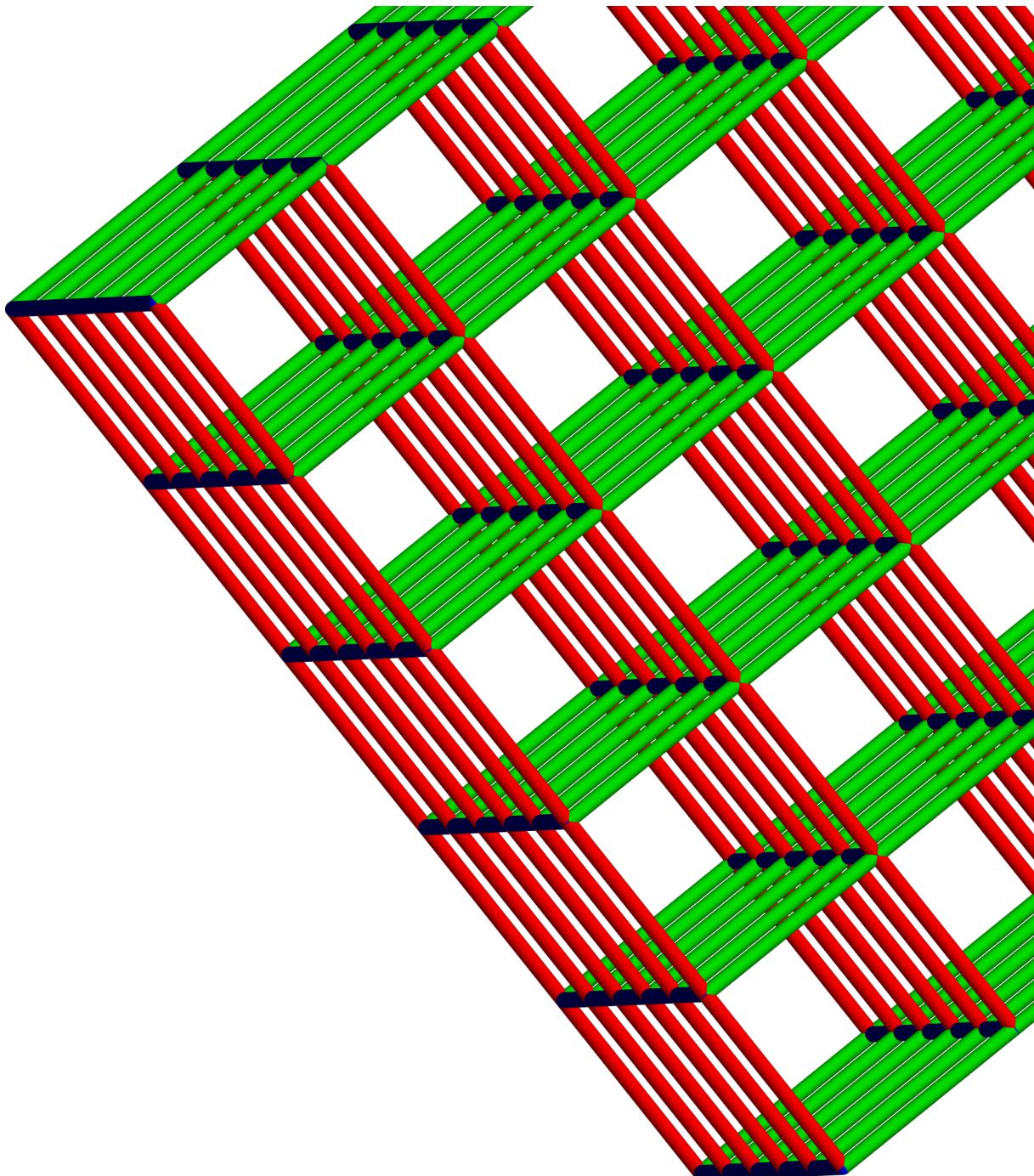
```
Out[1]= C:\\drorbn\\AcademicPensieve\\Talks\\Fields-2011
```

Makelimage

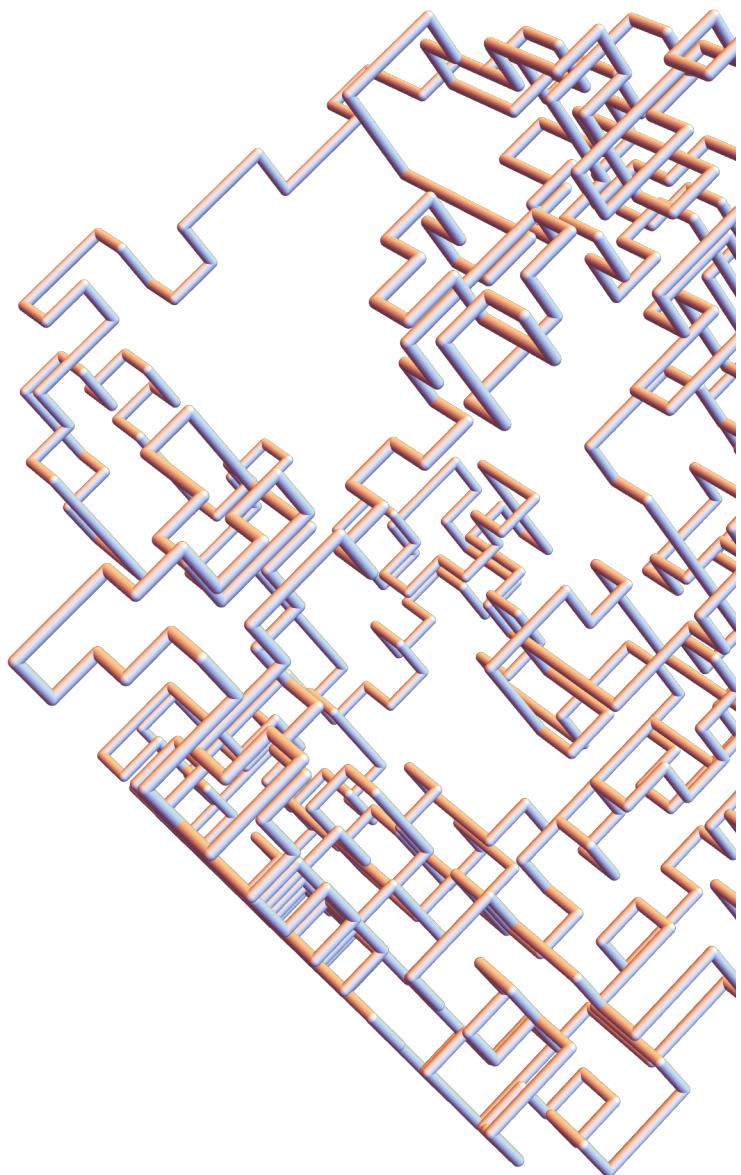
```
Options[MakeImage] = {ImageSize -> {2400}, ThumbnailSize -> {512}};
MakeImage[g_, opts___Rule] := Module[
  { isize = ImageSize /. {opts} /. Options[MakeImage]},
  ImageResize[
    ImageCrop[Rasterize[g, RasterSize -> isize, ImageSize -> isize]],
    isize]
];
MakeImage[name_String, g_, opts___Rule] := Module[{s,
  isize = ImageSize /. {opts} /. Options[MakeImage],
  tsize =ThumbnailSize /. {opts} /. Options[MakeImage]
},
  Export[name <> ".png",
  s = ImageResize[
    ImageCrop[Rasterize[$Image[name] = g, RasterSize -> isize, ImageSize -> isize]],
    isize]
];
  ImageResize[s, tsize]
];
```

```
In[2]:= n = 5;
Graphics3D[{
  Red, Table[Line[{{0, i, j}, {n, i, j}}], {i, 0, n}, {j, 0, n}],
  Green, Table[Line[{{i, 0, j}, {i, n, j}}], {i, 0, n}, {j, 0, n}],
  Blue, Table[Line[{{i, j, 0}, {i, j, n}}], {i, 0, n}, {j, 0, n}]
} /. Line -> Tube, ViewPoint -> {0, 0, \[Infinity]}, Boxed -> False]
```





```
In[1]:= n = 16; start = {1, 1, 1};
moves = {{1, 0, 0}, {-1, 0, 0}, {0, 1, 0}, {0, -1, 0}, {0, 0, 1}, {0, 0, -1}};
visited = Table[False, {n}, {n}, {n}];
path = {};
visited[[Sequence @@ (at = start)]] = True;
dirs = Range[6];
While[Length[dirs] > 0,
  d = RandomChoice[dirs];
  If[(And @@ ((1 ≤ # ≤ n) & /@ (next = at + moves[[d]]))) ∧ ! Extract[visited, next],
    AppendTo[path, Tube[{at, at = next}]];
    visited[[Sequence @@ at]] = True;
    dirs = Range[6],
    (*else*) dirs = DeleteCases[dirs, d]
  ]
];
Graphics3D[path, Boxed → False]
```



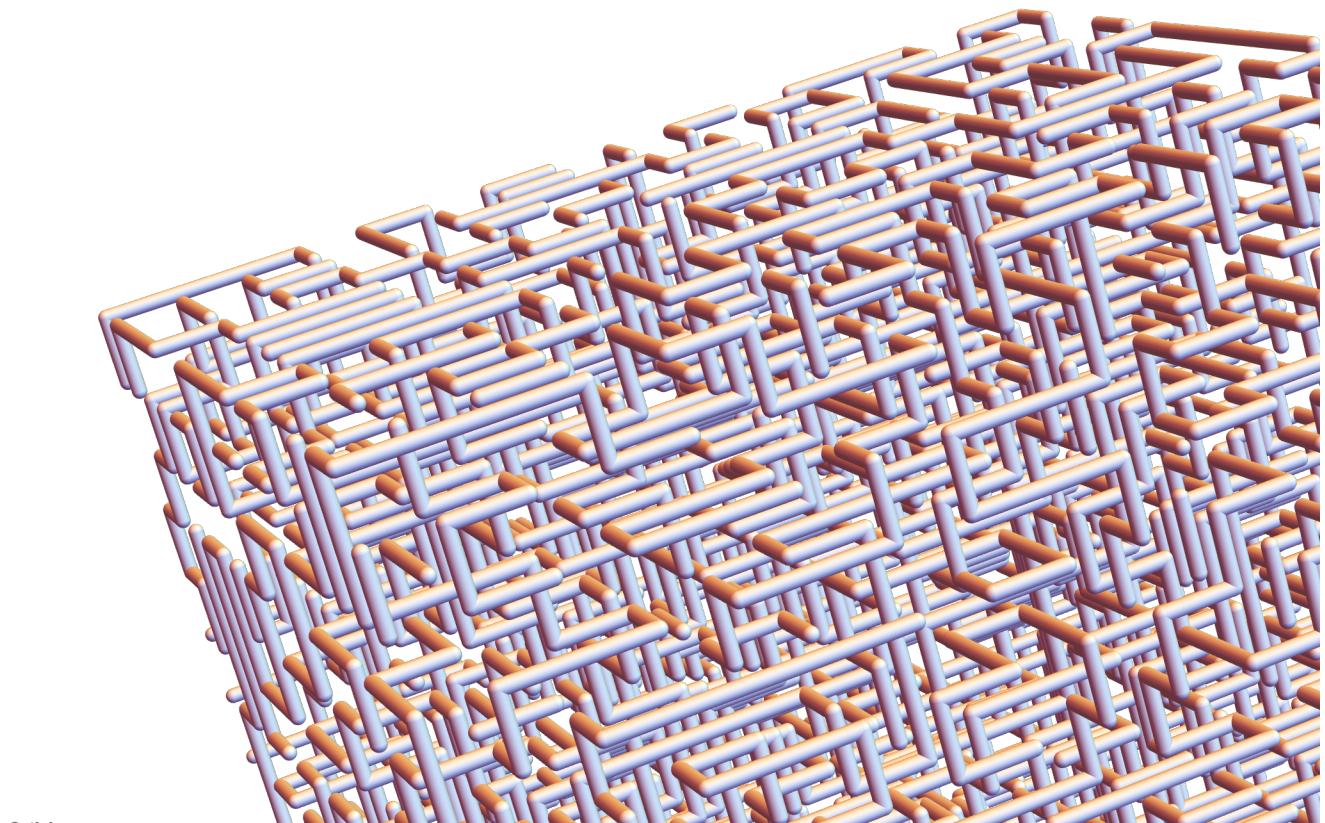
Out[\circ]=

```

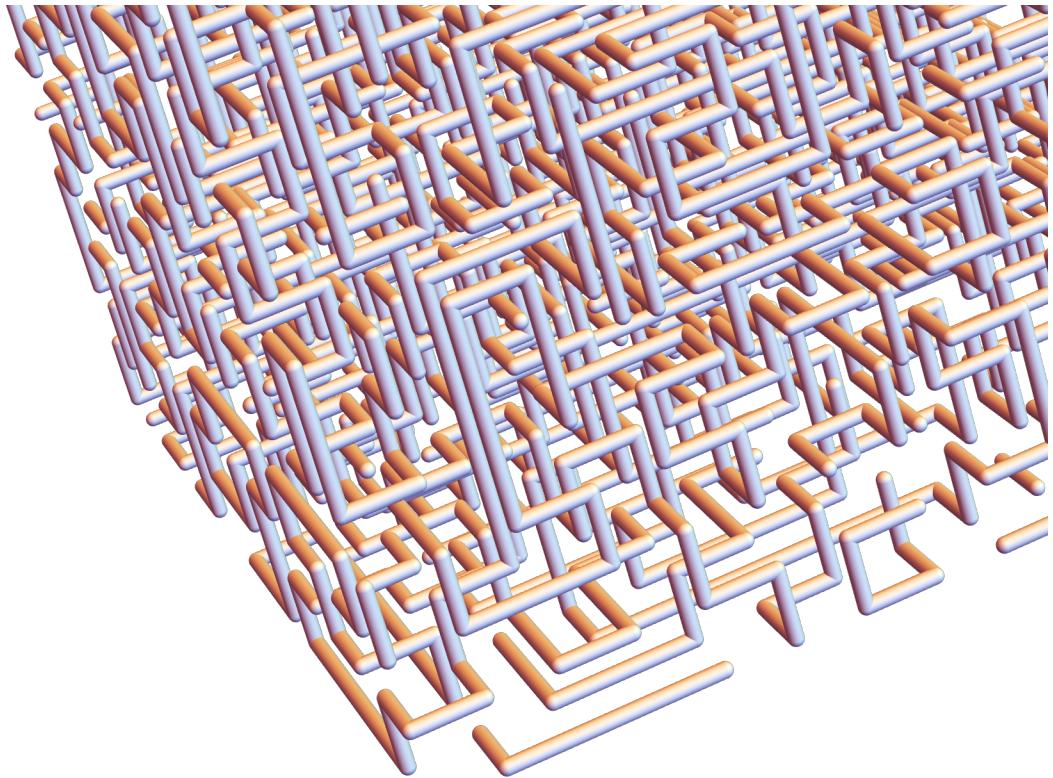
In[1]:= n = 16;
moves = {{1, 0, 0}, {-1, 0, 0}, {0, 1, 0}, {0, -1, 0}, {0, 0, 1}, {0, 0, -1}};
visited = Table[False, {n}, {n}, {n}];
path = {}; c = 0;
While[Length[pos = Position[visited, False]] > 0,
  ++c;
  visited[[Sequence @@ (at = RandomChoice[pos])]]= True;
  dirs = Range[6];
  While[Length[dirs] > 0,
    d = RandomChoice[dirs];
    If[(And @@ ((1 ≤ # ≤ n) & /@ (next = at + moves[[d]]))) ∧ ! Extract[visited, next],
      AppendTo[path, Tube[{at, at = next}]];
      visited[[Sequence @@ at]]= True;
      dirs = Range[6],
      (*else*) dirs = DeleteCases[dirs, d]
    ]
  ]
];
c
Graphics3D[path, Boxed → False]

```

Out[1]= 342

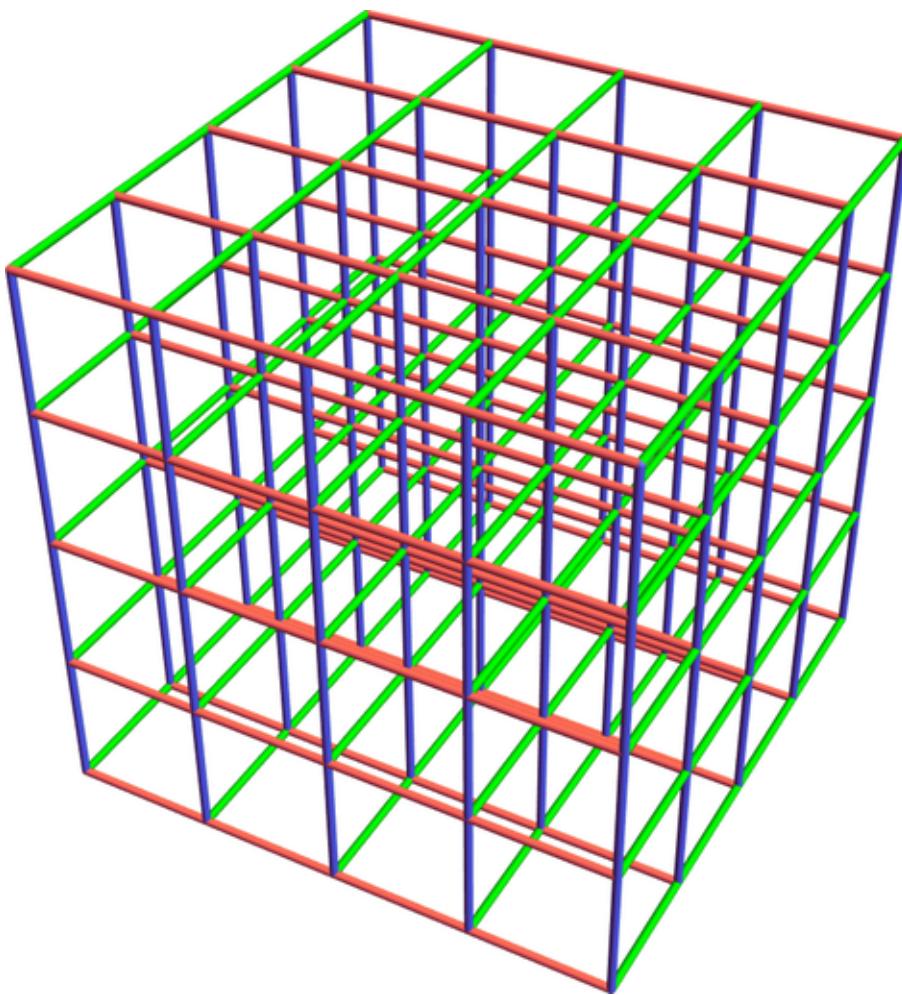


Out[=]=

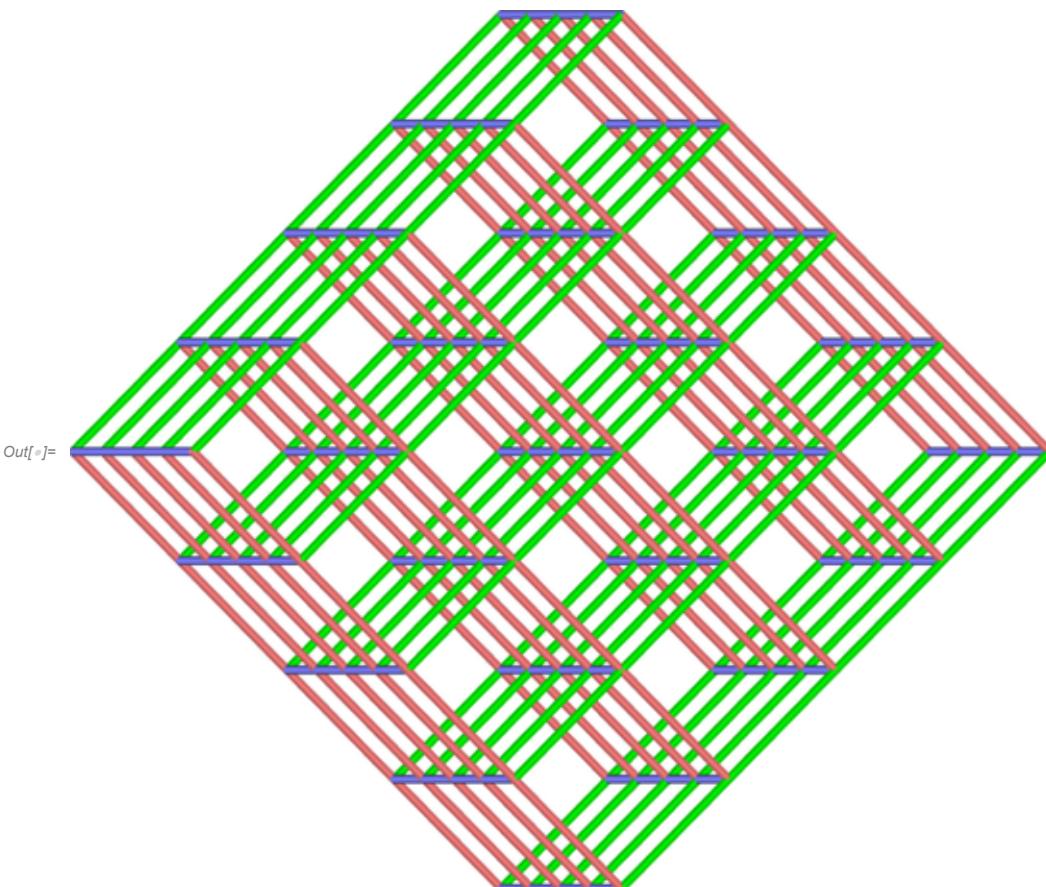


```
In[=]:= n = 5;
{e1, e2, e3} = IdentityMatrix[3];
es = RandomSample[Join[
  (# → # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
  (# → # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
  (# → # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
], Round[(1 #) &[3 n^2 (n - 1)]]];
MakeImage["4x4x4_Box", Graphics3D[{es /. x_ → y_ :>
  {Abs[y - x] /. {e1 → Pink, e2 → Green, e3 → RGBColor[0.5, 0.5, 1]}, Tube[{x, y}]}}},
  {Axes → False, Boxed → False}],
ImageSize → 800]
```

Out[\circ] =



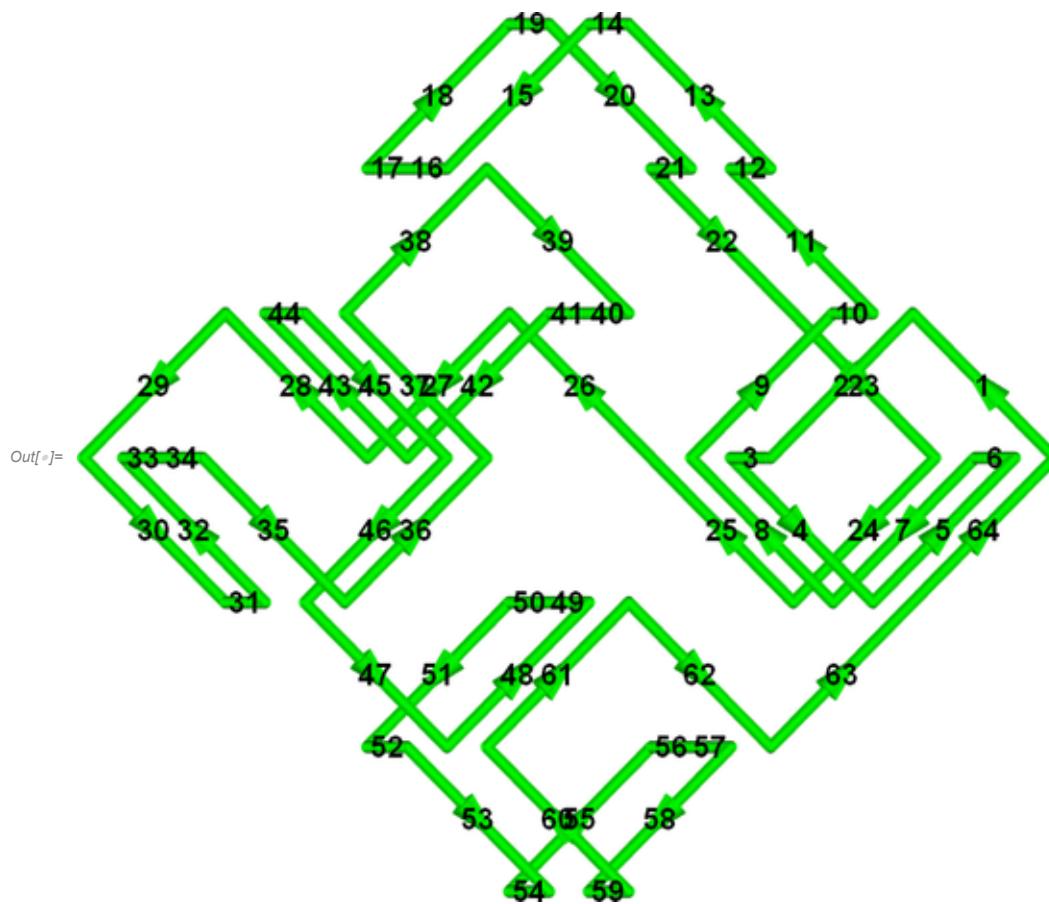
```
In[ $\circ$ ]:= n = 5;
{e1, e2, e3} = IdentityMatrix[3];
es = RandomSample[Join[
  (# → # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
  (# → # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
  (# → # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
], Round[(1 #) &[3 n2 (n - 1)]]];
MakeImage["4x4x4_Grid", Graphics3D[{es /. x_ → y_ :>
  {Abs[y - x] /. {e1 → Pink, e2 → Green, e3 → RGBColor[0.5, 0.5, 1]}, Tube[{x, y}]}}},
  {Axes → False, Boxed → False, ImageSize → {810.474, 837.}, Lighting →
    {"Directional", White, {10, 10, 10}}, {"Directional", White, {-10, -10, 10}}},
  ViewPoint → {-0.275, -0.275, 1.96107}, ViewProjection → "Orthographic",
  ViewVertical → {-0.7, 0.7, 0}}],
ImageSize →
800]
```



```

In[1]:= n = 4; SeedRandom[3];
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = RandomSample[Tuples[Range[n], 3]],
  es = RandomSample[Join[
    (# &gt;= # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# &gt;= # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# &gt;= # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ], Round[(1 #) &[3 n^2 (n - 1)]]]
];
hs = First@FindHamiltonianCycle[g];
hs = RotateLeft[hs, Position[hs, {n, n, n} &gt;= _][[1, 1]] - 1];
(*HighlightGraph[g, PathGraph@hs]*)
lhs = Complement[es, hs  $\cup$  (Reverse /@ hs)];
MakeImage["Knot_in_3x3x3", Graphics3D[{Arrowheads[0.05], Green,
  hs /. x_ &gt;= y_ :> {
    Abs[y - x] /. {e1 | e2 :> {Arrow@Tube[{x, (2 y + x) / 3}, 0.03],
      Tube[{(2 x + y) / 3, y}, 0.03]}, e3 :> Tube[{x, y}, 0.03]}
  },
  k = 0; Black,
  hs /. x_ &gt;= y_ :> Text[Style[++k, FontSize > 24, FontWeight > Bold], (x + y) / 2]
},
Boxed > False, Axes > False,
Lighting > {"Directional", White, 10 {1, 1, 1}}, {"Directional", White, 10 {-1, -1, 1}},
ViewPoint > {-0.275, -0.275, 1.96107},
ViewProjection > "Orthographic", ViewVertical > {-0.7, 0.7, 0}],
ImageSize > 800]

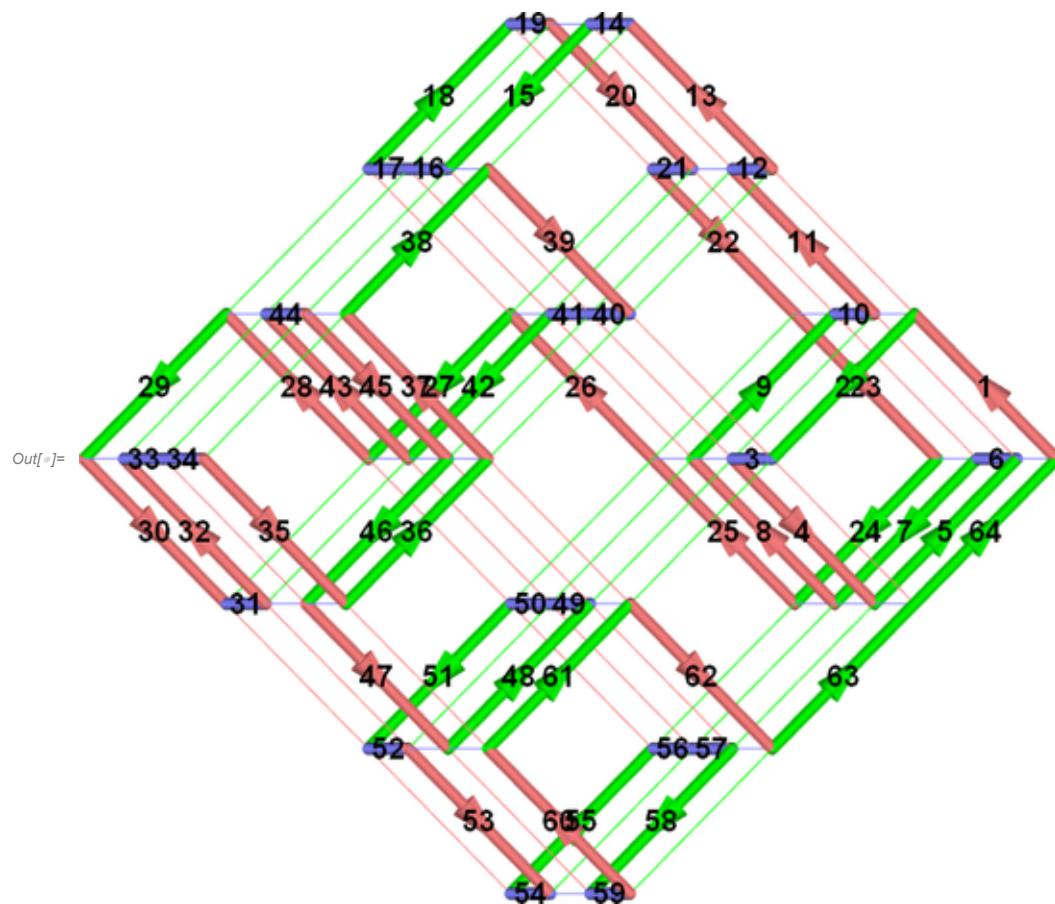
```



```

In[1]:= n = 4; SeedRandom[3];
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = RandomSample[Tuples[Range[n], 3]],
  es = RandomSample[Join[
    (# &gt; # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# &gt; # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# &gt; # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ], Round[(1 #) &[3 n^2 (n - 1)]]]
];
hs = First@FindHamiltonianCycle[g];
hs = RotateLeft[hs, Position[hs, {n, n, n} &gt; _][[1, 1]] - 1];
(*HighlightGraph[g, PathGraph@hs]*)
nhs = Complement[es, hs  $\cup$  (Reverse /@ hs)];
MakeImage["Knot_in_3x3x3_with_Grid", Graphics3D[{nhs /. x_ &gt; y_ :>
  {Abs[y - x] /. {e1 &gt; Pink, e2 &gt; Green, e3 &gt; RGBColor[0.5, 0.5, 1]}, Line[{x, y}]},
  Arrowheads[0.05],
  hs /. x_ &gt; y_ :> {
    (t = Abs[y - x]) /. {e1 &gt; Pink, e2 &gt; Green, e3 &gt; RGBColor[0.5, 0.5, 1]},
    t /. {e1 | e2 &gt; {Arrow@Tube[{x, (2 y + x) / 3}, 0.03], Tube[{(2 x + y) / 3, y}, 0.03]},
      e3 &gt; Tube[{x, y}, 0.03]}
  },
  k = 0; Black,
  hs /. x_ &gt; y_ :> Text[Style[++k, FontSize > 24, FontWeight > Bold], (x + y) / 2]
},
Boxed &gt; False, Axes &gt; False,
Lighting &gt; {"Directional", White, 10 {1, 1, 1}}, {"Directional", White, 10 {-1, -1, 1}},
ViewPoint &gt; {-0.275, -0.275, 1.96107},
ViewProjection &gt; "Orthographic", ViewVertical &gt; {-0.7, 0.7, 0}],
ImageSize &gt; 800]

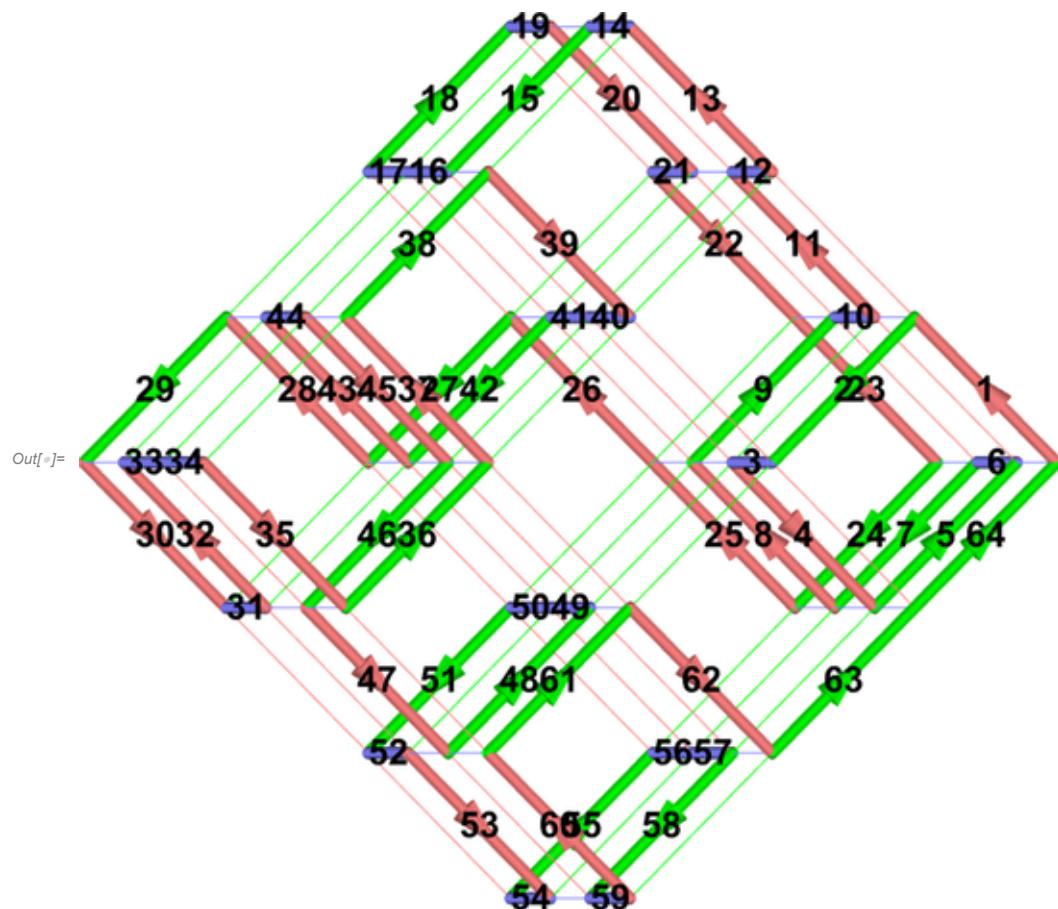
```



```

In[1]:= n = 4; SeedRandom[3];
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = RandomSample[Tuples[Range[n], 3]],
  es = RandomSample[Join[
    (# &gt;= # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# &gt;= # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# &gt;= # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ], Round[(1 #) &[3 n^2 (n - 1)]]]
];
hs = First@FindHamiltonianCycle[g];
hs = RotateLeft[hs, Position[hs, {n, n, n} &gt;= _][[1, 1]] - 1];
(*HighlightGraph[g, PathGraph@hs]*)
nhs = Complement[es, hs  $\cup$  (Reverse /@ hs)];
MakeImage["Knot_in_3x3x3_with_Grid_V2", Graphics3D[{nhs /. x_ &gt;= y_ :>
  {Abs[y - x] /. {e1 &gt;= Pink, e2 &gt;= Green, e3 &gt;= RGBColor[0.5, 0.5, 1]}, Line[{x, y}]},
  Arrowheads[0.05],
  hs /. x_ &gt;= y_ :> {
    (t = Abs[y - x]) /. {e1 &gt;= Pink, e2 &gt;= Green, e3 &gt;= RGBColor[0.5, 0.5, 1]},
    t /. {e1 | e2 &gt;= {Arrow@Tube[{x, (2 y + x) / 3}, 0.03], Tube[{(2 x + y) / 3, y}, 0.03]},
      e3 &gt;= Tube[{x, y}, 0.03]}
  },
  k = 0; Black,
  hs /. x_ &gt;= y_ :> Text[Style[++k, FontSize >= 28, FontWeight >= Bold], (x + y) / 2]
},
Boxed &gt; False, Axes &gt; False,
Lighting &gt; {"Directional", White, 10 {1, 1, 1}}, {"Directional", White, 10 {-1, -1, 1}},
ViewPoint &gt; {-0.275, -0.275, 1.96107},
ViewProjection &gt; "Orthographic", ViewVertical &gt; {-0.7, 0.7, 0}],
ImageSize &gt; 800]

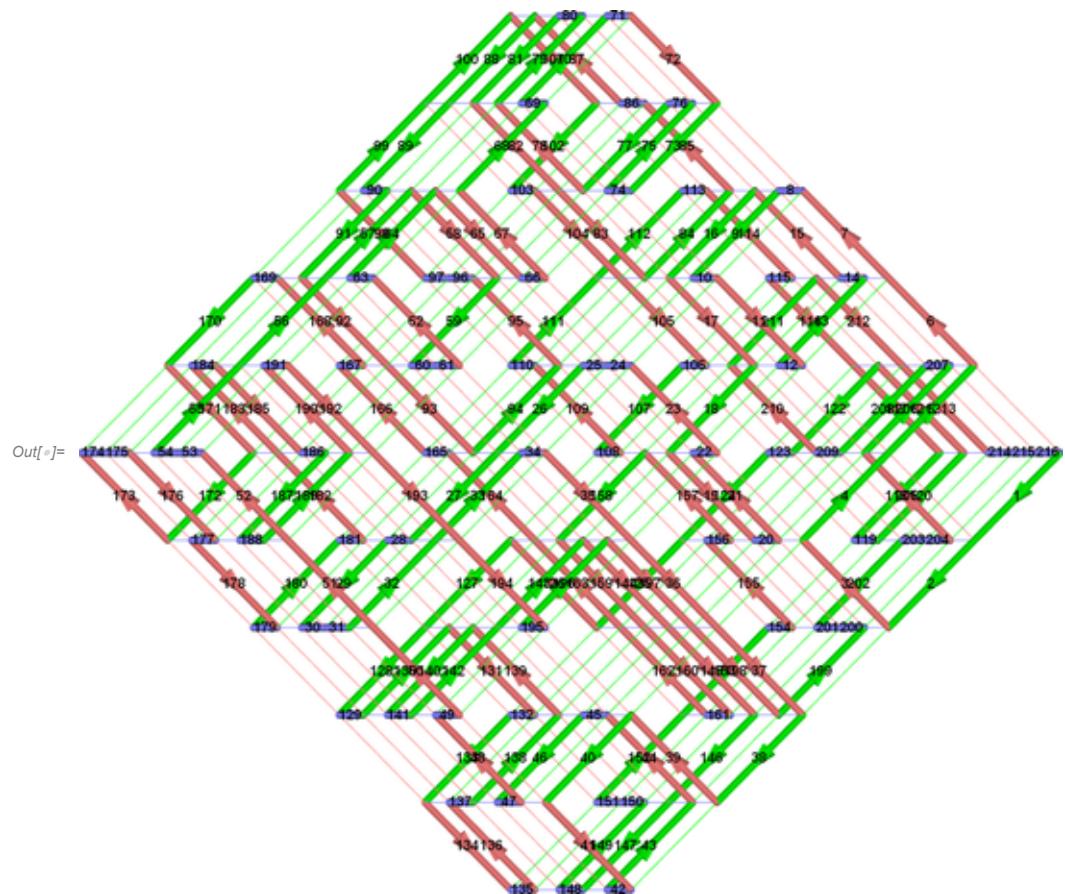
```



```

In[1]:= n = 6; SeedRandom[3];
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = RandomSample[Tuples[Range[n], 3]],
  es = RandomSample[Join[
    (# &gt; # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# &gt; # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# &gt; # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ], Round[(1 #) &[3 n^2 (n - 1)]]]
];
hs = First@FindHamiltonianCycle[g];
hs = RotateLeft[hs, Position[hs, {n, n, n} &gt; _][[1, 1]] - 1];
(*HighlightGraph[g, PathGraph@hs]*)
nhs = Complement[es, hs  $\cup$  (Reverse /@ hs)];
MakeImage["Knot_in_5x5x5_with_Grid", Graphics3D[{nhs /. x_ &gt; y_ :>
  {Abs[y - x] /. {e1 &gt; Pink, e2 &gt; Green, e3 &gt; RGBColor[0.5, 0.5, 1]}, Line[{x, y}]},
  Arrowheads[0.03],
  hs /. x_ &gt; y_ :> {
    (t = Abs[y - x]) /. {e1 &gt; Pink, e2 &gt; Green, e3 &gt; RGBColor[0.5, 0.5, 1]},
    t /. {e1 | e2 &gt; {Arrow@Tube[{x, (2 y + x) / 3}, 0.03], Tube[{(2 x + y) / 3, y}, 0.03]},
      e3 &gt; Tube[{x, y}, 0.03]}
  },
  k = 0; Black,
  hs /. x_ &gt; y_ :> Text[Style[++k, FontSize > 16, FontWeight > Bold], (x + y) / 2]
},
{Axes &gt; False, Boxed &gt; False, ImageSize &gt; {810.474, 837.}, Lighting &gt;
{{"Directional", White, {10, 10, 10}}, {"Directional", White, {-10, -10, 10}}},
ViewPoint &gt; {-0.275, -0.275, 1.96107}, ViewProjection &gt; "Orthographic",
ViewVertical &gt; {-0.7, 0.7, 0}}],
ImageSize &gt;
1200]

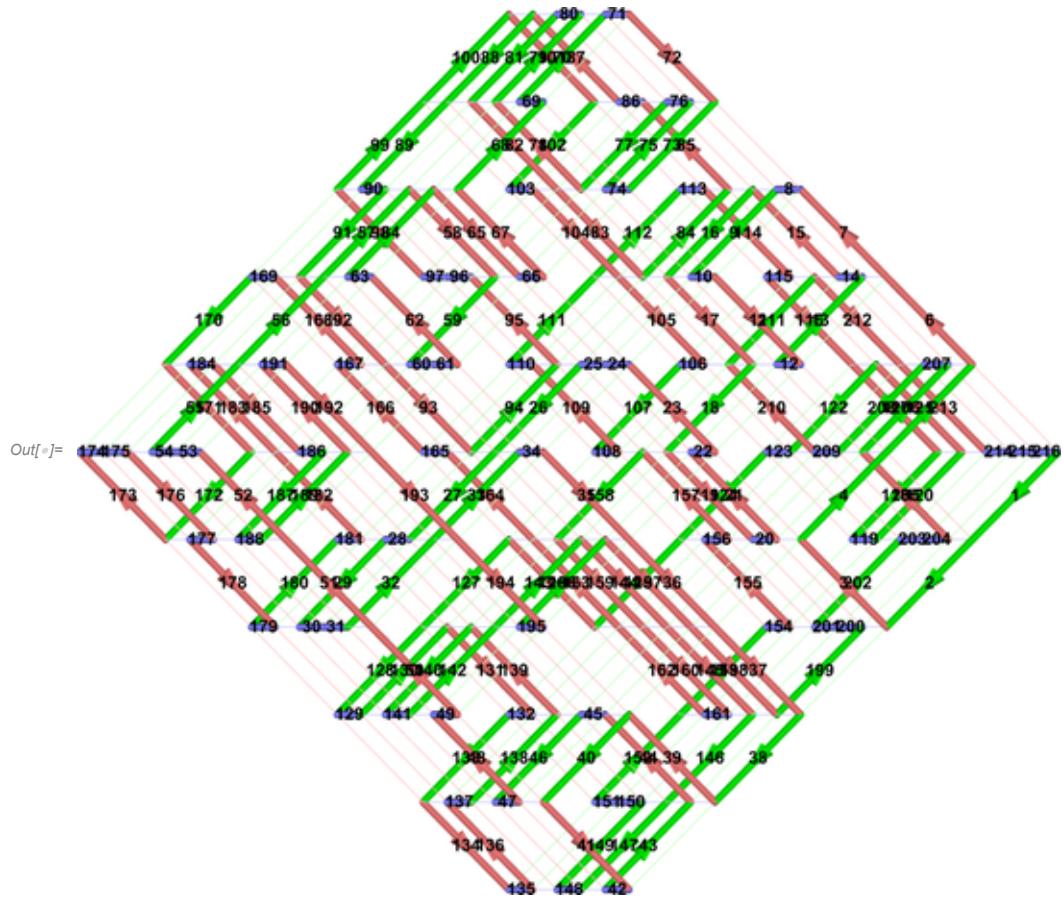
```



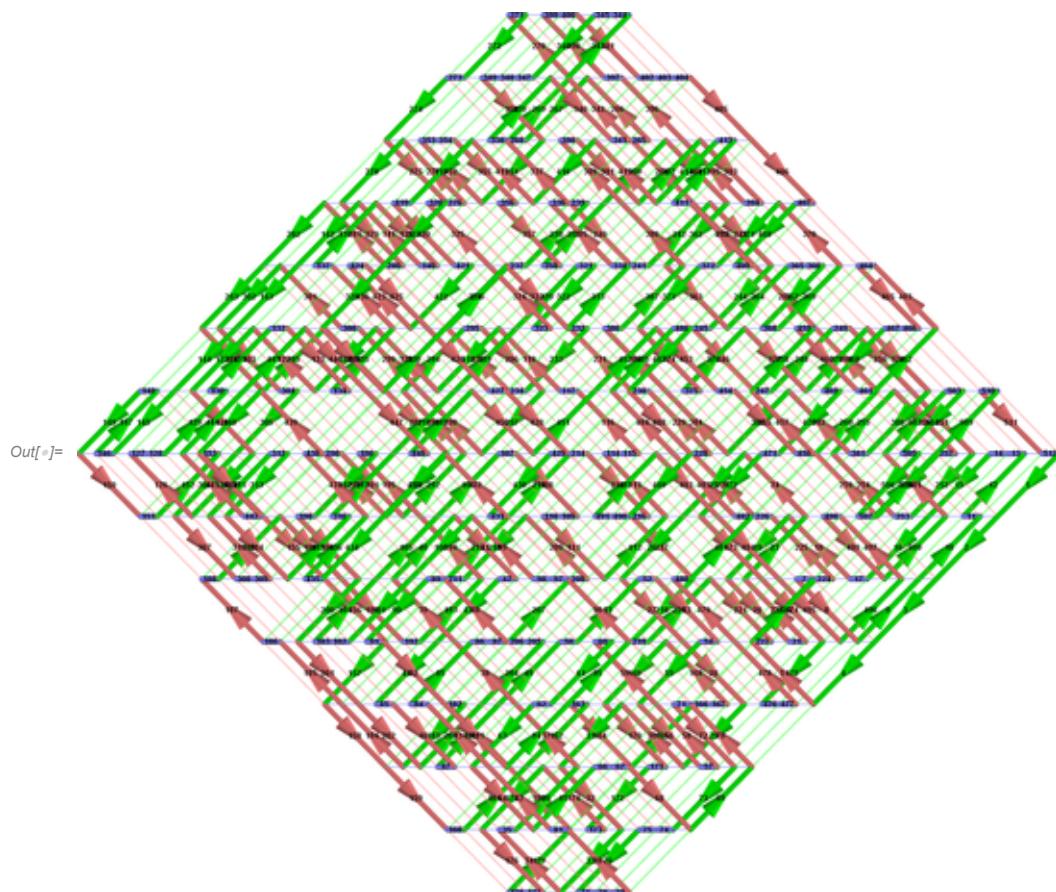
```

In[1]:= n = 6; SeedRandom[3];
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = RandomSample[Tuples[Range[n], 3]],
  es = RandomSample[Join[
    (# &gt; # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# &gt; # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# &gt; # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ], Round[(1 #) &[3 n^2 (n - 1)]]]
];
hs = First@FindHamiltonianCycle[g];
hs = RotateLeft[hs, Position[hs, {n, n, n} &gt; _][[1, 1]] - 1];
(*HighlightGraph[g, PathGraph@hs]*)
nhs = Complement[es, hs  $\cup$  (Reverse /@ hs)];
MakeImage["Knot_in_5x5x5_with_Grid_V2",
 Graphics3D[{nhs /. x_ &gt; y_ &gt; {Abs[y - x] /. {e1 &gt; RGBColor[1, 0.75, 0.75],
   e2 &gt; RGBColor[0.75, 1, 0.75], e3 &gt; RGBColor[0.75, 0.75, 1]}, Line[{x, y}]},
   Arrowheads[0.03],
   hs /. x_ &gt; y_ &gt; {
     (t = Abs[y - x]) /. {e1 &gt; Pink, e2 &gt; Green, e3 &gt; RGBColor[0.5, 0.5, 1]},
     t /. {e1 | e2 &gt; {Arrow@Tube[{x, (2 y + x) / 3}, 0.03], Tube[{(2 x + y) / 3, y}, 0.03]},
       e3 &gt; Tube[{x, y}, 0.03]}
   },
   k = 0; Black,
   hs /. x_ &gt; y_ &gt; Text[Style[++k, FontSize > 20, FontWeight > Bold], (x + y) / 2]
  },
  {Axes &gt; False, Boxed &gt; False, ImageSize > {810.474, 837.}, Lighting &gt;
   {{ "Directional", White, {10, 10, 10}}, {"Directional", White, {-10, -10, 10}}},
   ViewPoint &gt; {-0.275, -0.275, 1.96107}, ViewProjection &gt; "Orthographic",
   ViewVertical &gt; {-0.7, 0.7, 0}}],
  ImageSize &gt;
  1200]

```



```
(*n=8; SeedRandom[6];
{e1,e2,e3}=IdentityMatrix[3];
g=Graph[
  vs=RandomSample[Tuples[Range[n],3]],
  es=RandomSample[Join[
    (#+#+{1,0,0})&/@Tuples[{Range[n-1],Range[n],Range[n]}],
    (#+#+{0,1,0})&/@Tuples[{Range[n],Range[n-1],Range[n]}],
    (#+#+{0,0,1})&/@Tuples[{Range[n],Range[n],Range[n-1]}]
  ],Round[(1#)&[3n^2(n-1)]]]
];
hs=First@FindHamiltonianCycle[g];
hs=RotateLeft[hs,Position[hs,{n,n,n}~>~_] [[1,1]]-1];
(*HighlightGraph[g,PathGraph@@hs]*)
nhs=Complement[es, hs $\cup$ (Reverse/@hs)];
MakeImage["Knot_in_7x7x7_with_Grid",Graphics3D[
  {nhs/.x~>~y~>~{Abs[y-x]/.{e1~>~Pink,e2~>~Green,e3~>~RGBColor[0.5,0.5,1]},Line[{x,y}]},
  Arrowheads[0.03],
  hs/.x~>~y~>~{
    (t=Abs[y-x])/.{e1~>~Pink,e2~>~Green,e3~>~RGBColor[0.5,0.5,1]},
    t/.{e1|e2~>~{Arrow@Tube[{x,(2y+x)/3},0.03], Tube[{(2x+y)/3,y},0.03]},
         e3~>~Tube[{x,y},0.03]}
  },
  k=0; Black,
  hs/.x~>~y~>~Text[Style[++k,FontSize->12,FontWeight->Bold], (x+y)/2]
],
{Axes->False,Boxed->False,ImageSize->{810.474,837.},
 Lighting->{{"Directional",White,{10,10,10}}, {"Directional",White,{-10,-10,10}}},
 ViewPoint->{-0.275,-0.275,1.96107},
 ViewProjection->"Orthographic",ViewVertical->{-0.7,0.7,0}}],
ImageSize->1600] *)
```



(*hs>>HamiltonCycleIn7x7x7.m*)

```

In[7]:= n = 8;
{e1, e2, e3} = IdentityMatrix[3];
g = Graph[
  vs = Tuples[Range[n], 3],
  es = Join[
    (# → # + {1, 0, 0}) & /@ Tuples[{Range[n - 1], Range[n], Range[n]}],
    (# → # + {0, 1, 0}) & /@ Tuples[{Range[n], Range[n - 1], Range[n]}],
    (# → # + {0, 0, 1}) & /@ Tuples[{Range[n], Range[n], Range[n - 1]}]
  ]
];
hs = Get["HamiltonCycleIn7x7x7.m"];
(*HighlightGraph[g, PathGraph@hs]*)
nhs = Complement[es, hs ∪ (Reverse /@ hs)];
MakeImage["Knot_in_7x7x7_with_Grid", Graphics3D[{nhs /. x_ ↔ y_ :>
  {Abs[y - x] /. {e1 → Pink, e2 → Green, e3 → RGBColor[0.5, 0.5, 1]}, Line[{x, y}]},
  Arrowheads[0.03],
  hs /. x_ ↔ y_ :> {
    (t = Abs[y - x]) /. {e1 → Pink, e2 → Green, e3 → RGBColor[0.5, 0.5, 1]},
    t /. {e1 | e2 → {Arrow@Tube[{x, (2 y + x) / 3}, 0.03], Tube[{(2 x + y) / 3, y}, 0.03]},
      e3 → Tube[{x, y}, 0.02]}
  },
  k = 0; Black,
  hs /. x_ ↔ y_ :> Text[Style[++k, FontSize → 12, FontWeight → Bold], (x + y) / 2]
},
{Axes → False, Boxed → False, ImageSize → {810.474, 837.}, Lighting →
  {{Directional, White, {10, 10, 10}}, {Directional, White, {-10, -10, 10}}},
  ViewPoint → {-0.205, -0.205, 1.96107}, ViewProjection → "Orthographic",
  ViewVertical → {-0.7, 0.7, 0}}],
ImageSize →
2400]

```

