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In[*]:= CF[ $\mathcal{E}$ _List] := CF /@  $\mathcal{E}$ ;
CF[ $\mathcal{E}$ _] := Module[{vs, ps, c},
  vs = Union@Cases[ $\{\mathcal{E}\}$ , g_.,  $\infty$ ];
  Total[CoefficientRules[Expand[ $\mathcal{E}$ ], vs] /. (ps_ -> c_) := Factor[c] (Times @@ vsps) ]];
```

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In[*]:= CF[g1,j+, $\beta$ ]
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Out[*]=
g1,j+, $\beta$ 
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In[*]:= T3 = T1 T2;
ggRuless-,i-,j- := { (* Generic g-Rules *)
  g $\gamma$ ,i, $\beta$  := T $\gamma$ s g $\gamma$ ,i+, $\beta$  + (1 - T $\gamma$ s) g $\gamma$ ,j+, $\beta$ , g $\gamma$ ,j, $\beta$  := g $\gamma$ ,j+, $\beta$ ,
  g $\gamma$ , $\alpha$ ,i := T $\gamma$ -s g $\gamma$ , $\alpha$ ,i+, g $\gamma$ , $\alpha$ ,j := g $\gamma$ , $\alpha$ ,j+ + (1 - T $\gamma$ -s) g $\gamma$ , $\alpha$ ,i+
};
rggRuless-,i-,j- := { (* Reverse Generic g-Rules *)
  g $\gamma$ ,i+, $\beta$  := T $\gamma$ -s g $\gamma$ ,i, $\beta$  + (1 - T $\gamma$ -s) g $\gamma$ ,j, $\beta$ , g $\gamma$ ,j, $\beta$  := g $\gamma$ ,j+, $\beta$ ,
  g $\gamma$ , $\alpha$ ,i+ := T $\gamma$ s g $\gamma$ , $\alpha$ ,i, g $\gamma$ , $\alpha$ ,j+ := g $\gamma$ , $\alpha$ ,j + (1 - T $\gamma$ s) g $\gamma$ , $\alpha$ ,i
};
CF[{g1,i+, $\beta$ , g1,j+, $\beta$ , g1, $\alpha$ ,i+, g1, $\alpha$ ,j+} /. rggRules1,i,j /. ggRules1,i,j]
CF[{g1,i, $\beta$ , g1,j, $\beta$ , g1, $\alpha$ ,i, g1, $\alpha$ ,j} /. ggRules1,i,j /. rggRules1,i,j]
```

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Out[*]=
{g1,i, $\beta$ , g1,j, $\beta$ , g1, $\alpha$ ,i, g1, $\alpha$ ,j}
```

```
Out[*]=
{g1,i+, $\beta$ , g1,j+, $\beta$ , g1, $\alpha$ ,i+, g1, $\alpha$ ,j+}
```

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In[*]:= CF[g1,i+,k g2,i+,k g3,k,i+ + g1,j+,k g2,j+,k g3,k,j+ - g1,i,k g2,i,k g3,k,i - g1,j,k g2,j,k g3,k,j /. ggRules1,i,j]
```

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Out[*]=

$$\frac{(-1 + T_1) g_{1,j^+,k} g_{2,i^+,k} g_{3,k,i^+}}{T_1} +$$


$$\frac{(-1 + T_2) g_{1,i^+,k} g_{2,j^+,k} g_{3,k,i^+}}{T_2} - \frac{(-T_1 - T_2 + 2 T_1 T_2) g_{1,j^+,k} g_{2,j^+,k} g_{3,k,i^+}}{T_1 T_2}$$

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```
In[*]:= CF[g1,i+,k g2,i+,k g3,k,i+ + g1,j+,k g2,j+,k g3,k,j+ - g1,i,k g2,i,k g3,k,i - g1,j,k g2,j,k g3,k,j /. rggRules1,i,j]
```

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Out[*]=
(-1 + T1) g1,j,k g2,i,k g3,k,i + (-1 + T2) g1,i,k g2,j,k g3,k,i + (2 - T1 - T2) g1,j,k g2,j,k g3,k,i
```

Matches $d_5 p_{1,j} p_{2,i} x_{3,i} + d_3 p_{1,i} p_{2,j} x_{3,i} + (-d_3 - d_5) p_{1,j} p_{2,j} x_{3,i}$ as in DeterminingThePXXandXPPCoefficients.nb, with

In[*]:= **CF** [-g_{1,k,i} g_{2,k,i} g_{3,i,k} - g_{1,k,j} g_{2,k,j} g_{3,j,k} + g_{1,k,i} g_{2,k,i} g_{3,i⁺,k} + g_{1,k,j} g_{2,k,j} g_{3,j⁺,k} /. **ggRules**_{1,i,j}]

Out[*]=

$$\frac{(-2 + T_1 + T_2) g_{1,k,i} g_{2,k,i} g_{3,j^+,k}}{T_1 T_2} - \frac{(-1 + T_2) g_{1,k,j} g_{2,k,i} g_{3,j^+,k}}{T_2} - \frac{(-1 + T_1) g_{1,k,i} g_{2,k,j} g_{3,j^+,k}}{T_1}$$

In[*]:= **CF** [-g_{1,k,i} g_{2,k,i} g_{3,i,k} - g_{1,k,j} g_{2,k,j} g_{3,j,k} + g_{1,k,i} g_{2,k,i} g_{3,i⁺,k} + g_{1,k,j} g_{2,k,j} g_{3,j⁺,k} /. **rggRules**_{1,i,j}]

Out[*]=

$$(-T_1 - T_2 + 2 T_1 T_2) g_{1,k,i} g_{2,k,i} g_{3,j,k} + (1 - T_2) g_{1,k,j} g_{2,k,i} g_{3,j,k} + (1 - T_1) g_{1,k,i} g_{2,k,j} g_{3,j,k}$$

Matches $c_5 p_{3,j} X_{1,i} X_{2,i} - \frac{(c_5 + c_6 T_2) p_{3,j} X_{1,i} X_{2,i}}{T_1} + c_6 p_{3,j} X_{1,i} X_{2,i}$ as in DeterminingThePXXandXPPCoefficients.nb as follows:

In[*]:= **Simplify** [- $\frac{c_5 + c_6 T_2}{T_1}$ /. { **c**₅ → -T₁ - T₂ + 2 T₁ T₂, **c**₆ → 1 - T₁ }]

Out[*]=

$$1 - T_2$$