

Series[e^{x+y} , {x, 0, 3}, {y, 0, 4}]

$$\left(1 + y + \frac{y^2}{2} + \frac{y^3}{6} + \frac{y^4}{24} + O[y]^5\right) + \left(1 + y + \frac{y^2}{2} + \frac{y^3}{6} + \frac{y^4}{24} + O[y]^5\right) x +$$

$$\left(\frac{1}{2} + \frac{y}{2} + \frac{y^2}{4} + \frac{y^3}{12} + \frac{y^4}{48} + O[y]^5\right) x^2 + \left(\frac{1}{6} + \frac{y}{6} + \frac{y^2}{12} + \frac{y^3}{36} + \frac{y^4}{144} + O[y]^5\right) x^3 + O[x]^4$$

ser = Sum[a[i, j] xⁱ y^j, {i, 0, 3}, {j, 0, 2}]

$$a[0, 0] + ya[0, 1] + y^2 a[0, 2] + xa[1, 0] + xya[1, 1] + xy^2 a[1, 2] +$$

$$x^2 a[2, 0] + x^2 ya[2, 1] + x^2 y^2 a[2, 2] + x^3 a[3, 0] + x^3 ya[3, 1] + x^3 y^2 a[3, 2]$$

ser1 = (ser /. {x → x h, y → y h}) + O[h]^3

$$a[0, 0] + (ya[0, 1] + xa[1, 0]) h + (y^2 a[0, 2] + xya[1, 1] + x^2 a[2, 0]) h^2 + O[h]^3$$

ser1²

$$a[0, 0]^2 + 2 a[0, 0] (ya[0, 1] + xa[1, 0]) h +$$

$$\left((ya[0, 1] + xa[1, 0])^2 + 2 a[0, 0] (y^2 a[0, 2] + xya[1, 1] + x^2 a[2, 0])\right) h^2 + O[h]^3$$