

$\text{DP}_{x \rightarrow D_\alpha, y \rightarrow D_\beta}[P_][f_] := (* \text{ means } P[\partial_\alpha, \partial_\beta][f] *)$   
 $\text{Total}[\text{CoefficientRules}[P, \{x, y\}]] /.$   
 $(\{m_, n_\} \rightarrow c_) \Rightarrow c D[f, \{\alpha, m\}, \{\beta, n\}]];$   
 $\text{CF}[\mathbb{E}[\omega_, L_, Q_, P_]] := \text{Expand} /@ \text{Together} /@$   
 $\mathbb{E}[\omega /. b \Rightarrow \text{Log}[t], L, Q /. b \Rightarrow \text{Log}[t],$   
 $P /. b \Rightarrow \text{Log}[t]];$   
 $\mathbb{E} /: \mathbb{E}[\omega_1_, L1_, Q1_, P1_] \mathbb{E}[\omega_2_, L2_, Q2_, P2_] :=$   
 $\text{CF}@\mathbb{E}[\omega_1 \omega_2, L1 + L2, \omega_2 Q1 + \omega_1 Q2, \omega_2^4 P1 + \omega_1^4 P2];$   
 $\text{N}_{u_i c_j \rightarrow k}[\mathbb{E}[\omega_, L_, Q_, P_]] :=$   
 $\text{With}[\{q = e^{-\gamma} \beta u_k + \gamma c_k\}, \text{CF}[\mathbb{E}[\omega, \gamma c_k + (L /. c_j \rightarrow 0), \omega e^{-\gamma} \beta u_k + (Q /. u_i \rightarrow 0), e^{-q} \text{DP}_{c_j \rightarrow D_\gamma, u_i \rightarrow D_\beta}[P][e^q]] /.$   
 $\{\gamma \rightarrow \partial_{c_j} L, \beta \rightarrow \omega^{-1} \partial_{u_i} Q\}]];$   
 $\text{N}_{w_i c_j \rightarrow k}[\mathbb{E}[\omega_, L_, Q_, P_]] :=$   
 $\text{With}[\{q = e^\gamma \alpha w_k + \gamma c_k\}, \text{CF}[\mathbb{E}[\omega, \gamma c_k + (L /. c_j \rightarrow 0), \omega e^\gamma \alpha w_k + (Q /. w_i \rightarrow 0), e^{-q} \text{DP}_{c_j \rightarrow D_\gamma, w_i \rightarrow D_\alpha}[P][e^q]] /.$   
 $\{\gamma \rightarrow \partial_{c_j} L, \alpha \rightarrow \omega^{-1} \partial_{w_i} Q\}]];$   
 $\text{N}_{w_i u_j \rightarrow k}[\mathbb{E}[\omega_, L_, Q_, P_]] :=$   
 $\text{With}[\{q = (1 - t) \mu^{-1} \alpha \beta + \mu^{-1} \beta u_k + \mu^{-1} \delta u_k w_k + \mu^{-1} \alpha w_k\}, \text{CF}[\mathbb{E}[\mu \omega, L, \mu \omega q + \mu (Q /. w_i | u_j \rightarrow 0), \mu^4 e^{-q} \text{DP}_{w_i \rightarrow D_\alpha, u_j \rightarrow D_\beta}[P][e^q] + \omega^4 \Lambda[k]] /.$   
 $\mu \rightarrow 1 + (t - 1) \delta /.$   
 $\{\alpha \rightarrow \omega^{-1} (\partial_{w_i} Q /. u_j \rightarrow 0), \beta \rightarrow \omega^{-1} (\partial_{u_j} Q /. w_i \rightarrow 0), \delta \rightarrow \omega^{-1} \partial_{w_i, u_j} Q\}]];$   
 $m_{i_, j \rightarrow k}[\mathbb{Z}_] := \text{Module}[\{x, y, z\},$   
 $\mathbb{Z} // \text{N}_{w_i c_j \rightarrow x} // \text{N}_{w_x u_j \rightarrow y} //$   
 $\text{ReplaceAll}[\{c_{x|y} \rightarrow c_x, w_j \rightarrow w_y\}] // \text{N}_{u_i c_x \rightarrow x} //$   
 $\text{ReplaceAll}[\mathbb{Z}_{i|j|x|y} \rightarrow z_k] // \text{CF}]$