

Conventions on August 18

Only one algebra (not necessarily Lie!) at a time, and it comes with a list of (Latin) generators and their Greek duals, and a default PBW order. If some Verma module is needed, it is added once and by means of extra generators.

Generators are of the form $x_{\alpha,\beta}[i]$, $a_\alpha[i]$, etc., where i is the tensor factor.

In the commutative context we have $\mathbb{E}_{i,j \rightarrow k}[L_0, L_1, \dots]$, where L_p is the coefficient of ϵ^p , and (maybe) $\mathbb{Q}_{i,j \rightarrow k}[F]$.

In the non-commutative context, generators do not carry a “tensor factor” designations. Instead we consider expressions like $U_i[x, y, y, x]$.

Issues: Upper and lower?

Experiments

```
In[*]:= e^a e^b
Out[*]= e^{a+b}
```

Conventions on August 17

Generators can be any Symbol (e.g. x,y,z,a,b,t,x12...). We use Format and Interpretation to make the appearances prettier, as in $x_{12} \rightarrow x_{12}$.

Latin to Greek duality is global: $x^* = \xi$, etc.

In the non-commutative context, generators do not carry a “tensor factor” designations. Instead we consider expressions like

$U1_i[x, y, y, x]$

Experiments

```
In[*]:= U1@i[x, y, y, x]
Out[*]= U1[i[x, y, y, x]]
```

```
In[*]:= Format[x12, StandardForm] = x_{12}
Out[*]= x_{1,2}
```

```
In[*]:= {x13@3, x12_3}
Out[*]= {x_{13}[3], x_{1,2_3}}
```

```

In[ ]:= Do[
  Format[Evaluate@Symbol["x" <> ToString[i] <> ToString[j]], StandardForm] =  $x_{10\ i+j}$ ,
  {i, 3}, {j, 3}
]

In[ ]:=  $x_{23}_4$ 
Out[ ]=
 $x_{2,3}_4$ 

In[ ]:= Module[{x},
   $x_{i,j}$  := Symbol["x" <> ToString[i] <> ToString[j]];
  Do[
    Format[ $x_{i,j}$ , StandardForm] = ToExpression[SubscriptBox["x", ToString@i <> ToString@j]],
    {i, 3}, {j, 3}
  ];
  Do[
    B[ $x_{i,j}$ ,  $x_{k,1}$ ] =  $x_{i,1}$ ,
    {i, 3}, {j, 3}, {k, 3}, {1, 3}
  ]
]

In[ ]:= B[x12, x23]_4
Out[ ]=
 $x_{134}$ 

In[ ]:=  $x_{1,2}$ 
Out[ ]=
 $x_{ij}$ 

In[ ]:= ToBoxes[y1,2]
Out[ ]=
SubscriptBox[y, RowBox[{1, , 2}]]

In[ ]:= ToExpression[SubscriptBox["y", RowBox[{1, ", ", "2"}]]]
Out[ ]=
 $y_{1,2}$ 

```