

$\mathbb{V}@\mathbf{r}_{3,1}[i_, j_] :=$

$$\begin{aligned} & \left(4 p_i x_i - 4 p_j x_i + 2 (5 + 7 T) p_i p_j x_i^2 - 2 (5 + 7 T) p_j^2 x_i^2 - 4 (-5 + 6 T) p_i^2 p_j x_i^3 + \right. \\ & 4 (-16 + 17 T + 2 T^2) p_i p_j^2 x_i^3 - 4 (-11 + 11 T + 2 T^2) p_j^3 x_i^3 + 3 (-1 + T) p_i^3 p_j x_i^4 - \\ & 3 (-1 + T) (4 + 3 T) p_i^2 p_j^2 x_i^4 + (-1 + T) (13 + 22 T + T^2) p_i p_j^3 x_i^4 - \\ & (-1 + T) (4 + 13 T + T^2) p_j^4 x_i^4 - 28 p_i p_j x_i x_j + 28 p_j^2 x_i x_j + 36 p_i^2 p_j x_i^2 x_j - \\ & 12 (9 + 2 T) p_i p_j^2 x_i^2 x_j + 24 (3 + T) p_j^3 x_i^2 x_j - 4 p_i^3 p_j x_i^3 x_j + 28 T p_i^2 p_j^2 x_i^3 x_j - \\ & 4 (-6 + 17 T + T^2) p_i p_j^3 x_i^3 x_j + 4 (-5 + 10 T + T^2) p_j^4 x_i^3 x_j + 24 p_i p_j^2 x_i x_j^2 - \\ & 24 p_j^3 x_i x_j^2 - 24 p_i^2 p_j^2 x_i^2 x_j^2 + 6 (10 + T) p_i p_j^3 x_i^2 x_j^2 - 6 (6 + T) p_j^4 x_i^2 x_j^2 - \\ & \left. 4 p_i p_j^3 x_i x_j^3 + 4 p_j^4 x_i x_j^3 \right) / 24 \end{aligned}$$