

```
Expm[U :  $\mathbb{U}_{is \rightarrow \{i1\}}[\_]$ ] :=
```

```
Module[{ $\lambda$ ,  $\mu$ , k, n, F, f, i, j, lhs, rhs, U1, MI  
(*multi-index*), mis, mi, yax},
```

```
MI /: Coefficient[ $\mathcal{E}$ _, MI[p_, n_, q_]] :=
```

```
Coefficient[Coefficient[Coefficient[ $\mathcal{E}$ ,  $y_i$ , p],  
a_i, n], x_i, q];
```

```
yax /: yaxMI[p_, n_, q_] :=  $y_i^p a_i^n x_i^q$ ;
```

```
U1 = U /. (v : (y | b | t | a | x | B | T |  $\mathcal{A}$ ))i1 → vi;
```

```
F =  $\mathbb{E}_{is \rightarrow \{i\}}[ ]$ ;
```

```
Do[AppendTo[F, 0]; Do[
```

```
mis = Flatten@Table[MI[p, n, q],  
{p, 0, Min[k + 1, 2 k + 2 - 2 n]},  
{q, 0, Min[k + 1, 2 k + 2 - 2 n - p]}];
```

```
F[[-1]] += Sum[fmi[ $\lambda$ ] yaxmi, {mi, mis}];
```

```
lhs =
```

```
( $\partial_\mu$  U21@Last[F /. { $\lambda \rightarrow \mu$ , i → j}]) //  
mi,j→i) /.  $\mu \rightarrow 0$  /. f_[0] → 0 /.
```

```
Table[fmi'[0] → Coefficient[U1[[k + 1]], mi],  
{mi, mis}];
```

```
rhs =  $\partial_\lambda$  U21@Last[F];
```

```
F =
```

```
12U[
```

```
F /.
```

```
First@
```

```
DSolve[Table[Coefficient[lhs - rhs, mi] == 0 &  $\wedge$ 
```

```
fmi[0] == 0, {mi, mis}],
```

```
Table[fmi, {mi, mis}],  $\lambda$ ],
```

```
{n, k + 1, 0, -1}], {k, 0, Length[U1] - 1}];
```

```
CF@12U[F /. { $\lambda \rightarrow 1$ , i → i1}] ]
```