

```
In[*]:= CF[ε_] := ε / . e^L_ -> e^Expand[L]
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In[*]:= msol =
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Echo[# -> Simplify[DSolve[{# - ε ξ1,1 f1,2[λ] + ε ξ1,2 f1,2[λ] - ε ξ2,1 f1,2[λ] + ε ξ2,2 f1,2[λ] - ε f1,2'[λ] == 0, f1,2[0] == 0},
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f1,2[λ], λ
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]]] & /@
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```
(List@@ (6 ε λ2 η1,2 ξ1,2 ξ2,2 + 2 ε λ3 η1,2 ξ1,1 ξ1,2 ξ2,2 - 2 ε λ3 η1,2 ξ1,2 ξ2,2 ξ2,2 + 2 ε λ3 η1,2 ξ1,2 ξ2,1,1 ξ2,2 + 3 eλ ξ2,1-λ ξ2,2 ε λ2 η1,2 ξ2,1,22 + eλ ξ2,1-λ ξ2,2 ε λ3 η1,2 ξ1,1 ξ2,1,22 - eλ ξ2,1-λ ξ2,2 ε λ3 η1,2 ξ1,2 ξ2,1,22 + 2 eλ ξ2,1-λ ξ2,2 ε λ3 η1,2 ξ2,1,1 ξ2,1,22 - 2 eλ ξ2,2-λ ξ2,3 ε λ η1,2,3 ξ2,1,3 - eλ ξ2,2-λ ξ2,3 ε λ2 η1,2,3 ξ1,1 ξ2,1,3 + 3 eλ ξ2,2-λ ξ2,3 ε λ2 η1,3 ξ1,1,2 ξ2,1,3 + eλ ξ2,2-λ ξ2,3 ε λ3 η1,3 ξ1,1,1 ξ2,1,3 + eλ ξ2,2-λ ξ2,3 ε λ2 η2,3 ξ1,2 ξ2,1,3 - eλ ξ2,2-λ ξ2,3 ε λ3 η1,3 ξ1,2 ξ2,1,3 - eλ ξ2,2-λ ξ2,3 ε λ2 η2,3 ξ2,1,1 ξ2,1,3 + eλ ξ2,2-λ ξ2,3 ε λ3 η1,3 ξ1,1,2 ξ2,1,3 - 2 eλ ξ2,2-λ ξ2,3 ε λ3 η1,2 ξ1,1,2 ξ2,1,2 ξ2,2 - 2 eλ ξ2,1-λ ξ2,2 ε λ3 η1,2 ξ2,1,22 ξ2,2 - 3 e-λ ξ2,1+2 λ ξ2,2-λ ξ2,3 ε λ2 η2,3 ξ1,1,2 ξ2,2,3 - e-λ ξ2,1+2 λ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ1,1,1 ξ1,2 ξ2,2,3 + e-λ ξ2,1+2 λ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ1,1,2 ξ1,2 ξ2,2,3 - 3 eλ ξ2,2-λ ξ2,3 ε λ2 η1,3 ξ1,1,2 ξ2,2,3 - eλ ξ2,2-λ ξ2,3 ε λ4 η1,3 ξ1,1,1 ξ1,2 ξ2,1,2 ξ2,2,3 + eλ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ1,2 ξ2,1,2 ξ2,2,3 + eλ ξ2,2-λ ξ2,3 ε λ4 η1,3 ξ1,1,2 ξ1,2 ξ2,1,2 ξ2,2,3 - eλ ξ2,2-λ ξ2,3 ε λ4 η1,3 ξ1,1,1 ξ2,1,1 ξ2,1,2 ξ2,2,3 - 4 eλ ξ2,1-λ ξ2,3 ε λ3 η1,3 ξ2,1,22 ξ2,2,3 - eλ ξ2,1-λ ξ2,3 ε λ4 η1,3 ξ1,1,1 ξ2,1,22 ξ2,2,3 + eλ ξ2,1-λ ξ2,3 ε λ4 η1,3 ξ1,2 ξ2,1,22 ξ2,2,3 - 2 eλ ξ2,1-λ ξ2,3 ε λ4 η1,3 ξ2,1,1 ξ2,1,22 ξ2,2,3 - e-λ ξ2,1+2 λ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ1,1,2 ξ2,2,2 ξ2,2,3 + eλ ξ2,1-λ ξ2,3 ε λ4 η1,3 ξ2,1,22 ξ2,2,2 ξ2,2,3 + eλ ξ2,2-λ ξ2,3 ε λ2 η2,3 ξ2,1,3 ξ2,3,3 - eλ ξ2,2-λ ξ2,3 ε λ3 η1,3 ξ1,1,2 ξ2,1,3 ξ2,3,3 + e-λ ξ2,1+2 λ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ1,1,2 ξ2,2,3 ξ2,3,3 + eλ ξ2,2-λ ξ2,3 ε λ3 η2,3 ξ2,1,2 ξ2,2,3 ξ2,3,3 + eλ ξ2,2-λ ξ2,3 ε λ4 η1,3 ξ1,1,1 ξ2,1,22 ξ2,3,3))
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Out[*]=
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```
In[*]:= Simplify@Total[msol[[All, 2, 1, 1, 2]]]
```

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Out[*]=
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$$-e^{-(\xi_{2,1}+\xi_{2,2}+\xi_{2,3})} \lambda^2 \left( -e^{(\xi_{2,1}+\xi_{2,3})} \lambda \eta_{1,2} \xi_{2,1,2} \left( 2 e^{\lambda \xi_{2,2}} \xi_{1,1,2} + e^{\lambda \xi_{2,1}} \xi_{2,1,2} \right) + e^{2 \lambda \xi_{2,2}} \eta_{2,3} \left( e^{\lambda \xi_{2,1}} \xi_{2,1,3} + \lambda \left( e^{\lambda \xi_{2,2}} \xi_{1,1,2} + e^{\lambda \xi_{2,1}} \xi_{2,1,2} \right) \xi_{2,2,3} \right) + e^{\lambda (\xi_{2,1}+\xi_{2,2})} \lambda \eta_{1,3} \left( e^{\lambda \xi_{2,1}} \lambda \xi_{2,1,2}^2 \xi_{2,2,3} - e^{\lambda \xi_{2,2}} \xi_{1,1,2} (\xi_{2,1,3} - \lambda \xi_{2,1,2} \xi_{2,2,3}) \right) \right)$$

```
In[*]:= Expand@CF@Together@Total[msol[[All, 2, 1, 1, 2]]]
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Out[*]=
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$$2 \lambda^3 \eta_{1,2} \xi_{1,2} \xi_{2,1,2} + e^{\lambda \xi_{2,1}-\lambda \xi_{2,2}} \lambda^3 \eta_{1,2} \xi_{2,1,2}^2 - e^{\lambda \xi_{2,2}-\lambda \xi_{2,3}} \lambda^2 \eta_{2,3} \xi_{2,1,3} + e^{\lambda \xi_{2,2}-\lambda \xi_{2,3}} \lambda^3 \eta_{1,3} \xi_{1,1,2} \xi_{2,1,3} - e^{-\lambda \xi_{2,1}+2 \lambda \xi_{2,2}-\lambda \xi_{2,3}} \lambda^3 \eta_{2,3} \xi_{1,1,2} \xi_{2,2,3} - e^{\lambda \xi_{2,2}-\lambda \xi_{2,3}} \lambda^3 \eta_{1,2,3} \xi_{2,1,2} \xi_{2,2,3} - e^{\lambda \xi_{2,1}-\lambda \xi_{2,3}} \lambda^4 \eta_{1,3} \xi_{1,1,1} \xi_{2,1,2}^2 \xi_{2,2,3}$$

In[\*]:= **s = 0; k = 0;**

**Do**[

**s = ExpandDenominator@ExpandNumerator@Together@CF[s + t];**

**Echo**[(++k) →  $\frac{\text{Short}[\text{Numerator}[s]]}{\text{Factor}@\text{Denominator}[s]}$ ],

**{t, msol[[All, 2, 1, 1, 2]]}**

**]**

- » 1 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1}} (\ll 22 \gg + 6 \ll 5 \gg \xi_{2,2}^2)}{(\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^3}$
- » 2 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1}} \ll 1 \gg}{(\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 3 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1}} (\ll 84 \gg + 2 \ll 6 \gg \xi_{2,2}^3 \ll 1 \gg)}{(\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 4 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1}} \ll 1 \gg}{(\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 5 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2}} (\ll 685 \gg + 12 \ll 4 \gg \ll 1 \gg)}{(\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^3 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 6 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2}} (\ll 1227 \gg + 8 \ll 5 \gg \ll 1 \gg)}{(\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 7 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2}} \ll 1 \gg}{(\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 8 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2}} \ll 1 \gg}{(\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4}$
- » 9 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^2)}$
- » 10 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} (\ll 10746 \gg + \ll 1 \gg)}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^3)}$
- » 11 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} (\ll 12809 \gg + \ll 1 \gg)}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^3)}$
- » 12 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^4)}$
- » 13 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^4)}$
- » 14 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^4)}$
- » 15 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^4)}$
- » 16 →  $\frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \ll 1 \gg}{((\xi_{1,1} - \xi_{1,2,2} + 2 \xi_{2,1,1} - 2 \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,2,2})^4 (\xi_{1,1} - \xi_{1,2,2} + \xi_{2,1,1} - \xi_{2,3,3})^4)}$



$$\begin{aligned}
\gg 37 &\rightarrow \left( e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} ( \langle\langle 65\ 561 \rangle\rangle + \langle\langle 1 \rangle\rangle ) \right) / \\
&\quad \left( (\xi_{1,1} - \xi_{1,2} + \xi_{2,1} - \xi_{2,3})^5 (\xi_{1,1} - \xi_{1,2} + 2\xi_{2,1} - \xi_{2,2} - \xi_{2,3})^5 (\xi_{1,1} - \xi_{1,2} + \xi_{2,2} - \xi_{2,3})^4 \right) \\
\gg 38 &\rightarrow \frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \langle\langle 1 \rangle\rangle}{(\xi_{1,1} - \xi_{1,2} + \xi_{2,1} - \xi_{2,3})^5 (\xi_{1,1} - \xi_{1,2} + 2\xi_{2,1} - \xi_{2,2} - \xi_{2,3})^5} \\
\gg 39 &\rightarrow \frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \langle\langle 1 \rangle\rangle}{(\xi_{1,1} - \xi_{1,2} + \xi_{2,1} - \xi_{2,3})^5 (\xi_{1,1} - \xi_{1,2} + 2\xi_{2,1} - \xi_{2,2} - \xi_{2,3})^5} \\
\gg 40 &\rightarrow \frac{e^{-\lambda \xi_{1,1} - \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \langle\langle 1 \rangle\rangle}{(\xi_{1,1} - \xi_{1,2} + 2\xi_{2,1} - \xi_{2,2} - \xi_{2,3})^5} \\
\gg 41 &\rightarrow e^{-\lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} \left( 2 e^{\lambda \xi_{2,1} + \lambda \langle\langle 1 \rangle\rangle + \lambda \xi_{2,1}} \lambda^3 \eta_{1,2} \xi_{1,2} \xi_{2,1,2} + \langle\langle 12 \rangle\rangle \right)
\end{aligned}$$

In[\*]:= **Expand@CF@s**

Out[\*]=

$$\begin{aligned}
&2 \lambda^3 \eta_{1,2} \xi_{1,2} \xi_{2,1,2} + e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} \lambda^3 \eta_{1,2} \xi_{2,1,2}^2 - e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} \lambda^2 \eta_{1,3} \xi_{2,1,3} + \\
&e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} \lambda^3 \eta_{1,3} \xi_{1,2} \xi_{2,1,3} - e^{-\lambda \xi_{2,1} + 2\lambda \xi_{2,2} - \lambda \xi_{2,3}} \lambda^3 \eta_{1,2,3} \xi_{1,2} \xi_{2,2,3} - \\
&e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} \lambda^3 \eta_{1,2,3} \xi_{2,1,2} \xi_{2,2,3} - e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} \lambda^4 \eta_{1,3} \xi_{1,2} \xi_{2,1,2} \xi_{2,2,3} - e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} \lambda^4 \eta_{1,3} \xi_{2,1,2}^2 \xi_{2,2,3}
\end{aligned}$$


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In[\*]:= msol =

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Echo[# -> Simplify[DSolve[{# + e \xi_{1,1} g_{1,3}[\lambda] - e \xi_{1,3} g_{1,3}[\lambda] + e \xi_{2,1} g_{1,3}[\lambda] - e \xi_{2,3} g_{1,3}[\lambda] -
e g_{1,3}'[\lambda] == 0, g_{1,3}[0] == 0},
g_{1,3}[\lambda], \lambda
]]] & /@
(List@@(-2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda \eta_{1,2,3} \eta_{2,1,2} + e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1} - 2 e \lambda^2 \eta_{1,1,2} \eta_{2,1,3} \xi_{1,1,2} -
2 e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{1,1,1} \xi_{1,1,2} + 2 e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{1,1,2} \xi_{1,2,2} - 2 e \lambda^2 \eta_{1,2,3} \eta_{2,1,3} \xi_{1,2,3} -
2 e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{1,2,2} \xi_{1,2,3} - e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,3,3} + 2 e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{1,2,3} \xi_{1,3,3} +
e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{2,1,1} - 4 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,1,2} \eta_{1,1,3} \xi_{2,1,2} -
3 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,1,3} \eta_{2,1,2} \xi_{2,1,2} - 2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^2 \eta_{1,1,2} \eta_{2,1,3} \xi_{2,1,2} +
e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{2,1,2} \xi_{1,1,1} \xi_{2,1,2} - 2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{1,1,1} \xi_{2,1,2} +
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{1,2,2} \xi_{2,1,2} - 2 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{1,2,3} \xi_{2,1,2} -
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^3 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,2,3} \xi_{2,1,2} - 2 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,2,2} \xi_{1,2,3} \xi_{2,1,2} -
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,2,2} \xi_{1,2,3} \xi_{2,1,2} - e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{2,1,2} \xi_{1,3,3} \xi_{2,1,2} +
2 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,2,3} \xi_{1,3,3} \xi_{2,1,2} + 2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,2,3} \xi_{1,3,3} \xi_{2,1,2} -
2 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,2} \eta_{1,1,3} \xi_{2,1,1} \xi_{2,1,2} - 2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{2,1,1} \xi_{2,1,2} -
3 e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^2 \eta_{1,1,3}^2 \xi_{2,1,3} + e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{1,1,1} \xi_{2,1,3} -
e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{1,3,3} \xi_{2,1,3} - e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{2,1,1} \xi_{2,1,3} -
e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{2,2,2} + 2 e^{2 \lambda \xi_{2,1} - \lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,2} \eta_{1,1,3} \xi_{2,1,2} \xi_{2,2,2} +
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,2}} e \lambda^3 \eta_{1,1,2} \eta_{2,1,3} \xi_{2,1,2} \xi_{2,2,2} - e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^2 \eta_{1,1,3} \eta_{1,2,3} \xi_{2,2,3} -
2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^2 \eta_{1,2,3} \eta_{2,1,3} \xi_{2,2,3} - e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{1,2,3} \xi_{1,1,1} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{1,1,2} \xi_{2,2,3} + 2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,1,2} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,1,1} \xi_{1,1,2} \xi_{2,2,3} + 2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,1,1} \xi_{1,1,2} \xi_{2,2,3} -
2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{1,2,2} \xi_{2,2,3} - 2 e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,1,2} \xi_{1,2,2} \xi_{2,2,3} -
2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,1,2} \xi_{1,2,2} \xi_{2,2,3} + e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{1,2,3} \xi_{1,3,3} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{1,3,3} \xi_{2,2,3} + e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,1,1} \xi_{2,1,2} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,1,1} \xi_{2,1,2} \xi_{2,2,3} - 2 e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,2,2} \xi_{2,1,2} \xi_{2,2,3} -
4 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,2,2} \xi_{2,1,2} \xi_{2,2,3} + e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{1,3,3} \xi_{2,1,2} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{1,3,3} \xi_{2,1,2} \xi_{2,2,3} + e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{2,1,1} \xi_{2,1,2} \xi_{2,2,3} +
2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{2,1,1} \xi_{2,1,2} \xi_{2,2,3} - e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{1,2,3} \xi_{2,2,2} \xi_{2,2,3} -
2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{2,2,2} \xi_{2,2,3} - 2 e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{2,1,2} \xi_{2,2,2} \xi_{2,2,3} -
4 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{2,1,2} \xi_{2,2,2} \xi_{2,2,3} + e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3}^2 \xi_{2,1,3} \xi_{2,3,3} +
e^{\lambda \xi_{2,1} + \lambda \xi_{2,2} - 2 \lambda \xi_{2,3}} e \lambda^3 \eta_{1,1,3} \eta_{1,2,3} \xi_{2,2,3} \xi_{2,3,3} + 2 e^{\lambda \xi_{2,2} - \lambda \xi_{2,3}} e \lambda^3 \eta_{1,2,3} \eta_{2,1,3} \xi_{2,2,3} \xi_{2,3,3} +
e^{2 \lambda \xi_{2,1} - 2 \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3}^2 \xi_{2,1,2} \xi_{2,2,3} \xi_{2,3,3} + 2 e^{\lambda \xi_{2,1} - \lambda \xi_{2,3}} e \lambda^4 \eta_{1,1,3} \eta_{2,1,3} \xi_{2,1,2} \xi_{2,2,3} \xi_{2,3,3}))
```

Out[\*]=



In[\*]:= Factor[Total@msol[[1 ;; 15, 2, 1, 1, 2]]]

Out[\*]=

\$Aborted

```

In[*]:= s = 0; k = 0;
Do[
  s = ExpandDenominator@ExpandNumerator@Together[s + t];
  Echo[ (++k) ->  $\frac{\text{Short}[\text{Numerator}[s]]}{\text{Factor}@\text{Denominator}[s]}$  ],
  {t, msol[[1 ;; 15, 2, 1, 1, 2]]}
]
» 1 ->  $\frac{-2 e^{\lambda (\langle\langle 1 \rangle\rangle) + \lambda (\langle\langle 1 \rangle\rangle)} \eta_{1,2,3} \eta_{2,1,2} + \langle\langle 7 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^2}$ 
» 2 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^3 + \langle\langle 36 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3}$ 
» 3 ->  $-\frac{\langle\langle 1 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^3}$ 
» 4 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^7 + \langle\langle 1614 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 5 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^7 + \langle\langle 2186 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 6 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^7 + \langle\langle 2776 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 7 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^7 + \langle\langle 3344 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 8 ->  $-\frac{\langle\langle 1 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 9 ->  $\frac{-e^{\lambda (\xi_{2,2,2} - \xi_{2,3,3})} \lambda^2 \eta_{1,2,3} \eta_{2,1,2} \xi_{1,1,1}^7 + \langle\langle 3627 \rangle\rangle + e^{\lambda (\langle\langle 1 \rangle\rangle)} \lambda^2 \langle\langle 4 \rangle\rangle \xi_{2,1,1}^4}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 10 ->  $-\frac{\langle\langle 1 \rangle\rangle}{(\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4}$ 
» 11 ->  $-\left( \left( e^{-\lambda (-2 \xi_{2,1,1} + \xi_{2,2,2} + \xi_{2,3,3})} (\langle\langle 12\ 240 \rangle\rangle + 4 \langle\langle 5 \rangle\rangle \xi_{2,1,1}^4) \right) / \left( (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} - \xi_{2,1,1} + \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4 \right) \right)$ 
» 12 ->  $-\left( \left( e^{-\lambda (\xi_{1,3,3} - \xi_{2,1,1} + \xi_{2,3,3}) - \lambda (-2 \xi_{2,1,1} + \xi_{2,2,2} + \xi_{2,3,3})} (\langle\langle 28\ 004 \rangle\rangle + 3 \langle\langle 7 \rangle\rangle \langle\langle 1 \rangle\rangle) \right) / \left( (\xi_{1,1,1} - \xi_{1,3,3})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} - \xi_{2,1,1} + \xi_{2,2,2})^3 (\xi_{1,1,1} - \xi_{1,3,3} + \xi_{2,1,1} - \xi_{2,3,3})^4 \right) \right)$ 
Out[*]=
$Aborted

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In[\*]:= **Table**[**Simplify**@**DSolve**[**c**  $\lambda^k e^{b\lambda} + a g[\lambda] + g'[\lambda] == 0 \wedge g[0] == 0, g[\lambda], \lambda], \{k, 0, 5\}]$

Out[\*]=

$$\left\{ \left\{ \left\{ g[\lambda] \rightarrow \frac{c (e^{-a\lambda} - e^{b\lambda})}{a + b} \right\} \right\}, \left\{ \left\{ g[\lambda] \rightarrow -\frac{c e^{-a\lambda} (1 + e^{(a+b)\lambda} (-1 + a\lambda + b\lambda))}{(a + b)^2} \right\} \right\}, \right. \\ \left. \left\{ \left\{ g[\lambda] \rightarrow -\frac{c e^{-a\lambda} (-2 + e^{(a+b)\lambda} (2 - 2b\lambda + a^2\lambda^2 + b^2\lambda^2 + 2a\lambda(-1 + b\lambda)))}{(a + b)^3} \right\} \right\}, \right. \\ \left. \left\{ \left\{ g[\lambda] \rightarrow -\frac{1}{(a + b)^4} c e^{-a\lambda} \right. \right. \right. \\ \left. \left. \left. (6 + e^{(a+b)\lambda} (-6 + 6b\lambda - 3b^2\lambda^2 + a^3\lambda^3 + b^3\lambda^3 + 3a^2\lambda^2(-1 + b\lambda) + 3a\lambda(2 - 2b\lambda + b^2\lambda^2))) \right\} \right\}, \right. \\ \left. \left\{ \left\{ g[\lambda] \rightarrow -\frac{1}{(a + b)^5} c e^{-a\lambda} (-24 + e^{(a+b)\lambda} (24 - 24b\lambda + 12b^2\lambda^2 - 4b^3\lambda^3 + a^4\lambda^4 + b^4\lambda^4 + \right. \right. \right. \\ \left. \left. \left. 4a^3\lambda^3(-1 + b\lambda) + 6a^2\lambda^2(2 - 2b\lambda + b^2\lambda^2) + 4a\lambda(-6 + 6b\lambda - 3b^2\lambda^2 + b^3\lambda^3)) \right\} \right\}, \right. \\ \left. \left\{ \left\{ g[\lambda] \rightarrow -\frac{1}{(a + b)^6} c e^{-a\lambda} (120 + e^{(a+b)\lambda} (-120 + 120b\lambda - 60b^2\lambda^2 + 20b^3\lambda^3 - 5b^4\lambda^4 + \right. \right. \right. \\ \left. \left. \left. a^5\lambda^5 + b^5\lambda^5 + 5a^4\lambda^4(-1 + b\lambda) + 10a^3\lambda^3(2 - 2b\lambda + b^2\lambda^2) + \right. \right. \right. \\ \left. \left. \left. 10a^2\lambda^2(-6 + 6b\lambda - 3b^2\lambda^2 + b^3\lambda^3) + 5a\lambda(24 - 24b\lambda + 12b^2\lambda^2 - 4b^3\lambda^3 + b^4\lambda^4)) \right\} \right\} \right\}$$

In[\*]:= **DSolve**[**c**  $\lambda^3 + a g[\lambda] + g'[\lambda] == 0 \wedge g[0] == 0, g[\lambda], \lambda]$

Out[\*]=

$$\left\{ \left\{ g[\lambda] \rightarrow -\frac{c e^{-a\lambda} (6 - 6e^{a\lambda} + 6a e^{a\lambda}\lambda - 3a^2 e^{a\lambda}\lambda^2 + a^3 e^{a\lambda}\lambda^3)}{a^4} \right\} \right\}$$