

Pensieve header: HW6 Support Notebook.

Q1

$$\text{In[]:= } \left\{ \hat{y} = \begin{pmatrix} \theta & \theta \\ \epsilon & \theta \end{pmatrix}, \hat{b} = \begin{pmatrix} \theta & \theta \\ \theta & -\epsilon \end{pmatrix}, \hat{a} = \begin{pmatrix} 1 & \theta \\ \theta & \theta \end{pmatrix}, \hat{x} = \begin{pmatrix} \theta & 1 \\ \theta & \theta \end{pmatrix} \right\};$$

$$\left\{ \hat{a} \cdot \hat{x} - \hat{x} \cdot \hat{a} == \hat{x}, \hat{a} \cdot \hat{y} - \hat{y} \cdot \hat{a} == -\hat{y}, \hat{b} \cdot \hat{y} - \hat{y} \cdot \hat{b} == -\epsilon \hat{y}, \hat{b} \cdot \hat{x} - \hat{x} \cdot \hat{b} == \epsilon \hat{x}, \hat{x} \cdot \hat{y} - \hat{y} \cdot \hat{x} == \hat{b} + \epsilon \hat{a} \right\}$$

Out[]:= {True, True, True, True, True}

$$\text{In[]:= } \left\{ \hat{y} = \begin{pmatrix} \theta & \theta \\ 1 & \theta \end{pmatrix}, \hat{b} = \begin{pmatrix} 1 & \theta \\ \theta & \theta \end{pmatrix}, \hat{a} = \begin{pmatrix} \theta & \theta \\ \theta & -\epsilon^{-1} \end{pmatrix}, \hat{x} = \begin{pmatrix} \theta & 1 \\ \theta & \theta \end{pmatrix} \right\};$$

$$\text{Simplify@} \left\{ \hat{a} \cdot \hat{x} - \hat{x} \cdot \hat{a} == \hat{x}, \hat{a} \cdot \hat{y} - \hat{y} \cdot \hat{a} == -\hat{y}, \hat{b} \cdot \hat{y} - \hat{y} \cdot \hat{b} == -\epsilon \hat{y}, \hat{b} \cdot \hat{x} - \hat{x} \cdot \hat{b} == \epsilon \hat{x}, \hat{x} \cdot \hat{y} - \hat{y} \cdot \hat{x} == \hat{b} + \epsilon \hat{a} \right\}$$

Out[]:= $\left\{ \left\{ \left\{ \theta, \frac{1}{\epsilon} \right\}, \{ \theta, \theta \} \right\} == \{ \{ \theta, 1 \}, \{ \theta, \theta \} \}, \left\{ \{ \theta, \theta \}, \left\{ -\frac{1}{\epsilon}, \theta \right\} \right\} == \{ \{ \theta, \theta \}, \{ -1, \theta \} \}, \right.$
 $\left. \left\{ \{ \theta, \theta \}, \{ -1 + \epsilon, \theta \} \right\} == \{ \{ \theta, \theta \}, \{ \theta, \theta \} \}, \{ \{ \theta, 1 \}, \{ \theta, \theta \} \} == \{ \{ \theta, \epsilon \}, \{ \theta, \theta \} \}, \text{True} \right\}$

$$\text{In[]:= } \left\{ \hat{y} = \begin{pmatrix} \theta & \theta \\ \epsilon^{1/2} & \theta \end{pmatrix}, \hat{b} = \begin{pmatrix} \frac{1+\epsilon}{2} & \theta \\ \theta & \frac{1-\epsilon}{2} \end{pmatrix}, \hat{a} = \begin{pmatrix} \frac{1-\epsilon^{-1}}{2} & \theta \\ \theta & \frac{-1-\epsilon^{-1}}{2} \end{pmatrix}, \hat{x} = \begin{pmatrix} \theta & \epsilon^{1/2} \\ \theta & \theta \end{pmatrix} \right\};$$

$$\text{Simplify@} \left\{ \hat{a} \cdot \hat{x} - \hat{x} \cdot \hat{a} == \hat{x}, \hat{a} \cdot \hat{y} - \hat{y} \cdot \hat{a} == -\hat{y}, \hat{b} \cdot \hat{y} - \hat{y} \cdot \hat{b} == -\epsilon \hat{y}, \hat{b} \cdot \hat{x} - \hat{x} \cdot \hat{b} == \epsilon \hat{x}, \hat{x} \cdot \hat{y} - \hat{y} \cdot \hat{x} == \hat{b} + \epsilon \hat{a} \right\}$$

Out[]:= {True, True, True, True, True}