

page 197-198 / scan page 106-107:

We introduce the following two maps. For $X \in \text{Ob}(\mathcal{M}_{\mathfrak{g}})$, let X^0 denote the vector space X equipped with the trivial \mathfrak{g} -action. By Frobenius reciprocity, the map

$$\theta_X : \text{Hom}_{\mathfrak{g}}(M_- \otimes X^0, M_+^* \otimes X) \rightarrow \text{Hom}_k(X^0, X)$$

$$f \mapsto (1_+ \otimes 1) \circ f \circ (1_- \otimes 1)$$

is an isomorphism. We set

$$\psi = \theta_{M_-}^{-1}(1) : M_- \otimes M_- \rightarrow M_+^* \otimes M_-$$

and

$$\eta = \psi(1_- \otimes \cdot) : M_- \rightarrow M_+^* \otimes M_-.$$

Lemma 21.1. *The formulas for the product and coproduct in $U_h(\mathfrak{g}_+)$ can be written as follows:*

$$m : M_- \otimes M_- \xrightarrow{\sigma} M_- \otimes M_- \xrightarrow{\eta \otimes 1} (M_+^* \otimes M_-) \otimes M_-$$

$$\xrightarrow{\Phi} M_+^* \otimes (M_- \otimes M_-) \xrightarrow{1 \otimes \psi} M_+^* \otimes (M_+^* \otimes M_-) \quad (21.5)$$

$$\xrightarrow{1_+ \otimes 1 \otimes 1} M_+^* \otimes M_- \xrightarrow{1_+ \otimes 1} M_-,$$

$$\Delta : M_- \xrightarrow{i_-} M_- \otimes M_- \xrightarrow{J^{-1}} M_- \otimes M_-, \quad (21.6)$$

where J is the composition

$$M_- \otimes M_- \xrightarrow{\eta \otimes \eta} (M_+^* \otimes M_-) \otimes (M_+^* \otimes M_-) \xrightarrow{\Phi_{2,3,4}^{-1} \Phi_{1,2,3,4}} M_+^* \otimes ((M_+^* \otimes M_-) \otimes M_-)$$

$$\xrightarrow{\beta_{23}^{-1}} M_+^* \otimes ((M_- \otimes M_+^*) \otimes M_-) \xrightarrow{\Phi_{1,2,3,4}^{-1} \Phi_{2,3,4}} (M_+^* \otimes M_+^*) \otimes (M_- \otimes M_-)$$

$$\xrightarrow{(1_+ \otimes 1_+)^{\otimes 1}} M_- \otimes M_-. \quad (21.7)$$

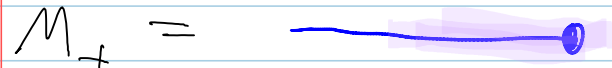
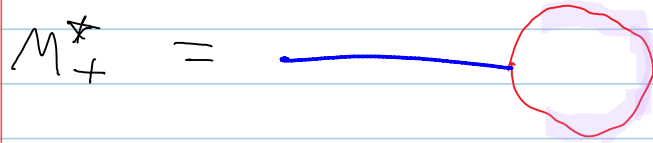
Proof: We leave it to the reader to check that these indeed coincide with formulas (21.2) and (21.4).

WTF!

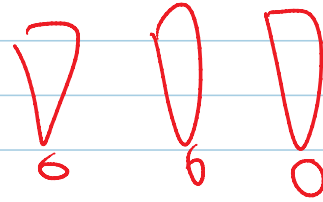
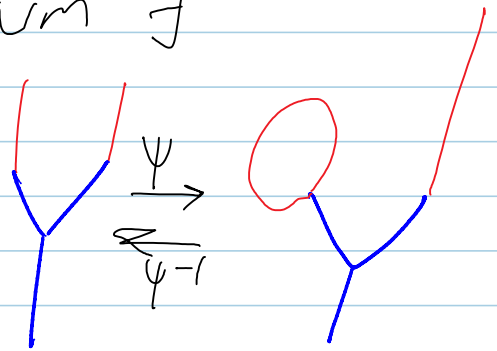
I need to add here their formulas for R .

... These don't seem to exist...

In the w case:

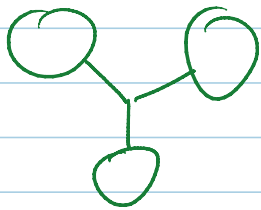



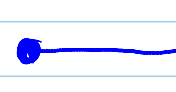
claim \exists



Is there another story?

Too easy?



Q. Is there a sense by which  is dual to ?