

Pensieve header: Experiments with exponential zipping.

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In[*]:= Unprotect[SeriesData];
SeriesData /: Expand[sd_SeriesData] := MapAt[Expand, sd, 3];
Protect[SeriesData];
z* =  $\zeta$ ;  $\zeta^*$  = z; Zip{}[P_] := P;
Zip{ $\zeta$ ,  $\zeta^*$ }[P_] := (Expand[P // Zip{ $\zeta$ ,  $\zeta^*$ }] /.  $f_.$   $\zeta^{d_}$   $\Rightarrow$   $\partial_{\{\zeta^*, d\}} f$ ) /.  $\zeta^* \rightarrow 0$ 

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$$\text{In[*]} := \text{Zip}_{\{\zeta\}} \left[\text{Series} \left[e^{\sum [a_{p,m,n} \epsilon^p z^m \zeta^n, \{p, 1, 3\}, \{m, 0, 3\}, \{n, 0, 3\}], \{\epsilon, 0, 3\}} \right] \right]$$

$$\begin{aligned} \text{Out[*]} = & 1 + \left(a_{1,0,0} + a_{1,1,1} + 2 a_{1,2,2} + 6 a_{1,3,3} \right) \epsilon + \\ & \left(\frac{1}{2} a_{1,0,0}^2 + a_{1,0,1} a_{1,1,0} + a_{1,0,0} a_{1,1,1} + a_{1,1,1}^2 + 2 a_{1,1,0} a_{1,1,2} + 2 a_{1,0,2} a_{1,2,0} + \right. \\ & 6 a_{1,1,3} a_{1,2,0} + 2 a_{1,0,1} a_{1,2,1} + 6 a_{1,1,2} a_{1,2,1} + 2 a_{1,0,0} a_{1,2,2} + 6 a_{1,1,1} a_{1,2,2} + \\ & 12 a_{1,2,2}^2 + 6 a_{1,1,0} a_{1,2,3} + 24 a_{1,2,1} a_{1,2,3} + 6 a_{1,0,3} a_{1,3,0} + 6 a_{1,0,2} a_{1,3,1} + \\ & 24 a_{1,1,3} a_{1,3,1} + 6 a_{1,0,1} a_{1,3,2} + 24 a_{1,1,2} a_{1,3,2} + 120 a_{1,2,3} a_{1,3,2} + 6 a_{1,0,0} a_{1,3,3} + \\ & \left. 24 a_{1,1,1} a_{1,3,3} + 120 a_{1,2,2} a_{1,3,3} + 360 a_{1,3,3}^2 + a_{2,0,0} + a_{2,1,1} + 2 a_{2,2,2} + 6 a_{2,3,3} \right) \epsilon^2 + \\ & \left(\frac{1}{6} a_{1,0,0}^3 + a_{1,0,0} a_{1,0,1} a_{1,1,0} + a_{1,0,2} a_{1,1,0}^2 + \frac{1}{2} a_{1,0,0}^2 a_{1,1,1} + 2 a_{1,0,1} a_{1,1,0} a_{1,1,1} + a_{1,0,0} a_{1,1,1}^2 + \right. \\ & a_{1,1,1}^3 + 2 a_{1,0,0} a_{1,1,0} a_{1,1,2} + 6 a_{1,1,0} a_{1,1,1} a_{1,1,2} + 3 a_{1,1,0}^2 a_{1,1,3} + a_{1,0,1}^2 a_{1,2,0} + 2 a_{1,0,0} a_{1,0,2} a_{1,2,0} + \\ & 6 a_{1,0,3} a_{1,1,0} a_{1,2,0} + 6 a_{1,0,2} a_{1,1,1} a_{1,2,0} + 6 a_{1,0,1} a_{1,1,2} a_{1,2,0} + 12 a_{1,1,2}^2 a_{1,2,0} + \\ & 6 a_{1,0,0} a_{1,1,3} a_{1,2,0} + 24 a_{1,1,1} a_{1,1,3} a_{1,2,0} + 2 a_{1,0,0} a_{1,0,1} a_{1,2,1} + 6 a_{1,0,2} a_{1,1,0} a_{1,2,1} + \\ & 6 a_{1,0,1} a_{1,1,1} a_{1,2,1} + 6 a_{1,0,0} a_{1,1,2} a_{1,2,1} + 24 a_{1,1,1} a_{1,1,2} a_{1,2,1} + 24 a_{1,1,0} a_{1,1,3} a_{1,2,1} + \\ & 24 a_{1,0,3} a_{1,2,0} a_{1,2,1} + 12 a_{1,0,2} a_{1,2,1}^2 + 60 a_{1,1,3} a_{1,2,1}^2 + a_{1,0,0}^2 a_{1,2,2} + 6 a_{1,0,1} a_{1,1,0} a_{1,2,2} + \\ & 6 a_{1,0,0} a_{1,1,1} a_{1,2,2} + 12 a_{1,1,1}^2 a_{1,2,2} + 24 a_{1,1,0} a_{1,1,2} a_{1,2,2} + 24 a_{1,0,2} a_{1,2,0} a_{1,2,2} + \\ & 120 a_{1,1,3} a_{1,2,0} a_{1,2,2} + 24 a_{1,0,1} a_{1,2,1} a_{1,2,2} + 120 a_{1,1,2} a_{1,2,1} a_{1,2,2} + 12 a_{1,0,0} a_{1,2,2}^2 + \\ & 60 a_{1,1,1} a_{1,2,2}^2 + 120 a_{1,2,2}^3 + 6 a_{1,0,0} a_{1,1,0} a_{1,2,3} + 24 a_{1,1,0} a_{1,1,1} a_{1,2,3} + 24 a_{1,0,1} a_{1,2,0} a_{1,2,3} + \\ & 120 a_{1,1,2} a_{1,2,0} a_{1,2,3} + 24 a_{1,0,0} a_{1,2,1} a_{1,2,3} + 120 a_{1,1,1} a_{1,2,1} a_{1,2,3} + 120 a_{1,1,0} a_{1,2,2} a_{1,2,3} + \\ & 720 a_{1,2,1} a_{1,2,2} a_{1,2,3} + 360 a_{1,2,0} a_{1,2,3}^2 + 6 a_{1,0,1} a_{1,0,2} a_{1,3,0} + 6 a_{1,0,0} a_{1,0,3} a_{1,3,0} + \\ & 24 a_{1,0,3} a_{1,1,1} a_{1,3,0} + 24 a_{1,0,2} a_{1,1,2} a_{1,3,0} + 24 a_{1,0,1} a_{1,1,3} a_{1,3,0} + 120 a_{1,1,2} a_{1,1,3} a_{1,3,0} + \\ & 120 a_{1,0,3} a_{1,2,2} a_{1,3,0} + 120 a_{1,0,2} a_{1,2,3} a_{1,3,0} + 720 a_{1,1,3} a_{1,2,3} a_{1,3,0} + 3 a_{1,0,1}^2 a_{1,3,1} + \\ & 6 a_{1,0,0} a_{1,0,2} a_{1,3,1} + 24 a_{1,0,3} a_{1,1,0} a_{1,3,1} + 24 a_{1,0,2} a_{1,1,1} a_{1,3,1} + 24 a_{1,0,1} a_{1,1,2} a_{1,3,1} + \\ & 60 a_{1,1,2}^2 a_{1,3,1} + 24 a_{1,0,0} a_{1,1,3} a_{1,3,1} + 120 a_{1,1,1} a_{1,1,3} a_{1,3,1} + 120 a_{1,0,3} a_{1,2,1} a_{1,3,1} + \\ & 120 a_{1,0,2} a_{1,2,2} a_{1,3,1} + 720 a_{1,1,3} a_{1,2,2} a_{1,3,1} + 120 a_{1,0,1} a_{1,2,3} a_{1,3,1} + 720 a_{1,1,2} a_{1,2,3} a_{1,3,1} + \\ & 2520 a_{1,2,3}^2 a_{1,3,1} + 6 a_{1,0,0} a_{1,0,1} a_{1,3,2} + 24 a_{1,0,2} a_{1,1,0} a_{1,3,2} + 24 a_{1,0,1} a_{1,1,1} a_{1,3,2} + \\ & 24 a_{1,0,0} a_{1,1,2} a_{1,3,2} + 120 a_{1,1,1} a_{1,1,2} a_{1,3,2} + 120 a_{1,1,0} a_{1,1,3} a_{1,3,2} + 120 a_{1,0,3} a_{1,2,0} a_{1,3,2} + \\ & 120 a_{1,0,2} a_{1,2,1} a_{1,3,2} + 720 a_{1,1,3} a_{1,2,1} a_{1,3,2} + 120 a_{1,0,1} a_{1,2,2} a_{1,3,2} + 720 a_{1,1,2} a_{1,2,2} a_{1,3,2} + \\ & 120 a_{1,0,0} a_{1,2,3} a_{1,3,2} + 720 a_{1,1,1} a_{1,2,3} a_{1,3,2} + 5040 a_{1,2,2} a_{1,2,3} a_{1,3,2} + 720 a_{1,0,3} a_{1,3,1} a_{1,3,2} + \\ & 360 a_{1,0,2} a_{1,3,2}^2 + 2520 a_{1,1,3} a_{1,3,2}^2 + 3 a_{1,0,0}^2 a_{1,3,3} + 24 a_{1,0,1} a_{1,1,0} a_{1,3,3} + 24 a_{1,0,0} a_{1,1,1} a_{1,3,3} + \\ & 60 a_{1,1,1}^2 a_{1,3,3} + 120 a_{1,1,0} a_{1,1,2} a_{1,3,3} + 120 a_{1,0,2} a_{1,2,0} a_{1,3,3} + 720 a_{1,1,3} a_{1,2,0} a_{1,3,3} + \\ & 120 a_{1,0,1} a_{1,2,1} a_{1,3,3} + 720 a_{1,1,2} a_{1,2,1} a_{1,3,3} + 120 a_{1,0,0} a_{1,2,2} a_{1,3,3} + 720 a_{1,1,1} a_{1,2,2} a_{1,3,3} + \\ & 2520 a_{1,2,2}^2 a_{1,3,3} + 720 a_{1,1,0} a_{1,2,3} a_{1,3,3} + 5040 a_{1,2,1} a_{1,2,3} a_{1,3,3} + 720 a_{1,0,3} a_{1,3,0} a_{1,3,3} + \\ & 720 a_{1,0,2} a_{1,3,1} a_{1,3,3} + 5040 a_{1,1,3} a_{1,3,1} a_{1,3,3} + 720 a_{1,0,1} a_{1,3,2} a_{1,3,3} + 5040 a_{1,1,2} a_{1,3,2} a_{1,3,3} + \\ & 40320 a_{1,2,3} a_{1,3,2} a_{1,3,3} + 360 a_{1,0,0} a_{1,3,3}^2 + 2520 a_{1,1,1} a_{1,3,3}^2 + 20160 a_{1,2,2} a_{1,3,3}^2 + 60480 a_{1,3,3}^3 + \\ & a_{1,0,0} a_{2,0,0} + a_{1,1,1} a_{2,0,0} + 2 a_{1,2,2} a_{2,0,0} + 6 a_{1,3,3} a_{2,0,0} + a_{1,1,0} a_{2,0,1} + 2 a_{1,2,1} a_{2,0,1} + \\ & 6 a_{1,3,2} a_{2,0,1} + 2 a_{1,2,0} a_{2,0,2} + 6 a_{1,3,1} a_{2,0,2} + 6 a_{1,3,0} a_{2,0,3} + a_{1,0,1} a_{2,1,0} + 2 a_{1,1,2} a_{2,1,0} + \\ & 6 a_{1,2,3} a_{2,1,0} + a_{1,0,0} a_{2,1,1} + 2 a_{1,1,1} a_{2,1,1} + 6 a_{1,2,2} a_{2,1,1} + 24 a_{1,3,3} a_{2,1,1} + 2 a_{1,1,0} a_{2,1,2} + \\ & 6 a_{1,2,1} a_{2,1,2} + 24 a_{1,3,2} a_{2,1,2} + 6 a_{1,2,0} a_{2,1,3} + 24 a_{1,3,1} a_{2,1,3} + 2 a_{1,0,2} a_{2,2,0} + 6 a_{1,1,3} a_{2,2,0} + \\ & 2 a_{1,0,1} a_{2,2,1} + 6 a_{1,1,2} a_{2,2,1} + 24 a_{1,2,3} a_{2,2,1} + 2 a_{1,0,0} a_{2,2,2} + 6 a_{1,1,1} a_{2,2,2} + 24 a_{1,2,2} a_{2,2,2} + \\ & 120 a_{1,3,3} a_{2,2,2} + 6 a_{1,1,0} a_{2,2,3} + 24 a_{1,2,1} a_{2,2,3} + 120 a_{1,3,2} a_{2,2,3} + 6 a_{1,0,3} a_{2,3,0} + \\ & 6 a_{1,0,2} a_{2,3,1} + 24 a_{1,1,3} a_{2,3,1} + 6 a_{1,0,1} a_{2,3,2} + 24 a_{1,1,2} a_{2,3,2} + 120 a_{1,2,3} a_{2,3,2} + 6 a_{1,0,0} a_{2,3,3} + \\ & \left. 24 a_{1,1,1} a_{2,3,3} + 120 a_{1,2,2} a_{2,3,3} + 720 a_{1,3,3} a_{2,3,3} + a_{3,0,0} + a_{3,1,1} + 2 a_{3,2,2} + 6 a_{3,3,3} \right) \epsilon^3 + 0[\epsilon]^4 \end{aligned}$$