

Pensieve header: Read the Snappy data in DTs.txt and in Vols.txt and turn it into Vols.m

Startup

```
In[*]:= SetDirectory["C:\\drorbn\\AcademicPensieve\\Projects\\Theta\\Vols"];
```

```
<< KnotTheory`
```

Loading KnotTheory` version of October 29, 2024, 10:29:52.1301.

Read more at <http://katlas.org/wiki/KnotTheory>.

```
In[*]:= Rot[pd_PD] := Module[{n, xs, x, rots, Xp, Xm, front = {1}, k},
  n = Length@pd; rots = Table[0, {2 n + 1}];
  xs = Cases[pd, x_X => {Xp[x[[4]], x[[1]] PositiveQ@x,
    Xm[x[[2]], x[[1]] True}];
  For[k = 1, k <= 2 n, ++k,
    If[FreeQ[front, -k],
      front = Flatten@Replace[front, k -> {xs /. {
        Xp[k, l_] | Xm[l_, k] => {l + 1, k + 1, -l},
        Xp[l_, k] | Xm[k, l_] => {++rots[[l]]; {-l, k + 1, l + 1}},
        _Xp | _Xm => {}
      }}, {1}],
      Cases[front, k | -k] /. {k, -k} => --rots[[k];
    ];
  {xs /. {Xp[i_, j_] => {+1, i, j}, Xm[i_, j_] => {-1, i, j}}, rots}];
  Rot[K_] := Rot[PD[K]];
```

```
In[*]:= CF[E_] := Expand@Collect[E, g_, F] /. F -> Factor;
```

```
In[*]:= T3 = T1 T2;
```

```
In[*]:= F1[{s_, i_, j_}] := CF[
  s (1/2 - g3ii + T2^s g1ii g2ji - g1ii g2jj - (T2^s - 1) g2ji g3ii + 2 g2jj g3ii - (1 - T3^s) g2ji g3ji -
    g2ii g3jj - T2^s g2ji g3jj + g1ii g3jj + ((T1^s - 1) g1ji (T2^s g2ji - T2^s g2jj + T2^s g3jj) +
    (T3^s - 1) g3ji (1 - T2^s g1ii + g2ij + (T2^s - 2) g2jj - (T1^s - 1) (T2^s + 1) g1ji)) / (T2^s - 1))]
```

```
In[*]:= F2[{s0_, i0_, j0_}, {s1_, i1_, j1_}] := CF[
  s1 (T1^s0 - 1) (T2^s1 - 1)^-1 (T3^s1 - 1) g1,j1,i0 g3,j0,i1 ( (T2^s0 g2,i1,i0 - g2,i1,j0) - (T2^s0 g2,j1,i0 - g2,j1,j0) )]
```

```
In[*]:= F3[phi_, k_] = phi g3kk - phi / 2;
```

```

In[*]:=  $\Theta[K\_]$  :=  $\Theta[K]$  = Module[{X,  $\varphi$ , n, A,  $\Delta$ , G, ev,  $\Theta$ },
  (* 01 *) {X,  $\varphi$ } = Rot[K]; n = Length[X];
  (* 02 *) A = IdentityMatrix[2 n + 1];
  (* 03 *) Cases[X, {s_, i_, j_}  $\Rightarrow$  (A[[{i, j}, {i + 1, j + 1}]] +=  $\begin{pmatrix} -T^s & T^s - 1 \\ 0 & -1 \end{pmatrix}$ )]];
  (* 04 *)  $\Delta$  = T(-Total[ $\varphi$ ] - Total[X[[All, 1]]])/2 Det[A];
  (* 05 *) G = Inverse[A];
  (* 06 *) ev[ $\mathcal{E}_-$ ] := Factor[ $\mathcal{E}$  /. gv-,  $\alpha_-$ ,  $\beta_-$   $\Rightarrow$  (G[[ $\alpha$ ,  $\beta$ ]] /. T  $\rightarrow$  Tv)]];
  (* 07 *)  $\Theta$  = ev[ $\sum_{k=1}^n F_1[X[[k]]]$ ];
  (* 08 *)  $\Theta$  += ev[ $\sum_{k1=1}^n \sum_{k2=1}^n F_2[X[[k1]], X[[k2]]]$ ];
  (* 09 *)  $\Theta$  += ev[ $\sum_{k=1}^{2^n} F_3[\varphi[[k]], k]$ ];
  (* 10 *) Factor@{ $\Delta$ , ( $\Delta$  /. T  $\rightarrow$  T1) ( $\Delta$  /. T  $\rightarrow$  T2) ( $\Delta$  /. T  $\rightarrow$  T3)  $\Theta$ }
];

```

```

In[*]:= { $\Theta$ [DTCode[4, 6, 2]],  $\Theta$ [Knot[3, 1]]}

```

```

Out[*]=

$$\left\{ \left\{ \frac{1 - T + T^2}{T}, \frac{1 - T_1 + T_1^2 - T_2 - T_1^3 T_2 + T_2^2 + T_1^4 T_2^2 - T_1 T_2^3 - T_1^4 T_2^3 + T_1^2 T_2^4 - T_1^3 T_2^4 + T_1^4 T_2^4}{T_1^2 T_2^2} \right\}, \right.$$


$$\left. \left\{ \frac{1 - T + T^2}{T}, -\frac{1 - T_1 + T_1^2 - T_2 - T_1^3 T_2 + T_2^2 + T_1^4 T_2^2 - T_1 T_2^3 - T_1^4 T_2^3 + T_1^2 T_2^4 - T_1^3 T_2^4 + T_1^4 T_2^4}{T_1^2 T_2^2} \right\} \right\}$$


```

Reading and Confirming the SnapPy DTs

```

In[*]:= f = OpenRead["C:\\drorbn\\AcademicPensieve\\Projects\\Theta\\Vols\\DTs.txt"];
DTs = Table[{Read[f, Word], Read[f, String]}, 313230] /. {K_String, dt_String}  $\Rightarrow$ 
  (Knot[K]  $\rightarrow$  ToExpression@StringReplace[dt, {"["  $\rightarrow$  "DTCode["], "]"  $\rightarrow$  "]}]);
Close[f]; DTs

```

```

Out[*]=

```



```

In[*]:= Total[Drop[DTs, 249] /. { (K_  $\rightarrow$  dt_)  $\Rightarrow$  (DTCode[K] == dt) }]

```

```

... KnotTheory: Loading precomputed data in DTCode4KnotsTo11`.

```

```

... KnotTheory: Loading precomputed data in KnotTheory/12A.dts.

```

```

... KnotTheory: Loading precomputed data in KnotTheory/12N.dts.

```

```

... General: Further output of KnotTheory:loading will be suppressed during this calculation.

```

```

Out[*]=

```

```

312981 True

```

```

In[*]:= Short@Thread[DTCode /@ AllKnots[{3, 10}] == Take[DTs, 249] [[All, 2]]

```

```

Out[*]//Short=

```

```

{True, <<247>>,
 DTCode[6, 8, 14, 18, 16, 4, -20, 10, 2, -12] == DTCode[6, -10, -18, <<4>>, 8, -4, 12]}

```

```

In[ ]:= FindInRolfsen[K_] := Select[AllKnots[{3, 10}],
  (Theta[K][[1]] == Theta[#][[1]] & (Theta[K][[2]] == Theta[#][[2]] || Theta[K][[2]] == -Theta[#][[2]])) &]

In[ ]:= FindInRolfsen[DTCode[4, 6, 2]]
Out[ ]=
  {Knot[3, 1]}

In[ ]:= Table[1, 249] == Length /@ (FindInRolfsen /@ Take[DTs, 249][[All, 2]])
Out[ ]=
  True

```

```

In[ ]:= Take[DTs, 249] /. (K_ -> dt_) -> (K = First@FindInRolfsen[dt])
Out[ ]:=
{Knot[3, 1], Knot[4, 1], Knot[5, 2], Knot[5, 1], Knot[6, 3], Knot[6, 2], Knot[6, 1],
Knot[7, 7], Knot[7, 6], Knot[7, 5], Knot[7, 2], Knot[7, 3], Knot[7, 4], Knot[7, 1],
Knot[8, 14], Knot[8, 15], Knot[8, 10], Knot[8, 8], Knot[8, 12], Knot[8, 7], Knot[8, 13],
Knot[8, 2], Knot[8, 11], Knot[8, 6], Knot[8, 1], Knot[8, 18], Knot[8, 5], Knot[8, 17],
Knot[8, 16], Knot[8, 9], Knot[8, 4], Knot[8, 3], Knot[8, 20], Knot[8, 21], Knot[8, 19],
Knot[9, 30], Knot[9, 22], Knot[9, 19], Knot[9, 25], Knot[9, 28], Knot[9, 32],
Knot[9, 24], Knot[9, 8], Knot[9, 36], Knot[9, 15], Knot[9, 33], Knot[9, 27], Knot[9, 31],
Knot[9, 17], Knot[9, 26], Knot[9, 23], Knot[9, 14], Knot[9, 37], Knot[9, 20],
Knot[9, 11], Knot[9, 21], Knot[9, 12], Knot[9, 6], Knot[9, 18], Knot[9, 16], Knot[9, 7],
Knot[9, 2], Knot[9, 34], Knot[9, 41], Knot[9, 38], Knot[9, 29], Knot[9, 39], Knot[9, 9],
Knot[9, 13], Knot[9, 4], Knot[9, 5], Knot[9, 40], Knot[9, 3], Knot[9, 10], Knot[9, 35],
Knot[9, 1], Knot[9, 44], Knot[9, 45], Knot[9, 43], Knot[9, 42], Knot[9, 46], Knot[9, 48],
Knot[9, 47], Knot[9, 49], Knot[10, 60], Knot[10, 59], Knot[10, 73], Knot[10, 72],
Knot[10, 36], Knot[10, 57], Knot[10, 81], Knot[10, 80], Knot[10, 55], Knot[10, 71],
Knot[10, 88], Knot[10, 97], Knot[10, 49], Knot[10, 53], Knot[10, 47], Knot[10, 51],
Knot[10, 78], Knot[10, 77], Knot[10, 34], Knot[10, 58], Knot[10, 89], Knot[10, 70],
Knot[10, 35], Knot[10, 96], Knot[10, 45], Knot[10, 39], Knot[10, 75], Knot[10, 56],
Knot[10, 38], Knot[10, 40], Knot[10, 42], Knot[10, 44], Knot[10, 14], Knot[10, 30],
Knot[10, 41], Knot[10, 113], Knot[10, 67], Knot[10, 69], Knot[10, 87], Knot[10, 66],
Knot[10, 62], Knot[10, 65], Knot[10, 12], Knot[10, 28], Knot[10, 101], Knot[10, 92],
Knot[10, 95], Knot[10, 54], Knot[10, 37], Knot[10, 84], Knot[10, 63], Knot[10, 43],
Knot[10, 29], Knot[10, 13], Knot[10, 32], Knot[10, 5], Knot[10, 23], Knot[10, 27],
Knot[10, 2], Knot[10, 21], Knot[10, 25], Knot[10, 74], Knot[10, 18], Knot[10, 10],
Knot[10, 7], Knot[10, 107], Knot[10, 68], Knot[10, 15], Knot[10, 31], Knot[10, 6],
Knot[10, 24], Knot[10, 105], Knot[10, 76], Knot[10, 20], Knot[10, 1], Knot[10, 112],
Knot[10, 114], Knot[10, 79], Knot[10, 48], Knot[10, 52], Knot[10, 46], Knot[10, 50],
Knot[10, 82], Knot[10, 86], Knot[10, 119], Knot[10, 85], Knot[10, 83], Knot[10, 118],
Knot[10, 122], Knot[10, 121], Knot[10, 94], Knot[10, 90], Knot[10, 109], Knot[10, 115],
Knot[10, 106], Knot[10, 98], Knot[10, 102], Knot[10, 111], Knot[10, 117], Knot[10, 110],
Knot[10, 93], Knot[10, 120], Knot[10, 99], Knot[10, 100], Knot[10, 103], Knot[10, 91],
Knot[10, 17], Knot[10, 19], Knot[10, 33], Knot[10, 9], Knot[10, 26], Knot[10, 22],
Knot[10, 4], Knot[10, 8], Knot[10, 16], Knot[10, 11], Knot[10, 3], Knot[10, 104],
Knot[10, 108], Knot[10, 116], Knot[10, 123], Knot[10, 64], Knot[10, 61], Knot[10, 138],
Knot[10, 137], Knot[10, 136], Knot[10, 133], Knot[10, 135], Knot[10, 134], Knot[10, 154],
Knot[10, 151], Knot[10, 150], Knot[10, 153], Knot[10, 149], Knot[10, 148], Knot[10, 132],
Knot[10, 145], Knot[10, 125], Knot[10, 127], Knot[10, 126], Knot[10, 129], Knot[10, 131],
Knot[10, 130], Knot[10, 124], Knot[10, 128], Knot[10, 146], Knot[10, 147], Knot[10, 141],
Knot[10, 143], Knot[10, 139], Knot[10, 144], Knot[10, 140], Knot[10, 142], Knot[10, 161],
Knot[10, 156], Knot[10, 160], Knot[10, 159], Knot[10, 163], Knot[10, 152], Knot[10, 165],
Knot[10, 164], Knot[10, 155], Knot[10, 162], Knot[10, 158], Knot[10, 157]}

```

```
In[ ]:= f = OpenRead["C:\\drorbn\\AcademicPensieve\\Projects\\Theta\\Vols\\Vols.txt"];  
Vols = Table[{Read[f, Word], Read[f, String]}, 313 230] /.  
  {K_String, v_String}  $\mapsto$  (Knot[K]  $\rightarrow$  ToExpression[StringReplace[v, " E"  $\rightarrow$  "*^"]]);  
Close[f]; Vols
```

Out[]=



```
In[ ]:= Sort[Vols] >> "Vols.m"
```