

# Non Commutative Gaussian Elimination @ HUJI

Pensieve Header: NCGE games towards a HUJI class.

## Program 0

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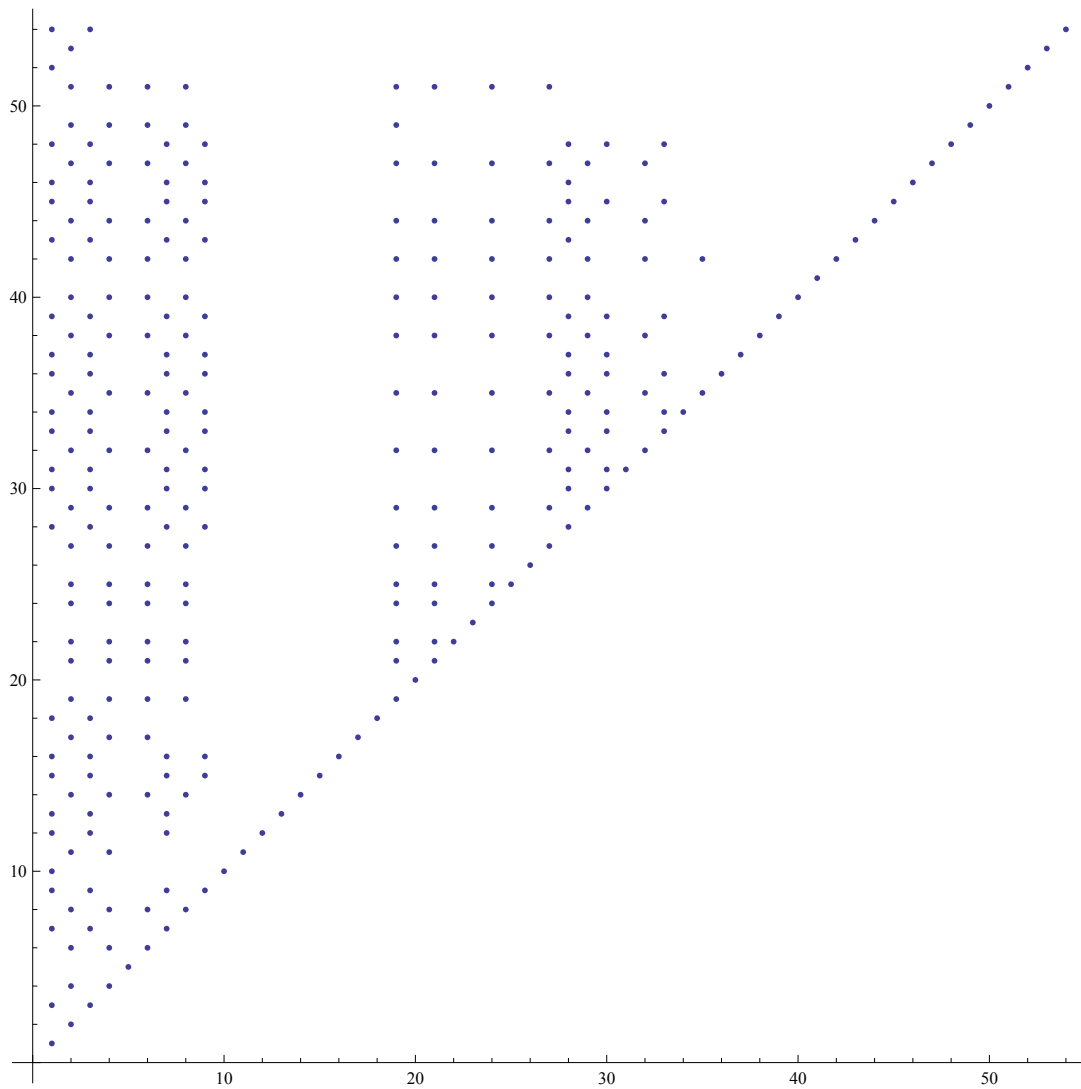
gs = {purple = P[18, 27, 36, 4, 5, 6, 7, 8, 9, 3, 11, 12, 13, 14, 15,
  16, 17, 45, 2, 20, 21, 22, 23, 24, 25, 26, 44, 1, 29, 30, 31, 32, 33, 34, 35,
  43, 37, 38, 39, 40, 41, 42, 10, 19, 28, 52, 49, 46, 53, 50, 47, 54, 51, 48],
white = P[1, 2, 3, 4, 5, 6, 16, 25, 34, 10, 11, 9, 15, 24, 33, 39, 17, 18, 19,
  20, 8, 14, 23, 32, 38, 26, 27, 28, 29, 7, 13, 22, 31, 37, 35, 36, 12,
  21, 30, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 52, 53, 54],
green = P[1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20,
  21, 22, 23, 24, 25, 26, 27, 31, 32, 33, 34, 35, 36, 48, 47, 46, 39,
  42, 45, 38, 41, 44, 37, 40, 43, 30, 29, 28, 49, 50, 51, 52, 53, 54],
blue = P[3, 6, 9, 2, 5, 8, 1, 4, 7, 54, 53, 52, 10, 11, 12, 13, 14, 15, 19, 20,
  21, 22, 23, 24, 25, 26, 27, 28, 29, 30, 31, 32, 33, 34, 35, 36, 37,
  38, 39, 40, 41, 42, 43, 44, 45, 46, 47, 48, 49, 50, 51, 18, 17, 16],
red = P[13, 2, 3, 22, 5, 6, 31, 8, 9, 12, 21, 30, 37, 14, 15, 16, 17, 18, 11,
  20, 29, 40, 23, 24, 25, 26, 27, 10, 19, 28, 43, 32, 33, 34, 35, 36,
  46, 38, 39, 49, 41, 42, 52, 44, 45, 1, 47, 48, 4, 50, 51, 7, 53, 54],
yellow = P[1, 2, 48, 4, 5, 51, 7, 8, 54, 10, 11, 12, 13, 14, 3, 18, 27, 36, 19,
  20, 21, 22, 23, 6, 17, 26, 35, 28, 29, 30, 31, 32, 9, 16, 25, 34, 37,
  38, 15, 40, 41, 24, 43, 44, 33, 46, 47, 39, 49, 50, 42, 52, 53, 45]};

($RecursionLimit = 2^16;
n = 54;
P /: p_P**P[a___] := p[{{a}}];
Inv[p_P] := P@@Ordering[p];
Feed[P@@Range[n]] := Null;
Feed[p_P] := Module[{i, j},
  For[i = 1, p[[i]] == i, ++i]; j = p[[i]];
  If[Head[s[i, j]] === P,
    Feed[Inv[s[i, j]]**p],
    (*Else*)s[i, j] = p;
  Do[If[Head[s[k, 1]] == P,
    Feed[s[i, j]**s[k, 1]];
    Feed[s[k, 1]**s[i, j]]
  ],
  {k, n}, {1, n}
];
);

(Feed[#]; Product[1 + Length[Select[Range[n], Head[s[i, #]] === P &]], {i, n}]) &/@gs
{4, 16, 159 993 501 696 000, 21 119 142 223 872 000, 43 252 003 274 489 856 000, 43 252 003 274 489 856 000}

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Images[i_] := {i}~Join~Select[Range[n], Head[s[i, #]] === P &];
ListPlot[
  Join@@Table[{i, #} & /@ Images[i], {i, n}],
  AspectRatio -> 1
]
```



$$43\,252\,003\,274\,489\,856\,000 / (8! * 3^8 * 12! * 2^{12})$$

$$\frac{1}{12}$$