

thb[x_, y_][UU[L_], UU[R_]] :=

CF[UU[Expand[Distribute[pp[L, R]] /. {

pp[0, _] → 0, pp[_ , 0] → 0,

pp[_β | _δβ | _δa | _δaa, _β | _δβ | _δa | _δaa] → 0,

pp[_a, _β | _δβ] → 0,

pp[β[f_], a[g_, i_, j_]] :=>

Kδ_{yj} δhb[g ∂_{b_x} f, i, ϕ, y],

pp[a[f_, i_, j_], a[g_, k_, l_]] :=> Kδ_{y1} (

γa[g ∂_{b_x} f, k, l, i, j] + Kδ_{xi} (

δhb[-b_k g ∂_{b_x} f, i, ϕ, j] + δa[b_k g ∂_{b_x} f, i, j] -

δa[b_i g ∂_{b_x} f, k, j] + hb[f g, k, i, j] +

δaa[f g, ϕ, j, k, l] - δaa[f g, ϕ, l, k, j]))),

pp[a[f_, i_, j_], δa[g_, k_, l_]] :=>

Kδ_{xi} Kδ_{y1} (-δa[b_k f g, i, j] + δa[b_i f g, k, j]),

pp[a[f_, i_, j_], δaa[g_, k_, l_, m_, n_]] :=> Kδ_{xi} (

Kδ_{y1} (-δaa[b_k f g, i, j, m, n] +

δaa[b_i f g, k, j, m, n]) +

Kδ_{yn} (-δaa[b_m f g, k, l, i, j] +

δaa[b_i f g, k, l, m, j]) +

Kδ_{y1n} (δa[b_x b_m f g, k, j] - δa[b_k b_m f g, x, j]))),

pp[_δβ, _a] → 0,

pp[δa[f_, i_, j_], a[g_, k_, l_]] :=>

Kδ_{xi} Kδ_{y1} (-δa[b_k f g, i, j] + δa[b_i f g, k, j]),

pp[δaa[f_, i_, j_, m_, n_], a[g_, k_, l_]] :=>

Kδ_{xi} Kδ_{y1} (-δaa[b_k f g, i, j, m, n] +

δaa[b_i f g, k, j, m, n]) +

Kδ_{xm} Kδ_{y1} (-δaa[b_k f g, i, j, m, n] +

δaa[b_m f g, i, j, k, n]))];];];

htb[x_, y_][L_UU, R_UU] := -thb[y, x][R, L];