

In[*]:= **First@Solve**[**a x + b == 0, x**]

Out[*]=

$$\left\{ x \rightarrow -\frac{b}{a} \right\}$$

In[*]:= **First@Solve**[**a x² + b x + c == 0, x**]

Out[*]=

$$\left\{ x \rightarrow \frac{-b - \sqrt{b^2 - 4 a c}}{2 a} \right\}$$

In[*]:= **First@Solve**[**a x³ + b x² + c x + d == 0, x**]

Out[*]=

$$\left\{ x \rightarrow -\frac{b}{3 a} - \frac{2^{1/3} (-b^2 + 3 a c)}{3 a \left(-2 b^3 + 9 a b c - 27 a^2 d + \sqrt{4 (-b^2 + 3 a c)^3 + (-2 b^3 + 9 a b c - 27 a^2 d)^2} \right)^{1/3}} + \frac{\left(-2 b^3 + 9 a b c - 27 a^2 d + \sqrt{4 (-b^2 + 3 a c)^3 + (-2 b^3 + 9 a b c - 27 a^2 d)^2} \right)^{1/3}}{3 \times 2^{1/3} a} \right\}$$

In[*]:= First@Solve[a x⁴ + b x³ + c x² + d x + e == 0, x]

Out[*]=

$$\left\{ x \rightarrow \begin{aligned} &-\frac{b}{4a} - \frac{1}{2} \sqrt{\left(\frac{b^2}{4a^2} - \frac{2c}{3a} + (2^{1/3}(c^2 - 3bd + 12ae))\right) / \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} + \\ &\frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3} - \\ &\frac{1}{2} \sqrt{\left(\frac{b^2}{2a^2} - \frac{4c}{3a} - (2^{1/3}(c^2 - 3bd + 12ae))\right) / \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} - \\ &\frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3} - \\ &\left(-\frac{b^3}{a^3} + \frac{4bc}{a^2} - \frac{8d}{a}\right) / \left(4 \sqrt{\left(\frac{b^2}{4a^2} - \frac{2c}{3a} + (2^{1/3}(c^2 - 3bd + 12ae))\right) / \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} + \right. \\ &\left. \frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}\right) \end{aligned} \right\}$$

In[*]:= First@Solve[a x⁴ + b x³ + c x² + d x + e == 0, x] // TeXForm

Out[*]//TeXForm=

$$\left\{ \left\{ x \rightarrow -\frac{1}{4} \sqrt{\frac{b^2}{a^2} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3a} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3a}} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3} - \frac{1}{2} \sqrt{\frac{b^2}{2a^2} - \frac{4c}{3a} - \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3a}} - \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3} - \frac{\left(-\frac{b^3}{a^3} + \frac{4bc}{a^2} - \frac{8d}{a}\right)}{\left(4 \sqrt{\frac{b^2}{4a^2} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3a} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3a}} + \frac{\sqrt[3]{\left(-72ace + 27ad^2 + 27b^2e - 9bcd + 2c^3\right)}}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}}\right)} \right\}$$

In[*]:= **Solve**[$a x^4 + b x^3 + c x^2 + d x + e == 0, x$] **[[1, 1, 2]]**

Out[*]=

$$\begin{aligned}
 & -\frac{b}{4a} - \frac{1}{2} \sqrt{\left(\frac{b^2}{4a^2} - \frac{2c}{3a} + (2^{1/3}(c^2 - 3bd + 12ae))\right) / \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace) + \right.} \\
 & \quad \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} + \\
 & \quad \frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \right. \\
 & \quad \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} - \\
 & \frac{1}{2} \sqrt{\left(\frac{b^2}{2a^2} - \frac{4c}{3a} - (2^{1/3}(c^2 - 3bd + 12ae))\right) / \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace) + \right.} \\
 & \quad \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} - \\
 & \quad \frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \right. \\
 & \quad \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3} - \\
 & \left(-\frac{b^3}{a^3} + \frac{4bc}{a^2} - \frac{8d}{a}\right) / \left(4 \sqrt{\left(\frac{b^2}{4a^2} - \frac{2c}{3a} + (2^{1/3}(c^2 - 3bd + 12ae))\right) / \right.} \\
 & \quad \left. \left(3a(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace) + \right. \right. \\
 & \quad \left. \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}}\right) + \\
 & \quad \frac{1}{3 \times 2^{1/3} a} \left(2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace + \right. \\
 & \quad \left. \sqrt{-4(c^2 - 3bd + 12ae)^3 + (2c^3 - 9bcd + 27ad^2 + 27b^2e - 72ace)^2}\right)^{1/3}} \Big) \Big) \Big)
 \end{aligned}$$

In[*]:= **Solve** [$a x^4 + b x^3 + c x^2 + d x + e == 0, x$] [[1, 1, 2]] // **Simplify**

Out[*]=

$$\begin{aligned}
 &-\frac{1}{12 a} \\
 &\left(3 b + \sqrt{3} a \sqrt{\left(\frac{1}{a^2} \left(3 b^2 - 8 a c + (4 \times 2^{1/3} a (c^2 - 3 b d + 12 a e)) \right) / \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - \right. \right. \right. \\
 &\quad \left. \left. \left. 72 a c e + \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} + \right. \right. \\
 &\quad \left. \left. 2 \times 2^{2/3} a \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - 72 a c e + \right. \right. \right. \\
 &\quad \left. \left. \left. \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} \right) \right) + \sqrt{6} a \\
 &\sqrt{\left(-\frac{1}{a^3} \left(-3 a b^2 + 8 a^2 c + (2 \times 2^{1/3} a^2 (c^2 - 3 b d + 12 a e)) / \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - 72 \right. \right. \right. \right. \\
 &\quad \left. \left. \left. a c e + \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} + \right. \right. \\
 &\quad \left. \left. 2^{2/3} a^2 \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - 72 a c e + \right. \right. \right. \\
 &\quad \left. \left. \left. \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} - \right. \right. \\
 &\quad \left. \left. \left(3 \sqrt{3} (b^3 - 4 a b c + 8 a^2 d) \right) / \left(\sqrt{\left(\frac{1}{a^2} \left(3 b^2 - 8 a c + (4 \times 2^{1/3} a (c^2 - 3 b d + 12 a e)) \right) / \right. \right. \right. \right. \\
 &\quad \left. \left. \left. \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - 72 a c e + \right. \right. \right. \right. \\
 &\quad \left. \left. \left. \left. \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} + \right. \right. \right. \\
 &\quad \left. \left. \left. 2 \times 2^{2/3} a \left(2 c^3 - 9 b c d + 27 a d^2 + 27 b^2 e - 72 a c e + \right. \right. \right. \right. \\
 &\quad \left. \left. \left. \left. \sqrt{-4 (c^2 - 3 b d + 12 a e)^3 + (2 c^3 - 9 c (b d + 8 a e) + 27 (a d^2 + b^2 e))^2} \right)^{1/3} \right) \right) \right) \\
 &\left. \left. \left. \left. \left. \right) \right) \right) \right) \right)
 \end{aligned}$$

In[*]:= **Solve** [$a x^4 + b x^3 + c x^2 + d x + e == 0, x$] [[1, 1, 2]] // **FullSimplify**

Out[*]=

\$Aborted