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TLS1[K_, ω_] := Module[{spd, a, s = 0, c, cs, A, is},
  spd = Times @@ PD[K] /.
    x_X :> If[PositiveQ@x, Xp, Xm] @@ x;
  cs = spd /. {
    Xp[i_, j_, k_, l_] :> a[j, i][++s] a[k, -j][++s]
      a[-l, -k][++s] a[-i, l][++s],
    Xm[i_, j_, k_, l_] :>
      a[-j, i][++s] a[k, j][++s] a[l, -k][++s] a[-i, -l][++s]
    } //.
    a[i_, j_][x__] a[j_, k_][y__] :> a[i, k][x, y] /.
    a__[x__] :> a[x];
  A = Table[0, Length@cs, Length@cs];
  Do[is = Position[cs, 4 i - #][[1, 1]] & /@
    {3, 2, 1, 0};
   A[[is, is]] += If[spd[[i, 0]] === Xp,
     
$$\begin{pmatrix} 0 & 0 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & -1 & 0 & 1 \\ -1 & 2 & 0 & -1 \end{pmatrix}, \begin{pmatrix} 1 & -1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ -2 & 1 & 1 & 0 \\ 1 & 0 & -1 & 0 \end{pmatrix}],$$

    {i, Length[spd]}];
  Total[Sign[Select[
    Eigenvalues[(1 - ω) A + (1 - ω*) A^T],
    Abs[#] > 10^-6 &]]]];

```