

(*Working Casimir, not unique!*)

Define [

$$\omega_i = \mathbb{E}_{\{\} \rightarrow \{i\}} \left[\theta, \theta, \text{Series} \left[y e^{\epsilon a} x + \frac{e^{\epsilon(a+1)} + e^{-\epsilon a} T}{e^{\epsilon} - 1} - (T+1) \epsilon^{-1}, \{\epsilon, \theta, 3\} \right] /. \right. \\ \left. \{a \rightarrow a_i, T \rightarrow T_i, x \rightarrow x_i, y \rightarrow y_i\} \right]$$

$$\omega_{sq} = \omega_1 \omega_2 // \text{tm}_{1,2 \rightarrow 1};$$

$$\omega_{cub} = \omega_{sq} \omega_2 // \text{tm}_{1,2 \rightarrow 1};$$

$$\omega_4 = \omega_{cub} \omega_2 // \text{tm}_{1,2 \rightarrow 1};$$

(*Cleaned versions*)

$$\omega_c = \omega_1[[3]] /. \{T_1 \rightarrow T, a_1 \rightarrow a, x_1 \rightarrow x, y_1 \rightarrow y\} // \text{Normal};$$

$$\omega_{sqc} = \omega_{sq}[[3]] /. \{T_1 \rightarrow T, a_1 \rightarrow a, x_1 \rightarrow x, y_1 \rightarrow y\} // \text{Normal};$$

$$\omega_{cubc} = \omega_{cub}[[3]] /. \{T_1 \rightarrow T, a_1 \rightarrow a, x_1 \rightarrow x, y_1 \rightarrow y\} // \text{Normal};$$

$$\omega_{4c} = \omega_4[[3]] /. \{T_1 \rightarrow T, a_1 \rightarrow a, x_1 \rightarrow x, y_1 \rightarrow y\} // \text{Normal};$$