

$$T_3 = T_1 T_2;$$

$\Theta[K\_]$  :=

Module [ {Cs,  $\varphi$ , n, A, s, i, j, k,  $\Delta$ , G, v,  $\alpha$ ,  
 $\beta$ , gEval, c, z},

{Cs,  $\varphi$ } = Rot [K]; n = Length [Cs];

A = IdentityMatrix [2 n + 1];

Cases [Cs, {s\_, i\_, j\_}  $\Rightarrow$

$\left( A[\{i, j\}, \{i + 1, j + 1\}] += \begin{pmatrix} -T^s & T^s & -1 \\ \theta & & -1 \end{pmatrix} \right) ]$ ;

$\Delta = T^{(-\text{Total}[\varphi] - \text{Total}[\text{Cs}[\text{All}, 1]]) / 2} \text{Det} [A]$ ;

G = Inverse [A];

gEval [ $\mathcal{E}$ \_] :=

Factor [ $\mathcal{E} / . \mathbf{g}_{v, \alpha, \beta} \Rightarrow (\mathbf{G}[\alpha, \beta] / . T \rightarrow T_v)$ ];

z = gEval [ $\sum_{k=1}^n R_{11} @@ \text{Cs} [k]$ ];

z += gEval [ $\sum_{k1=1}^n \sum_{k2=1}^n R_{12} [\text{Cs} [k1], \text{Cs} [k2]]$ ];

z += gEval [ $\sum_{k=1}^{2n} T_1 [\varphi [k], k]$ ];

{ $\Delta$ , ( $\Delta / . T \rightarrow T_1$ ) ( $\Delta / . T \rightarrow T_2$ ) ( $\Delta / . T \rightarrow T_3$ ) z} //  
Factor ];