Dror Bar-Natan: Talks: HUJI-1912:

Some Feynman Diagrams in Pure Algebra

With Roland
van der Veen

Thanks for allowing me at the Hebrew U!
ωεβ:=http://drorbn.net/hu19
Slides w/ no handout/URL should be banned!

Abstract. I will explain how Feynman diagrams arise in pure algebra: how the computation of compositions of maps of a certain natural class, from one polynomial ring into another, naturally leads to a certain composition operation of quadratics and to Feynman diagrams.

I will also explain, with very little detail, how this is used in the construction of some very well-behaved poly-time computable knot polynomials, and then with better detail, why I care about having such invariants.

The PBW Principle Many algebras are isomorphic as vector spaces to polynomial algebras. So we want to understand arbitrary linear maps between polynomial algebras.

Gentle Agreement. Everything converges!

Convention. For a finite set A, let $z_A := \{z_i\}_{i\in A}$ and let $\zeta_A := \{z_i^* = \zeta_i\}_{i\in A}$. $(y,b,a,x)^* = (\eta,\beta,\alpha,\xi)$

The Generating Series $\mathcal{G}$: $\operatorname{Hom}(\mathbb{Q}[z_A]\to\mathbb{Q}[z_B]) \to \mathbb{Q}[\![\zeta_A, z_B]\!]$.

Claim. $L\in\operatorname{Hom}(\mathbb{Q}[z_A]\to\mathbb{Q}[z_B]) \underset{\mathcal{G}}{\xrightarrow{\sim}} \mathbb{Q}[z_B][\![\zeta_A]\!] \ni \mathcal{L}$ via

$$\mathcal{G}(L) := \sum_{n\in\mathbb{N}^A}\frac{\zeta_A^n}{n!}L(z_A^n) = L\left(\mathbb{e}^{\sum_{a\in A}\zeta_a z_a}\right) = \mathcal{L} = {}_{\text{greek}}\mathcal{L}_{\text{latin}},$$

$$\mathcal{G}^{-1}(\mathcal{L})(p) = \left(p|_{z_a\to\partial_{\zeta_a}}\mathcal{L}\right)_{\zeta_a=0} \quad \text{for } p\in\mathbb{Q}[z_A].$$

Claim. If $L\in\operatorname{Hom}(\mathbb{Q}[z_A]\to\mathbb{Q}[z_B])$, $M\in\operatorname{Hom}(\mathbb{Q}[z_B]\to\mathbb{Q}[z_C])$, then $\mathcal{G}(L/\!\!/M) = \left(\mathcal{G}(L)|_{z_b\to\partial_{\zeta_b}}\mathcal{G}(M)\right)_{\zeta_b=0}$.

Basic Examples. 1. $\mathcal{G}(id\colon \mathbb{Q}[y,a,x]\to\mathbb{Q}[y,a,x]) = \mathbb{e}^{\eta y+\alpha a+\xi x}$.

2. The standard commutative product m_k^{ij} of polynomials is given by $z_i, z_j \to z_k$. Hence $\mathcal{G}(m_k^{ij}) = m_k^{ij}(\mathbb{e}^{\zeta_i z_i+\zeta_j z_j}) = \mathbb{e}^{(\zeta_i+\zeta_j)z_k}$.

$$\begin{tikzcd}
\mathbb{Q}[z]_i\otimes\mathbb{Q}[z]_j \arrow[r, "m_k^{ij}"] \arrow[d, equal] & \mathbb{Q}[z]_k \arrow[d, equal] \\
\mathbb{Q}[z_i,z_j] \arrow[r, "m_k^{ij}"] & \mathbb{Q}[z_k]
\end{tikzcd}$$

3. The standard co-commutative co-product Δ^i_{jk} of polynomials is given by $z_i \to z_j + z_k$. Hence $\mathcal{G}(\Delta^i_{jk}) = \Delta^i_{jk}(\mathbb{e}^{\zeta_i z_i}) = \mathbb{e}^{\zeta_i(z_j+z_k)}$.

$$\begin{tikzcd}
\mathbb{Q}[z]_i \arrow[r, "\Delta^i_{jk}"] \arrow[d, equal] & \mathbb{Q}[z]_j\otimes\mathbb{Q}[z]_k \arrow[d, equal] \\
\mathbb{Q}[z_i] \arrow[r, "\Delta^i_{jk}"] & \mathbb{Q}[z_j,z_k]
\end{tikzcd}$$

Heisenberg Algebras. Let $\mathbb{H} = \langle x,y\rangle/[x,y]=\hbar$ (with $\hbar$ a scalar), let $\mathbb{O}_i\colon\mathbb{Q}[x_i,y_i]\to\mathbb{H}_i$ is the "x before y" PBW ordering map and let hm_k^{ij} be the composition

$$\mathbb{Q}[x_i,y_i,x_j,y_j] \xrightarrow{\mathbb{O}_i\otimes\mathbb{O}_j} \mathbb{H}_i\otimes\mathbb{H}_j \xrightarrow{m_k^{ij}} \mathbb{H}_k \xrightarrow{\mathbb{O}_k^{-1}} \mathbb{Q}[x_k,y_k].$$

Then $\mathcal{G}(hm_k^{ij}) = \mathbb{e}^{\Lambda_\hbar}$, where $\Lambda_\hbar = -\hbar\eta_i\xi_j + (\xi_i+\xi_j)x_k + (\eta_i+\eta_j)y_k$.

Proof 1. Recall the "Weyl form of the CCR" $\mathbb{e}^{\eta y}\mathbb{e}^{\xi x} = \mathbb{e}^{-\hbar\eta\xi}\mathbb{e}^{\xi x}\mathbb{e}^{\eta y}$, and compute

$$\begin{aligned}\mathcal{G}(hm_k^{ij}) &= \mathbb{e}^{\xi_i x_i+\eta_i y_i+\xi_j x_j+\eta_j y_j}/\!\!/\mathbb{O}_i\otimes\mathbb{O}_j/\!\!/m_k^{ij}/\!\!/\mathbb{O}_k^{-1} \\
&= \mathbb{e}^{\xi_i x_i}\mathbb{e}^{\eta_i y_i}\mathbb{e}^{\xi_j x_j}\mathbb{e}^{\eta_j y_j}/\!\!/m_k^{ij}/\!\!/\mathbb{O}_k^{-1} = \mathbb{e}^{\xi_i x_k}\mathbb{e}^{\eta_i y_k}\mathbb{e}^{\xi_j x_k}\mathbb{e}^{\eta_j y_k}/\!\!/\mathbb{O}_k^{-1} \\
&= \mathbb{e}^{-\hbar\eta_i\xi_j}\mathbb{e}^{(\xi_i+\xi_j)x_k}\mathbb{e}^{(\eta_i+\eta_j)y_k}/\!\!/\mathbb{O}_k^{-1} = \mathbb{e}^{\Lambda_\hbar}.\end{aligned}$$

Proof 2. We compute in a faithful 3D representation ρ of $\mathbb{H}$: (ωεβ/hm)

$$\left\{\hat{x} = \begin{pmatrix}0&1&0\\0&0&0\\0&0&0\end{pmatrix}, \hat{y} = \begin{pmatrix}0&0&0\\0&0&\hbar\\0&0&0\end{pmatrix}, \hat{c} = \begin{pmatrix}0&0&1\\0&0&0\\0&0&0\end{pmatrix}\right\};$$

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{x̂.ŷ - ŷ.x̂ == ℏ ĉ, x̂.ĉ == ĉ.x̂, ŷ.ĉ == ĉ.ŷ}
{True, True, True}
```

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Λ = -ℏ ηi ξj ck + (ξi + ξj) xk + (ηi + ηj) yk;
Simplify@With[{𝔼 = MatrixExp},
  𝔼[x̂ ξi].𝔼[ŷ ηi].𝔼[x̂ ξj].𝔼[ŷ ηj] ==
   𝔼[x̂ ∂xk Λ].𝔼[ŷ ∂yk Λ].𝔼[ĉ ∂ck Λ]]
True
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A Real DoPeGDO Example (DoPeGDO:=Docile Perturbed Gaussian Differential Operators). Let $sl_{2+}^\epsilon := L\langle y,b,a,x\rangle$ subject to $[a,x]=x$, $[b,y]=-\epsilon y$, $[a,b]=0$, $[a,y]=-y$, $[b,x]=\epsilon x$, and $[x,y]=\epsilon a+b$. So $t:=\epsilon a-b$ is central and if $\exists\epsilon^{-1}$, $sl_{2+}^\epsilon\cong sl_2\oplus\langle t\rangle$. Let $CU := \mathcal{U}(sl_{2+}^\epsilon)$, and let cm_k^{ij} be the composition below, where $\mathbb{O}_i\colon\mathbb{Q}[y_i,b_i,a_i,x_i]\to CU_i$ be the PBW ordering map in the order $ybax$:

$$\begin{tikzcd}
CU_i\otimes CU_j \arrow[r, "m_k^{ij}"] & CU_k \\
\mathbb{Q}[y_i,b_i,a_i,x_i,y_j,b_j,a_j,x_j] \arrow[u, "\mathbb{O}_{i,j}"'] \arrow[r, "cm_k^{ij}"] & \mathbb{Q}[y_k,b_k,a_k,x_k] \arrow[u, "\mathbb{O}_k"']
\end{tikzcd}$$

Claim. Let (all brawn and no brains)

$$\begin{aligned}\Lambda = \left(\eta_i + \frac{e^{-\alpha_i-\epsilon\beta_i}\eta_j}{1+\epsilon\eta_j\xi_i}\right)y_k + \left(\beta_i+\beta_j+\frac{\log\left(1+\epsilon\eta_j\xi_i\right)}{\epsilon}\right)b_k + \\
\left(\alpha_i+\alpha_j+\log\left(1+\epsilon\eta_j\xi_i\right)\right)a_k + \left(\frac{e^{-\alpha_j-\epsilon\beta_j}\xi_i}{1+\epsilon\eta_j\xi_i}+\xi_j\right)x_k\end{aligned}$$

Then $\mathbb{e}^{\eta_i y_i+\beta_i b_i+\alpha_i a_i+\xi_i x_i+\eta_j y_j+\beta_j b_j+\alpha_j a_j+\xi_j x_j}/\!\!/\mathbb{O}_{i,j}/\!\!/cm_k^{ij} = \mathbb{e}^\Lambda/\!\!/\mathbb{O}_k$, and hence $\mathcal{G}(cm_k^{ij}) = \mathbb{e}^\Lambda$.

Proof. We compute in a faithful 2D representation ρ of CU: (ωεβ/sl2)

$$\left\{\hat{y} = \begin{pmatrix}0&0\\\epsilon&0\end{pmatrix}, \hat{b} = \begin{pmatrix}0&0\\0&-\epsilon\end{pmatrix}, \hat{a} = \begin{pmatrix}1&0\\0&0\end{pmatrix}, \hat{x} = \begin{pmatrix}0&1\\0&0\end{pmatrix}\right\};$$

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{â.x̂ - x̂.â == x̂, â.ŷ - ŷ.â == -ŷ, b̂.ŷ - ŷ.b̂ == -ϵ ŷ,
 b̂.x̂ - x̂.b̂ == ϵ x̂, x̂.ŷ - ŷ.x̂ == b̂ + ϵ â}
{True, True, True, True, True}
Simplify@With[{𝔼 = MatrixExp},
  𝔼[ηi ŷ].𝔼[βi b̂].𝔼[αi â].𝔼[ξi x̂].𝔼[ηj ŷ].𝔼[βj b̂].
   𝔼[αj â].𝔼[ξj x̂] == 𝔼[ŷ ∂yk Λ].𝔼[b̂ ∂bk Λ].𝔼[â ∂ak Λ].
   𝔼[x̂ ∂xk Λ]]
True
Series[Λ, {ϵ, 0, 2}]
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$$\begin{aligned}&(a_k\,(\alpha_i+\alpha_j) + y_k\,(\eta_i + \mathbb{e}^{-\alpha_i}\,\eta_j) + \\
&\quad b_k\,(\beta_i+\beta_j+\eta_j\,\xi_i) + x_k\,(\mathbb{e}^{-\alpha_j}\,\xi_i+\xi_j)) + \\
&\left(a_k\,\eta_j\,\xi_i - \frac{1}{2}\,b_k\,\eta_j^2\,\xi_i^2 - \mathbb{e}^{-\alpha_i}\,y_k\,\eta_j\,(\beta_i+\eta_j\,\xi_i) - \right.\\
&\quad\left.\mathbb{e}^{-\alpha_j}\,x_k\,\xi_i\,(\beta_j+\eta_j\,\xi_i)\right)\epsilon + \\
&\left(-\frac{1}{2}\,a_k\,\eta_j^2\,\xi_i^2 + \frac{1}{3}\,b_k\,\eta_j^3\,\xi_i^3 + \frac{1}{2}\,\mathbb{e}^{-\alpha_i}\,y_k\,\eta_j\,\left(\beta_i^2 + 2\,\beta_i\,\eta_j\,\xi_i + 2\,\eta_j^2\,\xi_i^2\right) + \right.\\
&\quad\left.\frac{1}{2}\,\mathbb{e}^{-\alpha_j}\,x_k\,\xi_i\,\left(\beta_j^2 + 2\,\beta_j\,\eta_j\,\xi_i + 2\,\eta_j^2\,\xi_i^2\right)\right)\epsilon^2 + \mathrm{O}[\epsilon]^3\end{aligned}$$

Note 1. If the lower half of the alphabet (a,b,α,β) is regarded as constants, then $\Lambda = C + Q + \sum_{k\geq1}\epsilon^k P^{(k)}$ is a docile perturbed Gaussian relative to the upper half of the alphabet (x,y,ξ,η): C is a scalar, Q is a quadratic, and $\deg P^{(k)}\leq 2k+2$.

Note 2. $\mathrm{wt}(x,y,\xi,\eta;a,b,\alpha,\beta;\epsilon) = (1,1,1,1;2,0,0,2;-2)$.

Quadratic Casimirs. If $c\in\mathfrak{g}\otimes\mathfrak{g}$ is the quadratic Casimir of a semi-simple Lie algebra $\mathfrak{g}$, then $\mathbb{e}^c$, regarded by PBW as an element of $\mathcal{S}^{\otimes2} = \operatorname{Hom}\left(\mathcal{S}(\mathfrak{g})^{\otimes0}\to\mathcal{S}(\mathfrak{g})^{\otimes2}\right)$, has a latin-latin dominant Gaussian factor. Likewise for R-matrices.

(baby) **DoPeGDO** := The category with objects finite sets$^{\dagger 1}$ and

$$\mathrm{mor}(A \to B) = \{\mathcal{L} = \omega \exp(Q + P)\} \subset \mathbb{Q}[\![\zeta_A, z_B, \epsilon]\!],$$

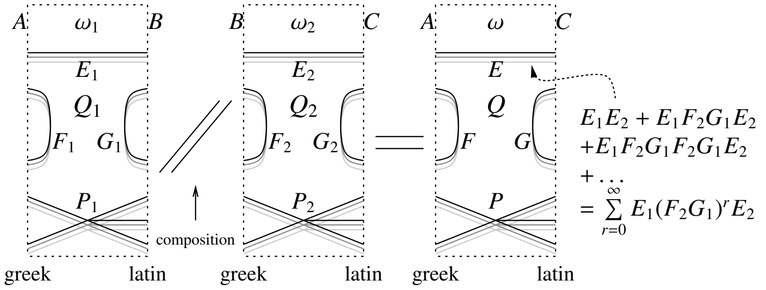
where: • ω is a scalar.$^{\dagger 2}$ • Q is a "small" ϵ-free quadratic in $\zeta_A \cup z_B$.$^{\dagger 3}$ • P is a "docile perturbation": $P = \sum_{k \geq 1} \epsilon^k P^{(k)}$, where $\deg P^{(k)} \leq 2k + 2$.$^{\dagger 4}$ • Compositions:$^{\dagger 6}$ $\mathcal{L} /\!\!/ \mathcal{M} := \left(\mathcal{L}|_{z_i \to \partial_{\zeta_i}} \mathcal{M} \right)_{\zeta_i = 0}$.

So What? If V is a representation, then $V^{\otimes n}$ explodes as a function of n, while in **DoPeGDO** up to a fixed power of ϵ, the ranks of $\mathrm{mor}(A \to B)$ grow polynomially as a function of $|A|$ and $|B|$.

Compositions. In $\mathrm{mor}(A \to B)$,

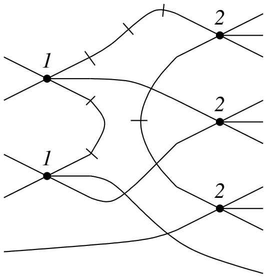
$$Q = \sum_{i \in A, j \in B} E_{ij} \zeta_i z_j + \frac{1}{2} \sum_{i,j \in A} F_{ij} \zeta_i \zeta_j + \frac{1}{2} \sum_{i,j \in B} G_{ij} z_i z_j,$$

and so (remember, $e^x = 1 + x + xx/2 + xxx/6 + \ldots$)



where • $E = E_1(I - F_2G_1)^{-1}E_2$.

- $F = F_1 + E_1F_2(I - G_1F_2)^{-1}E_1^T$.
- $G = G_2 + E_2^T G_1(I - F_2G_1)^{-1}E_2$.
- $\omega = \omega_1\omega_2 \det(I - F_2G_1)^{-1}$.
- P is computed as the solution of a messy PDE or using "connected Feynman diagrams" (yet we're still in pure algebra!). Docility is preserved.



DoPeGDO Footnotes. Each variable has a "weight"$\in \{0, 1, 2\}$, and always $\mathrm{wt}\, z_i + \mathrm{wt}\, \zeta_i = 2$.

†1. Really, "weight-graded finite sets" $A = A_0 \sqcup A_1 \sqcup A_2$.

†2. Really, a power series in the weight-0 variables$^{\dagger 5}$.

†3. The weight of Q must be 2, so it decomposes as $Q = Q_{20} + Q_{11}$. The coefficients of Q_{20} are rational numbers while the coefficients of Q_{11} may be weight-0 power series$^{\dagger 5}$.

†4. Setting $\mathrm{wt}\, \epsilon = -2$, the weight of P is ≤ 2 (so the powers of the weight-0 variables are not constrained)$^{\dagger 5}$.

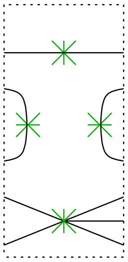
†5. In the knot-theoretic case, all weight-0 power series are rational functions of bounded degree in the exponentials of the weight-0 variables.

†6. There's also an obvious product

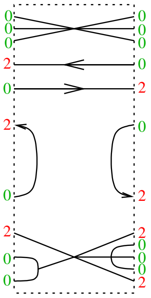
$$\mathrm{mor}(A_1 \to B_1) \times \mathrm{mor}(A_2 \to B_2) \to \mathrm{mor}(A_1 \sqcup A_2 \to B_1 \sqcup B_2).$$

Full DoPeGDO. Compute compositions in two phases:

- A 1-1 phase over the ring of power series in the weight-0 variables, in which the weight-2 variables are spectators.
- A (slightly modified) 2-0 phase over $\mathbb{Q}$, in which the weight-1 variables are spectators.



Analog. Solve $Ax = a,\ B(x)y = b$

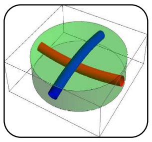


Questions. • Are there QFT precedents for "two-step Gaussian integration"?

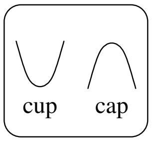
- In QFT, one saves even more by considering "one-particle-irreducible" diagrams and "effective actions". Does this mean anything here?
- Understanding $\mathrm{Hom}(\mathbb{Q}[z_A] \to \mathbb{Q}[z_B])$ seems like a good cause. Can you find other applications for the technology here?

$$\left(\begin{array}{l} QU = \mathcal{U}_\hbar(sl_{2+}^\epsilon) = A\langle y, b, a, x\rangle[\![\hbar]\!] \text{ with } [a, x] = x,\ [b, y] = -\epsilon y,\ [a, b] = 0, \\ {[a, y] = -y,\ [b, x] = \epsilon x, \text{ and } xy - qyx = (1 - AB)/\hbar, \text{ where } q = \mathbb{e}^{\hbar\epsilon}, A = \mathbb{e}^{-\hbar\epsilon a},} \\ \text{and } B = \mathbb{e}^{-\hbar b}. \text{ Also } \Delta(y, b, a, x) = (y_1 + B_1y_2, b_1 + b_2, a_1 + a_2, x_1 + A_1x_2), \\ S(y, b, a, x) = (-B^{-1}y, -b, -a, -A^{-1}x), \text{ and } R = \sum \hbar^{j+k} y^k b^j \otimes a^j x^k / j![k]_q!. \end{array} \right)$$

Theorem. Everything of value regrading $U = CU$ and/or its quantization $U = QU$ is **DoPeGDO**:



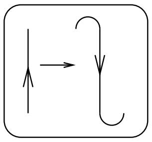
$R \in QU \otimes QU$



$C^{\pm 1} \in QU$

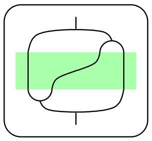
$m\colon U \otimes U \to U$

$\Delta\colon U \to U \otimes U$

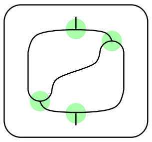


$S\colon U \to U$

$\mathrm{tr}\colon U \to U/wx{=}xw$



$\Phi \in CU^{\otimes 3}$

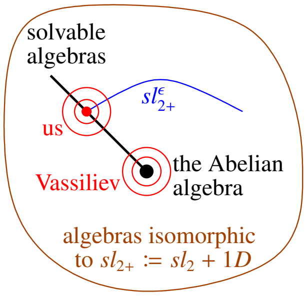


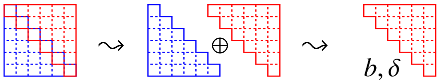
$J \in CU \otimes CU$

also Cartan's θ, the $\mathbb{D}$equantizator, and more, and all of their compositions.

Solvable Approximation. In sl_n, half is enough! Indeed $sl_n \oplus \mathfrak{a}_{n-1} = \mathcal{D}(◹, b, \delta)$. Now define $sl_{n+}^\epsilon := \mathcal{D}(◹, b, \epsilon\delta)$. Schematically, this is $[◹, ◹] = ◹$, $[◺, ◺] = \epsilon◺$, and $[◹, ◺] = ◺ + \epsilon◹$. The same process works for all semi-simple Lie algebras, and at $\epsilon^{k+1} = 0$ always yields a solvable Lie algebra.

4D Metrized Lie Algebras





$b(◹) = b\colon ◹ \otimes ◹ \to ◹$

$b(◺) \rightsquigarrow \delta\colon ◹ \to ◹ \otimes ◹$

Conclusion. There are lots of poly-time-computable well-behaved near-Alexander knot invariants: • They extend to tangles with appropriate multiplicative behaviour. • They have cabling and strand reversal formulas. ωεβ/akt

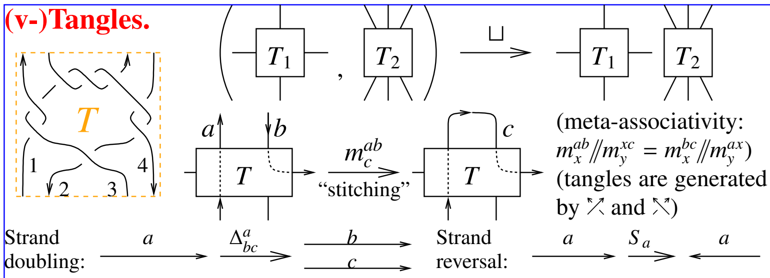
The invariant for $sl_{2+}^\epsilon/(\epsilon^2 = 0)$ (prior art: ωεβ/Ov) attains 2,883 distinct values on the 2,978 prime knots with $\leq$ 12 crossings. HOMFLY-PT and Khovanov homology together attain only 2,786 distinct values.

References.

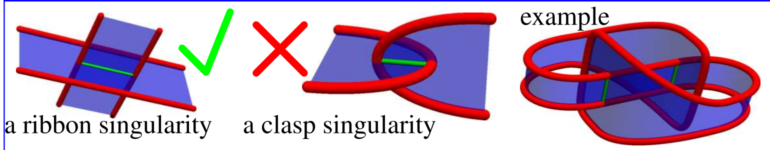
[GST] R. E. Gompf, M. Scharlemann, and A. Thompson, *Fibered Knots and Potential Counterexamples to the Property 2R and Slice-Ribbon Conjectures*, Geom. and Top. **14** (2010) 2305–2347, arXiv:1103.1601.

[Vo] H. Vo, *Alexander Invariants of Tangles via Expansions*, University of Toronto Ph.D. thesis, ωεβ/Vo.

(v-)Tangles.



(meta-associativity: $m^{ab}_x /\!\!/ m^{xc}_y = m^{bc}_x /\!\!/ m^{ax}_y$) (tangles are generated by ↗ and ↖)



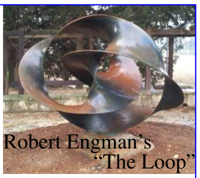
a ribbon singularity   a clasp singularity

A Bit About Ribbon Knots. A "ribbon knot" is a knot that can be presented as the boundary of a disk that has "ribbon singularities", but no "clasp singularities". A "slice knot" is a knot in $S^3 = \partial B^4$ which is the boundary of a non-singular disk in B^4. Every ribbon knots is clearly slice, yet,

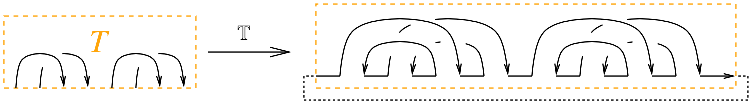
Conjecture. Some slice knots are not ribbon.

Fox-Milnor. The Alexander polynomial of a ribbon knot is always of the form $A(t) = f(t)f(1/t)$. (also for slice)

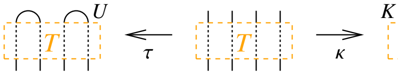
Genus. Every knot is the boundary of an orientable "Seifert Surface" (ωεβ/SS), and the least of their genera is the "genus" of the knot.


Robert Engman's "The Loop"

Claim. The knots of genus ≤ 2 are precisely the images of 4-component tangles via



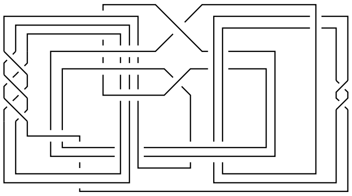
Theorem. K is ribbon iff it is κT for a tangle T for which τT is the untangle U.




Gompf, Scharlemann, Thompson [GST]

$$\begin{tikzcd} & U\in\mathcal{T}_n & & 1\in\mathcal{A}_n \\ \mathcal{T}_{2n} \arrow[ur, "\tau"] \arrow[dr, "\kappa"'] \arrow[rr, "z"] & & \mathcal{A}_{2n} \arrow[ur, "\tau"] \arrow[dr, "\kappa"'] & \\ & \text{ribbon } K\in\mathcal{T}_1 & & z(K)\in\mathcal{R}\subseteq\mathcal{A}_1 \end{tikzcd}$$

with $\mathcal{R} := \kappa(\tau^{-1}(1))$



Faster is better, leaner is meaner!

Vo's Thesis [Vo]. A proof of the Fox-Milnor theorem for ribbon knots using this technology (and more).

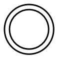
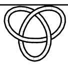
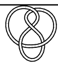
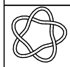
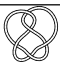
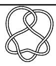
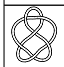
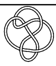
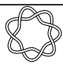
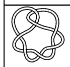
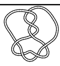
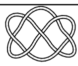
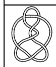
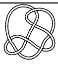
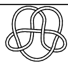
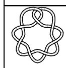
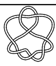
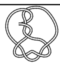
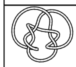
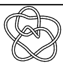
By a mixture of theory and experiment, for a knot K we get an invariant

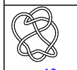
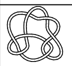
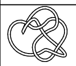
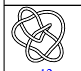
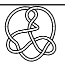
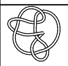
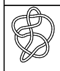
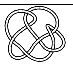
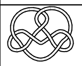
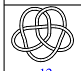
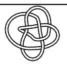
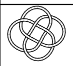
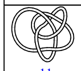
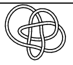
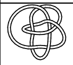
$$Z = \omega^{-1}\exp\left(Q + \frac{\epsilon}{\omega^2}P^{(1)} + \frac{\epsilon^2}{\omega^4}P^{(2)} + \dots\right)$$

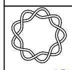
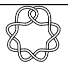
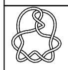
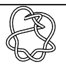
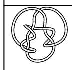
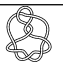
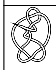
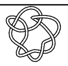
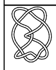
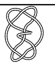
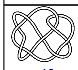
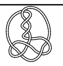
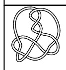
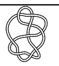
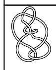
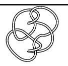
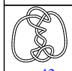
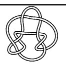
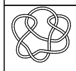
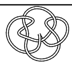
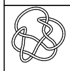
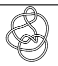
in which $Q = 0$ and ω is the Alexander polynomial. Below are tables of ω and of (p_1, p_2), the "essences" of the invariants $P^{(1)}$ and $P^{(2)}$ for the prime knots with up to 10 crossings (they are all palindromic Laurent polynomials in T, $p(T) = p(T^{-1})$, and so only their positive-powers parts (ω^+, p_1^+, p_2^+) are printed). $P^{(1)}$ and $P^{(2)}$ can be recovered from (ω, p_1, p_2) using the following ugly yet finite formulas (all brawn and no brains; over-dots are T-derivatives; ωεβ/ugly):

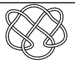
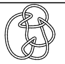
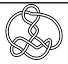
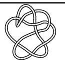
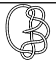
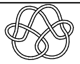
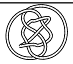
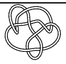
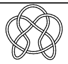
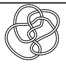
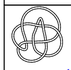
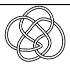
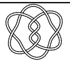
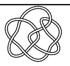
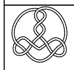
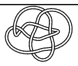
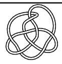
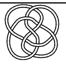
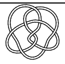
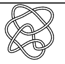
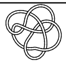
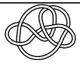
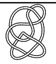
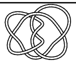
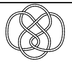
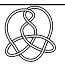
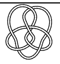
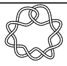
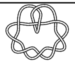
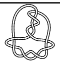
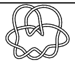
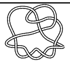
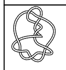
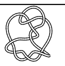
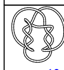
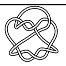
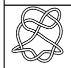
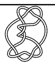
$$P^{(1)} = \left(T\omega\dot\omega - \frac{p_1(T-1)^2}{T}\right) + 2T\omega\dot\omega a + \frac{2T\omega\dot\omega}{1-T}xy,$$

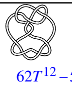
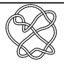
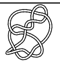
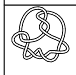
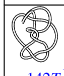
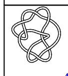
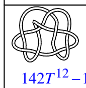
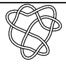
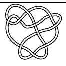
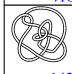
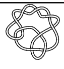
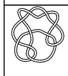
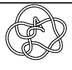
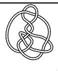
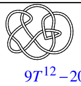
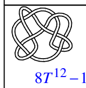
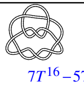
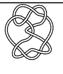
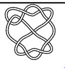
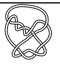
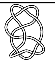
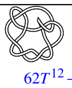
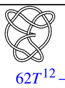
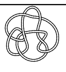
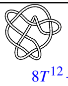
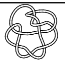
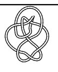
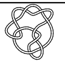
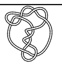
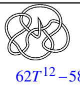
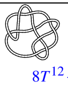
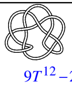
$$\begin{aligned} P^{(2)} = {} & \frac{T^2\left(\omega^2\left(2\dot p_1(T-1)^2+T\left(3\dot\omega^2T-2(\dot\omega+\ddot\omega T)\omega\right)\right)-p_2\right)-p_1^2(T-1)^4-2p_1(T-1)T\omega(2\dot\omega(T-1)T-(1+T)\omega)}{2T^2} \\ & +\frac{2\omega\left(p_1\left(T^2-1\right)\omega-2\dot\omega p_1(T-1)^2T+T\left(\dot p_1(T-1)^2+\dot\omega^2T^2\right)\omega-T^2(\dot\omega+\ddot\omega T)\omega^2\right)}{T}a \\ & +2T\omega^2(\dot\omega^2T-\dot\omega\omega-\ddot\omega T\omega)a^2+2\omega\left(2\dot\omega p_1(T-1)+\frac{\dot\omega^2T^2\omega}{T-1}-\frac{(\dot p_1(T-1)T+p_1(1+T))\omega}{T}\right)xy \\ & +\frac{4T\omega^2\left(\ddot\omega(T-1)T\omega-\dot\omega^2(T-1)T-\dot\omega\omega\right)}{(T-1)^2}axy+\frac{T\omega^2\left(2\dot\omega^2(T-1)T-\dot\omega(T-3)\omega-2\ddot\omega(T-1)T\omega\right)}{(T-1)^3}x^2y^2. \end{aligned}$$

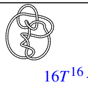
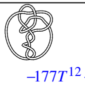
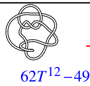
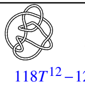
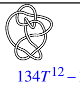
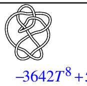
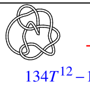
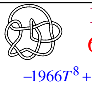
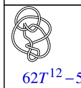
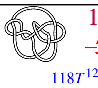
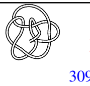
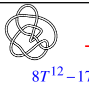
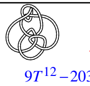
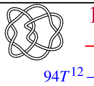
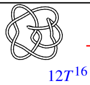
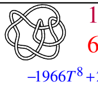
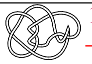
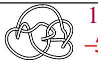
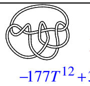
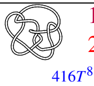
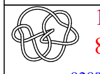
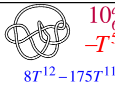
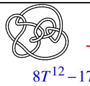
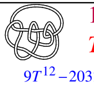
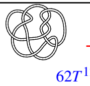
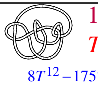
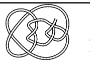
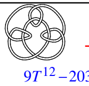
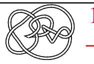
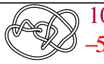
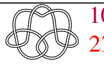
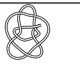
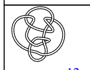
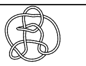
knot diag	n^t_k p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+	knot diag	n^t_k p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+	knot diag	n^t_k p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+
	0^a_1 0	1	0 / ✔ 0 / ✔	0		3^a_1 T	$T-1$	1 / ✘ 1 / ✘	$3T^3-12T^2+26T-38$		4^a_1 0	$3-T$	1 / ✘ 1 / ✔	$T^4-3T^3-15T^2+74T-110$
	5^a_1 $2T^3+3T$	T^2-T+1	2 / ✘ 2 / ✘	$5T^7-20T^6+55T^5-120T^4+217T^3-338T^2+450T-510$		5^a_2 $5T-4$	$2T-3$	1 / ✘ 1 / ✘	$-10T^4+120T^3-487T^2+1054T-1362$		6^a_1 $T-4$	$5-2T$	1 / ✔ 1 / ✘	$14T^4-16T^3-293T^2+1098T-1598$
	6^a_2 T^3-4T^2+4T-4	$-T^2+3T-3$	2 / ✘ 1 / ✘	$3T^8-21T^7+49T^6+15T^5-433T^4+1543T^3-3431T^2+5482T-6410$		6^a_3 0	T^2-3T+5	2 / ✘ 1 / ✔	$4T^8-33T^7+121T^6-203T^5-111T^4+1499T^3-4210T^2+7186T-8510$		7^a_1 $3T^5+5T^3+6T$	T^3-T^2+T-1	3 / ✘ 3 / ✘	$7T^{11}-28T^{10}+77T^9-168T^8+322T^7-560T^6+891T^5-1310T^4+1777T^3-2238T^2+2604T-2772$
	7^a_2 $14T-16$	$3T-5$	1 / ✘ 1 / ✘	$-129T^4+1177T^3-4421T^2+9226T-11718$		7^a_3 $-9T^3+8T^2-16T+12$	$2T^2-3T+3$	2 / ✘ 2 / ✘	$-18T^8+208T^7-917T^6+2666T^5-6049T^4+11283T^3-17671T^2+23356T-25736$		7^a_4 $32-24T$	$4T-7$	1 / ✘ 2 / ✘	$-352T^4+3616T^3-14378T^2+30700T-39188$
	7^a_5 $9T^3-16T^2+29T-28$	$2T^2-4T+5$	2 / ✘ 2 / ✘	$-18T^8+264T^7-1548T^6+5680T^5-15107T^4+31152T^3-51476T^2+69252T-76414$		7^a_6 $T^3-8T^2+19T-20$	$-T^2+5T-7$	2 / ✘ 1 / ✘	$3T^8-35T^7+128T^6+105T^5-2610T^4+11225T^3-28031T^2+47186T-55946$		7^a_7 $8-3T$	T^2-5T+9	2 / ✘ 1 / ✘	$4T^8-55T^7+310T^6-805T^5+86T^4+6349T^3-22686T^2+43610T-53622$
	8^a_1 $5T-16$	$7-3T$	1 / ✘ 1 / ✘	$42T^4+215T^3-2542T^2+7562T-10542$		8^a_2 $2T^5-8T^4+10T^3-12T^2+13T-12$	$-T^3+3T^2-3T+3$	3 / ✘ 2 / ✘	$5T^{12}-39T^{11}+119T^{10}-139T^9-249T^8+1660T^7-4959T^6+11131T^5-20813T^4+33595T^3-47521T^2+58988T-63556$		8^a_3 0	$9-4T$	1 / ✘ 2 / ✔	$224T^4-224T^3-3910T^2+14100T-20364$
	8^a_4 $3T^3-8T^2+6T-4$	$-2T^2+5T-5$	2 / ✘ 2 / ✘	$54T^8-344T^7+865T^6-650T^5-2723T^4+12243T^3-28461T^2+45792T-53540$		8^a_5 $-2T^5+8T^4-13T^3+20T^2-22T+24$	$-T^3+3T^2-4T+5$	3 / ✘ 2 / ✘	$5T^{12}-39T^{11}+128T^{10}-182T^9-274T^8+2476T^7-8642T^6+21517T^5-42924T^4+71719T^3-102448T^2+126480T-135628$		8^a_6 $5T^3-20T^2+28T-32$	$-2T^2+6T-7$	2 / ✘ 2 / ✘	$38T^8-216T^7+112T^6+2880T^5-14787T^4+42444T^3-85415T^2+128406T-146916$

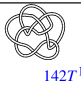
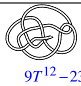
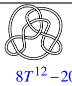
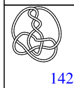
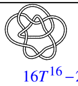
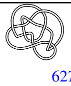
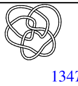
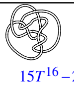
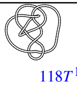
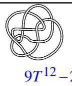
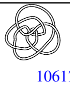
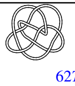
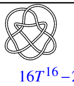
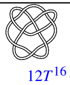
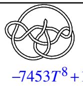
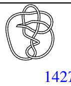
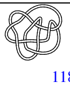
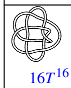
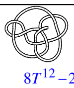
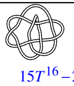
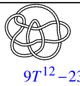
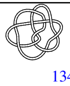
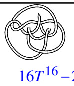
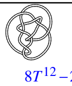
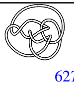
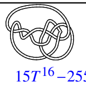
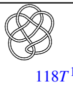
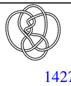
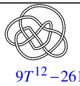
knot diag	n^t_k	Alexander's ω^+	genus / ribbon	p^+_1	unknotting # / amphi?	p^+_2
	8^a_7	T^3-3T^2+5T-5	3 / ✗	$-T^5+4T^4-10T^3+12T^2-13T+12$	1 / ✗	$8T^{12}-75T^{11}+343T^{10}-979T^9+1821T^8-1782T^7-1623T^6+12083T^5-33001T^4+64599T^3-101194T^2+131404T-143216$
	8^a_8	$2T^2-6T+9$	2 / ✓	$-T^3+4T^2-12T+16$	2 / ✗	$62T^8-504T^7+1736T^6-2408T^5-3717T^4+26492T^3-68493T^2+113418T-133180$
	8^a_9	$-T^3+3T^2-5T+7$	3 / ✓	0	1 / ✓	$9T^{12}-87T^{11}+417T^{10}-1305T^9+2858T^8-4134T^7+2114T^6+8285T^5-31925T^4+69235T^3-112773T^2+148508T-162396$
	8^a_{10}	T^3-3T^2+6T-7	3 / ✗	$-T^5+4T^4-11T^3+16T^2-21T+20$	2 / ✗	$8T^{12}-75T^{11}+362T^{10}-1122T^9+2306T^8-2540T^7-2198T^6+18817T^5-54380T^4+110103T^3-175694T^2+230080T-251346$
	8^a_{11}	$-2T^2+7T-9$	2 / ✗	$5T^3-24T^2+39T-44$	1 / ✗	$38T^8-264T^7+301T^6+3514T^5-21716T^4+68785T^3-146898T^2+227828T-263172$
	8^a_{12}	$T^2-7T+13$	2 / ✗	0	2 / ✓	$4T^8-77T^7+583T^6-1991T^5+987T^4+17311T^3-71802T^2+147914T-185846$
	8^a_{13}	$2T^2-7T+11$	2 / ✗	$-T^3+4T^2-14T+20$	1 / ✗	$62T^8-592T^7+2351T^6-3918T^5-4235T^4+40079T^3-111533T^2+191500T-227432$
	8^a_{14}	$-2T^2+8T-11$	2 / ✗	$5T^3-28T^2+57T-68$	1 / ✗	$38T^8-312T^7+444T^6+5096T^5-34777T^4+116368T^3-255750T^2+401632T-465478$
	8^a_{15}	$3T^2-8T+11$	2 / ✗	$21T^3-64T^2+120T-140$	2 / ✗	$-123T^8+2128T^7-15241T^6+66120T^5-199999T^4+451912T^3-792414T^2+1101720T-1228222$
	8^a_{16}	T^3-4T^2+8T-9	3 / ✗	$T^5-6T^4+17T^3-28T^2+35T-36$	2 / ✗	$8T^{12}-100T^{11}+598T^{10}-2205T^9+5292T^8-7164T^7-2380T^6+43100T^5-137314T^4+291750T^3-478742T^2+636488T-698666$
	8^a_{17}	$-T^3+4T^2-8T+11$	3 / ✗	0	1 / ✓	$9T^{12}-116T^{11}+722T^{10}-2843T^9+7656T^8-13668T^7+11117T^6+21968T^5-113086T^4+273778T^3-475622T^2+649064T-717954$
	8^a_{18}	$-T^3+5T^2-10T+13$	3 / ✗	0	2 / ✓	$9T^{12}-145T^{11}+1075T^{10}-4842T^9+14504T^8-28560T^7+27957T^6+35195T^5-225204T^4+573797T^3-1021641T^2+1411484T-1567262$
	8^n_{19}	T^3-T^2+1	3 / ✗	$-3T^5-4T^2-3T$	3 / ✗	$7T^{11}-19T^{10}+6T^9+48T^8-52T^7-91T^6+211T^5+16T^4-431T^3+289T^2+536T-1060$
	8^n_{20}	T^2-2T+3	2 / ✓	$4T-4$	1 / ✗	$4T^8-22T^7+66T^6-124T^5+52T^4+478T^3-1652T^2+3014T-3640$
	8^n_{21}	$-T^2+4T-5$	2 / ✗	$T^3-8T^2+16T-20$	1 / ✗	$3T^8-28T^7+49T^6+352T^5-2489T^4+8164T^3-17530T^2+27092T-31226$

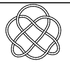
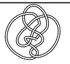
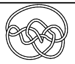
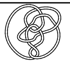
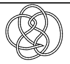
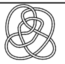
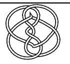
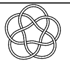
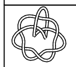
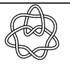
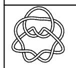
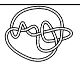
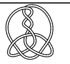
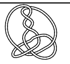
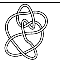
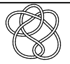
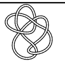
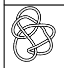
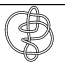
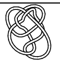
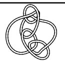
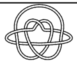
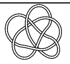
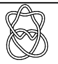
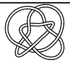
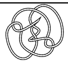
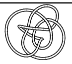
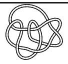
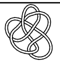
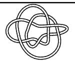
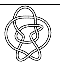
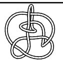
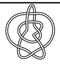
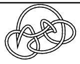
knot diag	n^t_k	Alexander's ω^+	genus / ribbon	p^+_1	unknotting # / amphi?	p^+_2
	9^a_1	$T^4-T^3+T^2-T+1$	4 / ✗	$4T^7+7T^5+9T^3+10T$	4 / ✗	$9T^{15}-36T^{14}+99T^{13}-216T^{12}+414T^{11}-720T^{10}+1170T^9-1800T^8+2630T^7-3662T^6+4853T^5-6142T^4+7423T^3-8572T^2+9420T-9780$
	9^a_2	$4T-7$	1 / ✗	$30T-40$	1 / ✗	$-728T^4+6088T^3-21946T^2+44788T-56420$
	9^a_3	$2T^3-3T^2+3T-3$	3 / ✗	$-13T^5+12T^4-25T^3+20T^2-32T+24$	3 / ✗	$-26T^{12}+296T^{11}-1311T^{10}+3838T^9-8867T^8+17613T^7-31407T^6+51061T^5-76085T^4+104297T^3-131779T^2+152840T-160976$
	9^a_4	$3T^2-5T+5$	2 / ✗	$23T^3-28T^2+46T-44$	2 / ✗	$-219T^8+1999T^7-8389T^6+23799T^5-52835T^4+96723T^3-149121T^2+194698T-213338$
	9^a_5	$6T-11$	1 / ✗	$100-65T$	2 / ✗	$-3234T^4+29792T^3-113241T^2+236818T-300294$
	9^a_6	$2T^3-4T^2+5T-5$	3 / ✗	$13T^5-24T^4+45T^3-52T^2+68T-64$	3 / ✗	$-26T^{12}+376T^{11}-2212T^{10}+8280T^9-23249T^8+53488T^7-106013T^6+185990T^5-292853T^4+416673T^3-537062T^2+626488T-659788$
	9^a_7	$3T^2-7T+9$	2 / ✗	$23T^3-56T^2+99T-108$	2 / ✗	$-219T^8+2717T^7-15720T^6+58389T^5-157698T^4+329265T^3-548657T^2+741610T-819394$
	9^a_8	$-2T^2+8T-11$	2 / ✗	$3T^3-16T^2+29T-28$	2 / ✗	$54T^8-552T^7+2124T^6-2216T^5-12641T^4+67112T^3-172118T^2+289304T-342134$
	9^a_9	$2T^3-4T^2+6T-7$	3 / ✗	$13T^5-24T^4+55T^3-72T^2+98T-96$	3 / ✗	$-26T^{12}+376T^{11}-2296T^{10}+9328T^9-28988T^8+73584T^7-158399T^6+295928T^5-486916T^4+712094T^3-930993T^2+1092074T-1151564$
	9^a_{10}	$4T^2-8T+9$	2 / ✗	$-40T^3+72T^2-114T+120$	2, 3 / ✗	$-608T^8+6720T^7-33776T^6+110928T^5-273462T^4+537040T^3-862768T^2+1145784T-1259748$
	9^a_{11}	$-T^3+5T^2-7T+7$	3 / ✗	$-2T^5+16T^4-41T^3+52T^2-66T+64$	2 / ✗	$5T^{12}-65T^{11}+312T^{10}-463T^9-2042T^8+14588T^7-50444T^6+126967T^5-258750T^4+444545T^3-654213T^2+827220T-895336$
	9^a_{12}	$-2T^2+9T-13$	2 / ✗	$5T^3-36T^2+84T-100$	1 / ✗	$38T^8-312T^7+45T^6+9790T^5-60473T^4+202775T^3-453255T^2+722176T-841572$
	9^a_{13}	$4T^2-9T+11$	2 / ✗	$-40T^3+92T^2-154T+168$	2, 3 / ✗	$-608T^8+7680T^7-43650T^6+158004T^5-417129T^4+856533T^3-1412461T^2+1899222T-2095210$
	9^a_{14}	$2T^2-9T+15$	2 / ✗	$-T^3+8T^2-35T+60$	1 / ✗	$62T^8-752T^7+3655T^6-7178T^5-9502T^4+97737T^3-294656T^2+531720T-642168$
	9^a_{15}	$-2T^2+10T-15$	2 / ✗	$-5T^3+40T^2-108T+136$	2 / ✗	$38T^8-360T^7+208T^6+12328T^5-84103T^4+298764T^3-691161T^2+1121034T-1313504$
	9^a_{16}	$2T^3-5T^2+8T-9$	3 / ✗	$-13T^5+36T^4-80T^3+120T^2-161T+168$	3 / ✗	$-26T^{12}+456T^{11}-3331T^{10}+15554T^9-53941T^8+149494T^7-345106T^6+680900T^5-1167591T^4+1759576T^3-2347749T^2+2786466T-2949428$
	9^a_{17}	T^3-5T^2+9T-9	3 / ✗	$T^5-8T^4+23T^3-32T^2+28T-24$	2 / ✗	$8T^{12}-125T^{11}+874T^{10}-3595T^9+9462T^8-15166T^7+6162T^6+47027T^5-181220T^4+415509T^3-716070T^2+982036T-1089796$
	9^a_{18}	$4T^2-10T+13$	2 / ✗	$40T^3-108T^2+193T-220$	2 / ✗	$-608T^8+8224T^7-51208T^6+201904T^5-570516T^4+1228920T^3-2087725T^2+2850858T-3159722$
	9^a_{19}	$2T^2-10T+17$	2 / ✗	$T^3-8T^2+20T-24$	1 / ✗	$62T^8-840T^7+4536T^6-10352T^5-7041T^4+116428T^3-372683T^2+688198T-836608$
	9^a_{20}	$-T^3+5T^2-9T+11$	3 / ✗	$2T^5-16T^4+47T^3-84T^2+117T-124$	2 / ✗	$5T^{12}-65T^{11}+330T^{10}-577T^9-2439T^8+21482T^7-86959T^6+247237T^5-548658T^4+993841T^3-1502637T^2+1918532T-2080192$
	9^a_{21}	$-2T^2+11T-17$	2 / ✗	$-5T^3+44T^2-127T+164$	1 / ✗	$38T^8-408T^7+493T^6+13802T^5-105014T^4+396685T^3-954552T^2+1583140T-1868380$
	9^a_{22}	$T^3-5T^2+10T-11$	3 / ✗	$-T^5+8T^4-24T^3+38T^2-40T+36$	1 / ✗	$8T^{12}-125T^{11}+893T^{10}-3824T^9+10605T^8-17902T^7+6990T^6+64299T^5-251573T^4+584313T^3-1012133T^2+1388650T-1540398$

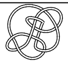
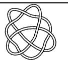
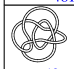
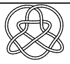
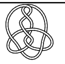
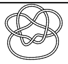
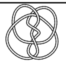
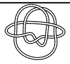
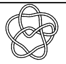
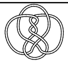
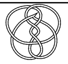
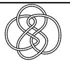
knot diag	n_k^t p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+	knot diag	n_k^t p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+
	9^a_{23} $40T^3-128T^2+243T-288$	$4T^2-11T+15$	2 / ✘ 2 / ✘	$-608T^8+9184T^7-62698T^6+265980T^5-794496T^4+1781111T^3-3107204T^2+4307350T-4797258$		9^a_{24} $-4T^2+16T-20$	$-T^3+5T^2-10T+13$	3 / ✘ 1 / ✘	$9T^{12}-145T^{11}+1075T^{10}-4850T^9+14600T^8-29112T^7+29921T^6+30667T^5-218916T^4+570933T^3-1029833T^2+1433476T-1595654$
	9^a_{25} $12T^3-70T^2+153T-188$	$-3T^2+12T-17$	2 / ✘ 2 / ✘	$174T^8-1200T^7-1027T^6+42696T^5-235512T^4+740956T^3-1585864T^2+2460360T-2841166$		9^a_{26} $-T^5+8T^4-31T^3+64T^2-85T+92$	$T^3-5T^2+11T-13$	3 / ✘ 1 / ✘	$8T^{12}-125T^{11}+900T^{10}-3861T^9+10351T^8-14356T^7-12391T^6+132473T^5-427732T^4+939309T^3-1588046T^2+2154028T-2381116$
	9^a_{27} $T^3-8T^2+24T-32$	$-T^3+5T^2-11T+15$	3 / ✔ 1 / ✘	$9T^{12}-145T^{11}+1096T^{10}-5115T^9+16088T^8-33784T^7+37362T^6+34075T^5-273854T^4+743153T^3-1374545T^2+1941332T-2171344$		9^a_{28} $T^5-8T^4+30T^3-68T^2+105T-120$	$T^3-5T^2+12T-15$	3 / ✘ 1 / ✘	$8T^{12}-125T^{11}+923T^{10}-4138T^9+11800T^8-18092T^7-11101T^6+159415T^5-543916T^4+1228781T^3-2107809T^2+2877256T-3186008$
	9^a_{29} $T^5-8T^4+26T^3-48T^2+59T-56$	$T^3-5T^2+12T-15$	3 / ✘ 2 / ✘	$8T^{12}-125T^{11}+931T^{10}-4290T^9+13096T^8-24848T^7+13335T^6+94047T^5-409576T^4+1010237T^3-1816557T^2+2543836T-2840192$		9^a_{30} $2T^3-10T^2+25T-32$	$-T^3+5T^2-12T+17$	3 / ✘ 1 / ✘	$9T^{12}-145T^{11}+1117T^{10}-5376T^9+17533T^8-38170T^7+43292T^6+43619T^5-347397T^4+957881T^3-1794189T^2+2553442T-2863228$
	9^a_{31} $T^5-8T^4+33T^3-80T^2+132T-152$	$T^3-5T^2+13T-17$	3 / ✘ 2 / ✘	$8T^{12}-125T^{11}+938T^{10}-4303T^9+12544T^8-19138T^7-17200T^6+204143T^5-703180T^4+1617365T^3-2818190T^2+3886636T-4319004$		9^a_{32} $-T^5+10T^4-42T^3+94T^2-133T+148$	$T^3-6T^2+14T-17$	3 / ✘ 2 / ✘	$8T^{12}-150T^{11}+1269T^{10}-6297T^9+19455T^8-32720T^7-11156T^6+260282T^5-930836T^4+2153618T^3-3750358T^2+5165114T-5736454$
	9^a_{33} $T^3-10T^2+30T-40$	$-T^3+6T^2-14T+19$	3 / ✘ 1 / ✘	$9T^{12}-174T^{11}+1539T^{10}-8207T^9+28913T^8-67184T^7+84077T^6+55866T^5-581640T^4+1664798T^3-3166838T^2+4539202T-5100726$		9^a_{34} $3T^3-18T^2+43T-56$	$-T^3+6T^2-16T+23$	3 / ✘ 1 / ✘	$9T^{12}-174T^{11}+1581T^{10}-8831T^9+32988T^8-81774T^7+109631T^6+73248T^5-829341T^4+2480938T^3-4869197T^2+7112552T-8043256$
	9^a_{35} $90T-144$	$7T-13$	1 / ✘ 2, 3 / ✘	$-6355T^4+58861T^3-224539T^2+470386T-596734$		9^a_{36} $-2T^5+16T^4-44T^3+66T^2-87T+88$	$-T^3+5T^2-8T+9$	3 / ✘ 2 / ✘	$5T^{12}-65T^{11}+321T^{10}-532T^9-2081T^8+17066T^7-64846T^6+175611T^5-376739T^4+668001T^3-998037T^2+1267342T-1372104$
	9^a_{37} $T^3-8T^2+22T-28$	$2T^2-11T+19$	2 / ✘ 2 / ✘	$62T^8-928T^7+5487T^6-13814T^5-6681T^4+154867T^3-520239T^2+983348T-1204192$		9^a_{38} $62T^3-204T^2+382T-452$	$5T^2-14T+19$	2 / ✘ 2, 3 / ✘	$-1414T^8+22122T^7-153560T^6+657340T^5-1976110T^4+4454362T^3-7806448T^2+10855582T-12103772$
	9^a_{39} $-12T^3+84T^2-210T+268$	$-3T^2+14T-21$	2 / ✘ 1 / ✘	$174T^8-1442T^7-690T^6+59068T^5-366222T^4+1247214T^3-2815796T^2+4505578T-5255776$		9^a_{40} $T^5-12T^4+57T^3-144T^2+229T-264$	$T^3-7T^2+18T-23$	3 / ✘ 2 / ✘	$8T^{12}-175T^{11}+1712T^{10}-9738T^9+34250T^8-66108T^7-11148T^6+553509T^5-2149560T^4+5230963T^3-9406248T^2+13187800T-14730526$
	9^a_{41} $3T^3-20T^2+70T-108$	$3T^2-12T+19$	2 / ✔ 2 / ✘	$309T^8-3288T^7+13885T^6-20928T^5-55179T^4+378100T^3-1035810T^2+1787808T-2129794$		9^n_{42} $-T^3+2T^2+T-4$	$-T^2+2T-1$	2 / ✘ 1 / ✘	$3T^8-14T^7+32T^6-96T^5+265T^4-294T^3-498T^2+2170T-3128$
	9^n_{43} $-2T^5+8T^4-7T^3+2T^2-5T+4$	$-T^3+3T^2-2T+1$	3 / ✘ 2 / ✘	$5T^{12}-39T^{11}+110T^{10}-108T^9-115T^8+570T^7-1477T^6+3453T^5-6651T^4+10951T^3-17188T^2+24718T-28462$		9^n_{44} $-2T^2+9T-12$	T^2-4T+7	2 / ✘ 1 / ✘	$4T^8-48T^7+237T^6-496T^5-346T^4+4988T^3-15044T^2+26768T-32126$
	9^n_{45} $T^3-14T^2+47T-60$	$-T^2+6T-9$	2 / ✘ 1 / ✘	$3T^8-42T^7+78T^6+1376T^5-11135T^4+42574T^3-102522T^2+169806T-200284$		9^n_{46} $3T-12$	$5-2T$	1 / ✔ 2 / ✘	$-2T^4+160T^3-1125T^2+3082T-4222$
	9^n_{47} $-T^5+6T^4-15T^3+16T^2-10T+12$	T^3-4T^2+6T-5	3 / ✘ 2 / ✘	$8T^{12}-100T^{11}+560T^{10}-1841T^9+3847T^8-4710T^7-42T^6+17494T^5-55447T^4+117058T^3-193749T^2+261386T-288924$		9^n_{48} $-T^3+12T^2-42T+52$	$-T^2+7T-11$	2 / ✘ 2 / ✘	$3T^8-49T^7+243T^6+267T^5-8051T^4+40499T^3-112167T^2+199850T-241202$
	9^n_{49} $-21T^3+38T^2-61T+60$	$3T^2-6T+7$	2 / ✘ 3 / ✘	$-123T^8+1614T^7-8744T^6+29928T^5-75873T^4+152714T^3-250794T^2+338238T-373944$		10^a_1 $14T-40$	$9-4T$	1 / ✘ 1 / ✘	$-24T^4+2136T^3-13430T^2+34860T-47068$
	10^a_2 $3T^7-12T^6+16T^5-20T^4+24T^3-24T^2+27T-24$	$-T^4+3T^3-3T^2+3T-3$	4 / ✘ 3 / ✘	$7T^{16}-57T^{15}+189T^{14}-293T^{13}-55T^{12}+1628T^{11}-5543T^{10}+13266T^9-26589T^8+47468T^7-77415T^6+116549T^5-162911T^4+212325T^3-258413T^2+292580T-305480$		10^a_3 $11T-28$	$13-6T$	1 / ✔ 2 / ✘	$870T^4+1288T^3-27795T^2+85718T-120138$
	10^a_4 $4T^3-8T^2+T+8$	$-3T^2+7T-7$	2 / ✘ 2 / ✘	$294T^8-1807T^7+4570T^6-4305T^5-9550T^4+49581T^3-117456T^2+189330T-221294$		10^a_5 $-2T^7+8T^6-20T^5+28T^4-36T^3+36T^2-39T+36$	$T^4-3T^3+5T^2-5T+5$	4 / ✘ 2 / ✘	$12T^{16}-117T^{15}+565T^{14}-1757T^{13}+3847T^{12}-5960T^{11}+5381T^{10}+2968T^9-26625T^8+75008T^7-157415T^6+279173T^5-436999T^4+615297T^3-785328T^2+909916T-955948$
	10^a_6 $9T^5-36T^4+56T^3-72T^2+81T-84$	$-2T^3+6T^2-7T+7$	3 / ✘ 3 / ✘	$62T^{12}-408T^{11}+712T^{10}+2280T^9-17493T^8+60652T^7-153492T^6+319048T^5-569584T^4+890397T^3-1228657T^2+1496150T-1599330$		10^a_7 $14T^3-72T^2+135T-160$	$-3T^2+11T-15$	2 / ✘ 1 / ✘	$114T^8-275T^7-5840T^6+51739T^5-222492T^4+626425T^3-1267348T^2+1914410T-2193462$
	10^a_8 $7T^5-20T^4+23T^3-28T^2+26T-24$	$-2T^3+5T^2-5T+5$	3 / ✘ 2 / ✘	$94T^{12}-672T^{11}+2115T^{10}-3678T^9+2535T^8+6453T^7-30645T^6+78385T^5-154895T^4+256601T^3-367525T^2+458500T-494524$		10^a_9 $-T^7+4T^6-10T^5+20T^4-25T^3+28T^2-28T+28$	$-T^4+3T^3-5T^2+7T-7$	4 / ✘ 1 / ✘	$15T^{16}-153T^{15}+787T^{14}-2727T^{13}+7084T^{12}-14404T^{11}+22886T^{10}-26134T^9+11540T^8+39332T^7-146866T^6+325115T^5-571077T^4+856941T^3-1131013T^2+1330668T-1403980$
	10^a_{10} $-5T^3+24T^2-71T+100$	$3T^2-11T+17$	2 / ✘ 1 / ✘	$285T^8-2735T^7+10078T^6-9479T^5-64000T^4+327253T^3-827377T^2+1378130T-1624314$		10^a_{11} $16T^3-52T^2+68T-72$	$-4T^2+11T-13$	2 / ✘ 2, 3 / ✘	$736T^8-4672T^7+9634T^6+11132T^5-125367T^4+413121T^3-873095T^2+1336974T-1536906$

knot diag	n^t_k	Alexander's ω^+	genus / ribbon	p^+_1	unknotting # / amphi?	p^+_2
	10^a_{12}	$2T^3-6T^2+10T-11$	3 / ✘	$-5T^5+20T^4-50T^3+72T^2-89T+92$	2 / ✘	$118T^{12}-1080T^{11}+4748T^{10}-12624T^9+19414T^8-2072T^7-88507T^6+320836T^5-750453T^4+1366922T^3-2053481T^2+2604638T-2816934$
	10^a_{14}	$-2T^3+8T^2-12T+13$	3 / ✘	$9T^5-52T^4+119T^3-180T^2+225T-236$	2 / ✘	$62T^{12}-584T^{11}+1720T^{10}+2816T^9-42848T^8+195040T^7-594177T^6+1407688T^5-2753604T^4+4575154T^3-6545078T^2+8106820T-8706026$
	10^a_{16}	$-4T^2+12T-15$	2 / ✘	$-16T^3+56T^2-76T+80$	2 / ✘	$736T^8-5248T^7+12944T^6+6528T^5-144162T^4+522200T^3-1155370T^2+1809228T-2093696$
	10^a_{18}	$-4T^2+14T-19$	2 / ✘	$16T^3-68T^2+121T-140$	1 / ✘	$736T^8-6240T^7+17736T^6+11088T^5-245648T^4+930168T^3-2109201T^2+3338706T-3874682$
	10^a_{20}	$-3T^2+9T-11$	2 / ✘	$14T^3-56T^2+88T-104$	2 / ✘	$114T^8-153T^7-4783T^6+34425T^5-128711T^4+327435T^3-618704T^2+899066T-1017366$
	10^a_{22}	$-2T^3+6T^2-10T+13$	3 / ✔	$-T^5+4T^4-10T^3+24T^2-37T+44$	2 / ✘	$142T^{12}-1368T^{11}+6524T^{10}-20120T^9+42790T^8-57928T^7+16919T^6+158700T^5-540707T^4+1130294T^3-1809643T^2+2363114T-2577418$
	10^a_{24}	$-4T^2+14T-19$	2 / ✘	$24T^3-116T^2+221T-268$	2 / ✘	$416T^8-1568T^7-13224T^6+136928T^5-604124T^4+1701008T^3-3414673T^2+5118714T-5846946$
	10^a_{26}	$-2T^3+7T^2-13T+17$	3 / ✘	$-T^5+4T^4-10T^3+28T^2-49T+60$	1 / ✘	$142T^{12}-1600T^{11}+8823T^{10}-31058T^9+74964T^8-117897T^7+67064T^6+255997T^5-1047600T^4+2360395T^3-3947888T^2+5281288T-5805248$
	10^a_{28}	$4T^2-13T+19$	2 / ✘	$-8T^3+36T^2-100T+136$	2 / ✘	$928T^8-7872T^7+26174T^6-22588T^5-142295T^4+689113T^3-1676391T^2+2728998T-3192146$
	10^a_{30}	$-4T^2+17T-25$	2 / ✘	$24T^3-148T^2+345T-440$	1 / ✘	$416T^8-2048T^7-17490T^6+219996T^5-1101894T^4+3396907T^3-7245510T^2+11243734T-12988226$
	10^a_{32}	$-2T^3+8T^2-15T+19$	3 / ✘	$T^5-4T^4+13T^3-40T^2+78T-96$	1 / ✘	$142T^{12}-1832T^{11}+11204T^{10}-42688T^9+109909T^8-184384T^7+124831T^6+360782T^5-1615391T^4+3759585T^3-6404890T^2+8655360T-9545252$
	10^a_{34}	$3T^2-9T+13$	2 / ✘	$-5T^3+20T^2-52T+68$	2 / ✘	$285T^8-2205T^7+6601T^6-3429T^5-43369T^4+185703T^3-431857T^2+687874T-799218$
	10^a_{36}	$-3T^2+13T-19$	2 / ✘	$14T^3-88T^2+208T-264$	2 / ✘	$114T^8-397T^7-7597T^6+81141T^5-393441T^4+1198967T^3-2544952T^2+3941362T-4550398$
	10^a_{38}	$-4T^2+15T-21$	2 / ✘	$24T^3-128T^2+270T-336$	2 / ✘	$416T^8-1632T^7-16122T^6+172460T^5-788845T^4+2280037T^3-4653713T^2+7038342T-8061882$
	10^a_{40}	$2T^3-8T^2+17T-21$	3 / ✘	$-5T^5+28T^4-89T^3+176T^2-258T+288$	2 / ✘	$118T^{12}-1464T^{11}+8692T^{10}-31256T^9+67987T^8-49624T^7-257955T^6+1301482T^5-3582545T^4+7240253T^3-11620382T^2+15292356T-16735336$
	10^a_{42}	$-T^3+7T^2-19T+27$	3 / ✔	$2T^3-8T^2+11T-12$	1 / ✘	$9T^{12}-203T^{11}+2093T^{10}-12971T^9+52885T^8-142268T^7+214987T^6+60931T^5-1368859T^4+4365895T^3-8815357T^2+13058404T-14831092$
	10^a_{44}	$T^3-7T^2+19T-25$	3 / ✘	$T^5-12T^4+56T^3-140T^2+220T-248$	1 / ✘	$8T^{12}-175T^{11}+1735T^{10}-10157T^9+37586T^8-81160T^7+29232T^6+500937T^5-2197451T^4+5635115T^3-10448058T^2+14900236T-16735696$
	10^a_{46}	$-T^4+3T^3-4T^2+5T-5$	4 / ✘	$-3T^7+12T^6-21T^5+34T^4-43T^3+52T^2-55T+56$	3 / ✘	$7T^{16}-57T^{15}+204T^{14}-382T^{13}+69T^{12}+2247T^{11}-9674T^{10}+27287T^9-61957T^8+121378T^7-211961T^6+335438T^5-485235T^4+644818T^3-789365T^2+891215T-928064$
	10^a_{13}	$2T^2-13T+23$	2 / ✘	$T^3-12T^2+51T-84$	2 / ✘	$62T^8-1088T^7+7367T^6-20586T^5-13356T^4+286509T^3-1005098T^2+1954280T-2416160$
	10^a_{15}	$2T^3-6T^2+9T-9$	3 / ✘	$-3T^5+12T^4-24T^3+24T^2-17T+12$	2 / ✘	$134T^{12}-1272T^{11}+5792T^{10}-16520T^9+31765T^8-37636T^7+2396T^6+120176T^5-371368T^4+752873T^3-1195043T^2+1560190T-1702986$
	10^a_{17}	$T^4-3T^3+5T^2-7T+9$	4 / ✘	0	1 / ✔	$16T^{16}-165T^{15}+861T^{14}-3043T^{13}+8173T^{12}-17514T^{11}+30162T^{10}-39958T^9+32666T^8+13998T^7-125081T^6+317743T^5-588481T^4+904569T^3-1207020T^2+1426556T-1506972$
	10^a_{19}	$2T^3-7T^2+11T-11$	3 / ✘	$3T^5-16T^4+35T^3-40T^2+30T-24$	2 / ✘	$134T^{12}-1480T^{11}+7641T^{10}-24194T^9+50855T^8-66007T^7+12323T^6+201357T^5-665287T^4+1397797T^3-2271085T^2+3006128T-3296368$
	10^a_{21}	$-2T^3+7T^2-9T+9$	3 / ✘	$9T^5-44T^4+80T^3-104T^2+121T-124$	2 / ✘	$62T^{12}-496T^{11}+1203T^{10}+2078T^9-24456T^8+97163T^7-267878T^6+592041T^5-1106738T^4+1789591T^3-2525732T^2+3113752T-3341184$
	10^a_{23}	$2T^3-7T^2+13T-15$	3 / ✘	$-5T^5+24T^4-67T^3+108T^2-137T+144$	1 / ✘	$118T^{12}-1272T^{11}+6541T^{10}-20402T^9+38443T^8-21945T^7-132442T^6+594335T^5-1530420T^4+2960363T^3-4622193T^2+5992048T-6526360$
	10^a_{25}	$-2T^3+8T^2-14T+17$	3 / ✘	$9T^5-52T^4+131T^3-232T^2+314T-344$	2 / ✘	$62T^{12}-584T^{11}+1856T^{10}+2264T^9-47052T^8+241288T^7-809541T^6+2068016T^5-4270010T^4+7347930T^3-10723331T^2+13406206T-14434208$
	10^a_{27}	$2T^3-8T^2+16T-19$	3 / ✘	$5T^5-28T^4+87T^3-164T^2+229T-252$	1 / ✘	$118T^{12}-1464T^{11}+8536T^{10}-29792T^9+62096T^8-39696T^7-242195T^6+1151848T^5-3078140T^4+6098910T^3-9661940T^2+12621240T-13779050$
	10^a_{29}	$T^3-7T^2+15T-17$	3 / ✘	$T^5-12T^4+52T^3-104T^2+124T-128$	2 / ✘	$8T^{12}-175T^{11}+1659T^{10}-8913T^9+29252T^8-54292T^7+10686T^6+290989T^5-1126663T^4+2673211T^3-4723498T^2+6566572T-7317656$
	10^a_{31}	$4T^2-14T+21$	2 / ✘	$-4T^2+9T-12$	1 / ✘	$992T^8-9440T^7+36936T^6-59136T^5-72624T^4+623304T^3-1691899T^2+2867550T-3391374$
	10^a_{33}	$4T^2-16T+25$	2 / ✘	0	1 / ✔	$992T^8-10816T^7+47856T^6-88336T^5-84402T^4+920320T^3-2655340T^2+4640912T-5542372$
	10^a_{35}	$2T^2-12T+21$	2 / ✔	$-T^3+12T^2-47T+76$	2 / ✘	$62T^8-1000T^7+6244T^6-15744T^5-15707T^4+232680T^3-775840T^2+1474372T-1810118$
	10^a_{37}	$4T^2-13T+19$	2 / ✘	0	2 / ✔	$992T^8-8736T^7+31914T^6-47212T^5-64499T^4+497921T^3-1308755T^2+2181630T-2566522$
	10^a_{39}	$-2T^3+8T^2-13T+15$	3 / ✘	$9T^5-52T^4+125T^3-204T^2+263T-280$	2 / ✘	$62T^{12}-584T^{11}+1788T^{10}+2480T^9-44191T^8+213488T^7-683173T^6+1684054T^5-3393468T^4+5753447T^3-8330571T^2+10379080T-11164828$
	10^a_{41}	$T^3-7T^2+17T-21$	3 / ✘	$T^5-12T^4+54T^3-120T^2+157T-164$	2 / ✘	$8T^{12}-175T^{11}+1697T^{10}-9543T^9+33561T^8-69114T^7+29117T^6+354127T^5-1527139T^4+3836499T^3-7019042T^2+9942516T-11145016$
	10^a_{43}	$-T^3+7T^2-17T+23$	3 / ✘	0	2 / ✔	$9T^{12}-203T^{11}+2051T^{10}-12253T^9+47594T^8-120962T^7+170450T^6+61017T^5-1045911T^4+3175271T^3-6209661T^2+9025932T-10186676$
	10^a_{45}	$-T^3+7T^2-21T+31$	3 / ✘	0	2 / ✔	$9T^{12}-203T^{11}+2135T^{10}-13689T^9+58324T^8-165246T^7+266640T^6+52413T^5-1738539T^4+5821367T^3-12123077T^2+18290148T-20900556$
	10^a_{47}	$T^4-3T^3+6T^2-7T+7$	4 / ✘	$-2T^7+8T^6-23T^5+38T^4-56T^3+60T^2-68T+64$	2, 3 / ✘	$12T^{16}-117T^{15}+598T^{14}-2030T^{13}+4959T^{12}-8715T^{11}+9312T^{10}+2921T^9-44823T^8+139602T^7-312112T^6+579182T^5-936546T^4+1347538T^3-1741633T^2+2029805T-2135930$

knot diag	n_k^t	Alexander's ω^+	genus / ribbon	p_1^+	unknotting # / amphi?	p_2^+
	10^a_{48}	$T^4-3T^3+6T^2-9T+11$	4 / ✔	$T^5-2T^4+2T^3-3T+4$	2 / ✘	$16T^{16}-165T^{15}+906T^{14}-3452T^{13}+10069T^{12}-23423T^{11}+43765T^{10}-63343T^9+59588T^8+8232T^7-192505T^6+537134T^5-1048176T^4+1669528T^3-2281994T^2+2735109T-2902594$
	10^a_{49}	$3T^3-8T^2+12T-13$	3 / ✘	$30T^5-94T^4+196T^3-292T^2+372T-392$	3 / ✘	$-177T^{12}+3028T^{11}-22080T^{10}+101361T^9-341354T^8+914348T^7-2044469T^6+3931812T^5-6622778T^4+9874270T^3-13105110T^2+15522532T-16422794$
	10^a_{50}	$-2T^3+7T^2-11T+13$	3 / ✘	$-9T^5+44T^4-94T^3+150T^2-186T+200$	2 / ✘	$62T^{12}-496T^{11}+1283T^{10}+2094T^9-29732T^8+134301T^7-412809T^6+990903T^5-1959941T^4+3278621T^3-4702408T^2+5824956T-6253664$
	10^a_{51}	$2T^3-7T^2+15T-19$	3 / ✘	$-5T^5+24T^4-73T^3+134T^2-194T+212$	2, 3 / ✘	$118T^{12}-1272T^{11}+6813T^{10}-22602T^9+45771T^8-28275T^7-180411T^6+857569T^5-2306697T^4+4602641T^3-7332665T^2+9612128T-10506256$
	10^a_{52}	$2T^3-7T^2+13T-15$	3 / ✘	$-3T^5+16T^4-37T^3+50T^2-49T+44$	2 / ✘	$134T^{12}-1480T^{11}+7961T^{10}-27058T^9+62159T^8-88993T^7+22042T^6+296843T^5-1040240T^4+2254967T^3-3720017T^2+4952400T-5437448$
	10^a_{53}	$6T^2-18T+25$	2 / ✘	$93T^3-346T^2+680T-828$	2, 3 / ✘	$-3642T^8+58248T^7-417976T^6+1846212T^5-5694639T^4+13084936T^3-23231163T^2+32545278T-36374532$
	10^a_{54}	$2T^3-6T^2+10T-11$	3 / ✘	$-3T^5+12T^4-24T^3+26T^2-21T+16$	2, 3 / ✘	$134T^{12}-1272T^{11}+5964T^{10}-17880T^9+36606T^8-46740T^7+6565T^6+150576T^5-487825T^4+1010638T^3-1619593T^2+2120978T-2316318$
	10^a_{55}	$5T^2-15T+21$	2 / ✘	$66T^3-246T^2+488T-596$	2 / ✘	$-1966T^8+30491T^7-215627T^6+945597T^5-2905831T^4+6662951T^3-11814712T^2+16540014T-18481854$
	10^a_{56}	$-2T^3+8T^2-14T+17$	3 / ✘	$-9T^5+52T^4-133T^3+234T^2-312T+340$	2 / ✘	$62T^{12}-584T^{11}+1800T^{10}+2840T^9-49588T^8+247616T^7-819257T^6+2077408T^5-4277830T^4+7364010T^3-10765639T^2+13481990T-14525656$
	10^a_{57}	$2T^3-8T^2+18T-23$	3 / ✘	$-5T^5+28T^4-93T^3+194T^2-300T+340$	2 / ✘	$118T^{12}-1464T^{11}+8808T^{10}-32264T^9+71276T^8-49320T^7-305843T^6+1537376T^5-4286854T^4+8774390T^3-14221383T^2+18829374T-20648444$
	10^a_{58}	$3T^2-16T+27$	2 / ✘	$3T^3-28T^2+94T-140$	2 / ✘	$309T^8-4384T^7+24039T^6-49896T^5-90763T^4+864784T^3-2647834T^2+4837480T-5867454$
	10^a_{59}	$T^3-7T^2+18T-23$	3 / ✘	$-T^5+12T^4-55T^3+128T^2-181T+196$	1 / ✘	$8T^{12}-175T^{11}+1716T^{10}-9858T^9+35706T^8-76124T^7+33704T^6+412653T^5-1824096T^4+4655939T^3-8596644T^2+12230816T-13727286$
	10^a_{60}	$-T^3+7T^2-20T+29$	3 / ✘	$5T^3-40T^2+122T-176$	1 / ✘	$9T^{12}-203T^{11}+2114T^{10}-13338T^9+55732T^8-154496T^7+241898T^6+66137T^5-1621594T^4+5326603T^3-10989858T^2+16499428T-18824860$
	10^a_{61}	$-2T^3+5T^2-6T+7$	3 / ✘	$-7T^5+20T^4-27T^3+36T^2-35T+36$	2, 3 / ✘	$94T^{12}-672T^{11}+2231T^{10}-4382T^9+4108T^8+6320T^7-40187T^6+113296T^5-235714T^4+400470T^3-576529T^2+714816T-767686$
	10^a_{62}	$T^4-3T^3+6T^2-8T+9$	4 / ✘	$-2T^7+8T^6-23T^5+40T^4-63T^3+76T^2-89T+88$	2 / ✘	$12T^{16}-117T^{15}+598T^{14}-2057T^{13}+5172T^{12}-9509T^{11}+10856T^{10}+2734T^9-54502T^8+178917T^7-414312T^6+786766T^5-1289208T^4+1865866T^3-2414454T^2+2812025T-2957594$
	10^a_{63}	$5T^2-14T+19$	2 / ✘	$66T^3-220T^2+416T-496$	2 / ✘	$-1966T^8+28318T^7-188080T^6+783388T^5-2311570T^4+5141906T^3-8929148T^2+12349082T-13743884$
	10^a_{64}	$-T^4+3T^3-6T^2+10T-11$	4 / ✘	$-T^7+4T^6-11T^5+24T^4-37T^3+52T^2-60T+64$	2 / ✘	$15T^{16}-153T^{15}+830T^{14}-3147T^{13}+9133T^{12}-20983T^{11}+37963T^{10}-50164T^9+30642T^8+68741T^7-310036T^6+745430T^5-1381735T^4+2150560T^3-2906317T^2+3464829T-3671204$
	10^a_{65}	$2T^3-7T^2+14T-17$	3 / ✘	$-5T^5+24T^4-71T^3+124T^2-169T+180$	2 / ✘	$118T^{12}-1272T^{11}+6657T^{10}-21282T^9+40874T^8-20768T^7-166691T^6+742216T^5-1933704T^4+3781794T^3-5950947T^2+7749120T-8452246$
	10^a_{66}	$3T^3-9T^2+16T-19$	3 / ✘	$30T^5-112T^4+279T^3-480T^2+662T-724$	3 / ✘	$-177T^{12}+3321T^{11}-27536T^{10}+145346T^9-561614T^8+1706788T^7-4256134T^6+8946173T^5-16135424T^4+25271935T^3-34647456T^2+41790680T-44471832$
	10^a_{67}	$-4T^2+16T-23$	2 / ✘	$24T^3-140T^2+312T-392$	2 / ✘	$416T^8-1696T^7-18592T^6+205384T^5-971474T^4+2884880T^3-6004484T^2+9188872T-10566612$
	10^a_{68}	$4T^2-14T+21$	2 / ✘	$8T^3-40T^2+117T-164$	2 / ✘	$928T^8-8448T^7+29784T^6-26736T^5-178984T^4+891736T^3-2217147T^2+3657390T-4297054$
	10^a_{69}	$T^3-7T^2+21T-29$	3 / ✘	$-T^5+12T^4-68T^3+212T^2-397T+476$	2 / ✘	$8T^{12}-175T^{11}+1753T^{10}-10339T^9+37435T^8-68174T^7-78997T^6+1015635T^5-3880779T^4+9697491T^3-17937826T^2+25646300T-28844672$
	10^a_{70}	$T^3-7T^2+16T-19$	3 / ✘	$-T^5+12T^4-53T^3+114T^2-146T+152$	2 / ✘	$8T^{12}-175T^{11}+1678T^{10}-9220T^9+31251T^8-60450T^7+14335T^6+337593T^5-1351773T^4+3275803T^3-5864336T^2+8208654T-9166724$
	10^a_{71}	$-T^3+7T^2-18T+25$	3 / ✘	T^3-2T^2-T+4	1 / ✘	$9T^{12}-203T^{11}+2072T^{10}-12608T^9+50167T^8-131082T^7+190655T^6+64937T^5-1206917T^4+3745659T^3-7436102T^2+10906778T-12346734$
	10^a_{72}	$-2T^3+9T^2-16T+19$	3 / ✘	$-9T^5+60T^4-167T^3+298T^2-410T+448$	2 / ✘	$62T^{12}-672T^{11}+2407T^{10}+2846T^9-67046T^8+358714T^7-1237440T^6+3225136T^5-6760702T^4+11767984T^3-17315777T^2+21757146T-23465324$
	10^a_{73}	$T^3-7T^2+20T-27$	3 / ✘	$T^5-12T^4+65T^3-194T^2+350T-416$	1 / ✘	$8T^{12}-175T^{11}+1738T^{10}-10112T^9+36117T^8-66038T^7-61235T^6+869449T^5-3296603T^4+8133803T^3-14880880T^2+21122890T-23697928$
	10^a_{74}	$-4T^2+16T-23$	2 / ✘	$24T^3-136T^2+290T-360$	2 / ✘	$416T^8-1984T^7-14448T^6+178832T^5-870542T^4+2626104T^3-5521764T^2+8500760T-9794748$
	10^a_{75}	$-T^3+7T^2-19T+27$	3 / ✔	$-4T^3+36T^2-117T+172$	2 / ✘	$9T^{12}-203T^{11}+2093T^{10}-12979T^9+53085T^8-144060T^7+222795T^6+45939T^5-1382507T^4+4528919T^3-9302365T^2+13926940T-15875332$
	10^a_{76}	$-2T^3+7T^2-12T+15$	3 / ✘	$-9T^5+44T^4-104T^3+184T^2-245T+272$	2, 3 / ✘	$62T^{12}-496T^{11}+1263T^{10}+2926T^9-37611T^8+174774T^7-553794T^6+1359740T^5-2727505T^4+4595668T^3-6610039T^2+8193314T-8796596$
	10^a_{77}	$2T^3-7T^2+14T-17$	3 / ✘	$-5T^5+24T^4-71T^3+132T^2-189T+208$	2, 3 / ✘	$118T^{12}-1272T^{11}+6657T^{10}-21170T^9+39602T^8-13480T^7-193563T^6+812568T^5-2072452T^4+3997538T^3-6227879T^2+8058912T-8771174$
	10^a_{78}	$-T^3+7T^2-16T+21$	3 / ✘	$2T^5-24T^4+105T^3-244T^2+390T-448$	2 / ✘	$5T^{12}-91T^{11}+626T^{10}-1310T^9-9682T^8+98268T^7-472808T^6+1558897T^5-3892200T^4+7699107T^3-12365278T^2+16351352T-17933784$
	10^a_{79}	$T^4-3T^3+7T^2-12T+15$	4 / ✘	0	2, 3 / ✔	$16T^{16}-165T^{15}+951T^{14}-3892T^{13}+12327T^{12}-31301T^{11}+64047T^{10}-102088T^9+108942T^8-5172T^7-328635T^6+1013644T^5-2099318T^4+3486798T^3-4904824T^2+5979109T-6380898$
	10^a_{80}	$3T^3-9T^2+15T-17$	3 / ✘	$30T^5-112T^4+260T^3-426T^2+568T-616$	3 / ✘	$-177T^{12}+3321T^{11}-26919T^{10}+137419T^9-511788T^8+1500906T^7-3625608T^6+7420093T^5-13101785T^4+20196767T^3-27388655T^2+32826444T-34860060$
	10^a_{81}	$-T^3+8T^2-20T+27$	3 / ✘	0	2 / ✔	$9T^{12}-232T^{11}+2632T^{10}-17347T^9+73146T^8-199476T^7+303717T^6+63516T^5-1783222T^4+5636674T^3-11239918T^2+16501092T-18681194$

knot diag	n_k^t p_1^+	Alexander's ω^+	genus / ribbon unknotting # / amphi?	p_2^+
	10^a_{82} $T^7-6T^6+19T^5-42T^4+64T^3-78T^2+84T-84$	$-T^4+4T^3-8T^2+12T-13$	4 / ✗ 1 / ✗	$15T^{16}-204T^{15}+1362T^{14}-5956T^{13}+19067T^{12}-46940T^{11}+89646T^{10}-125984T^9+94379T^8+118488T^7-663600T^6+1675944T^5-3187626T^4+5046508T^3-6899632T^2+8282752T-8796438$
	10^a_{83} $-5T^5+34T^4-110T^3+214T^2-301T+332$	$2T^3-9T^2+19T-23$	3 / ✗ 2 / ✗	$118T^{12}-1632T^{11}+10501T^{10}-40166T^9+92154T^8-74661T^7-344938T^6+1829049T^5-5155786T^4+10589003T^3-17184002T^2+22763416T-24966116$
	10^a_{84} $-5T^5+34T^4-116T^3+246T^2-373T+424$	$2T^3-9T^2+20T-25$	3 / ✗ 1 / ✗	$118T^{12}-1632T^{11}+10601T^{10}-40970T^9+93361T^8-60130T^7-457712T^6+2276184T^5-6379977T^4+13131088T^3-21370125T^2+28363542T-31128704$
	10^a_{85} $2T^7-12T^6+36T^5-68T^4+101T^3-124T^2+138T-140$	$T^4-4T^3+8T^2-10T+11$	4 / ✗ 2 / ✗	$12T^{16}-156T^{15}+986T^{14}-3982T^{13}+11319T^{12}-23042T^{11}+29987T^{10}-3098T^9-116460T^8+418314T^7-1005425T^6+1953048T^5-3252398T^4+4764776T^3-6220611T^2+7285042T-7676632$
	10^a_{86} $-T^5+6T^4-21T^3+58T^2-105T+128$	$-2T^3+9T^2-19T+25$	3 / ✗ 2 / ✗	$142T^{12}-2056T^{11}+14135T^{10}-60346T^9+173073T^8-322457T^7+256132T^6+640839T^5-3192178T^4+7806511T^3-13712731T^2+18852080T-20906284$
	10^a_{87} $-T^5+6T^4-23T^3+66T^2-125T+152$	$-2T^3+9T^2-18T+23$	3 / ✓ 2 / ✗	$142T^{12}-2056T^{11}+13955T^{10}-58318T^9+162798T^8-293228T^7+214867T^6+612960T^5-2882460T^4+6902570T^3-11979669T^2+16361444T-18106010$
	10^a_{88} 0	$-T^3+8T^2-24T+35$	3 / ✗ 1 / ✓	$9T^{12}-232T^{11}+2716T^{10}-18955T^9+86300T^8-257664T^7+436281T^6+55760T^5-2823656T^4+9657962T^3-20306480T^2+30775472T-35215022$
	10^a_{89} $T^5-14T^4+83T^3-264T^2+495T-596$	$T^3-8T^2+24T-33$	3 / ✗ 2 / ✗	$8T^{12}-200T^{11}+2236T^{10}-14461T^9+56992T^8-117072T^7-76152T^6+1508604T^5-6093936T^4+15620030T^3-29286604T^2+42155400T-47509694$
	10^a_{90} $-T^5+6T^4-21T^3+54T^2-93T+112$	$-2T^3+8T^2-17T+23$	3 / ✗ 2 / ✗	$142T^{12}-1824T^{11}+11452T^{10}-45568T^9+123153T^8-214976T^7+138515T^6+523918T^5-2309034T^4+54584443T^3-9432309T^2+12861496T-14226804$
	10^a_{91} $T^5-2T^4+2T^3-3T+4$	$T^4-4T^3+9T^2-14T+17$	4 / ✗ 1 / ✗	$16T^{16}-220T^{15}+1535T^{14}-7166T^{13}+24885T^{12}-67476T^{11}+145070T^{10}-242014T^9+278753T^8-78212T^7-624329T^6+2091910T^5-4424108T^4+7397630T^3-10425418T^2+12711814T-13565348$
	10^a_{92} $-9T^5+68T^4-216T^3+428T^2-622T+696$	$-2T^3+10T^2-20T+25$	3 / ✗ 2 / ✗	$62T^{12}-760T^{11}+3228T^{10}+1776T^9-90686T^8+555772T^7-2114169T^6+5951964T^5-13251159T^4+24127850T^3-36624016T^2+46862460T-50844652$
	10^a_{93} $3T^5-18T^4+43T^3-58T^2+55T-48$	$2T^3-8T^2+15T-17$	3 / ✗ 2 / ✗	$134T^{12}-1696T^{11}+10180T^{10}-37880T^9+94183T^8-147272T^7+62729T^6+424866T^5-1618596T^4+3616743T^3-6059793T^2+8130868T-8948936$
	10^a_{94} $-T^7+6T^6-20T^5+46T^4-76T^3+102T^2-115T+120$	$-T^4+4T^3-9T^2+14T-15$	4 / ✗ 2 / ✗	$15T^{16}-204T^{15}+1405T^{14}-6454T^{13}+21907T^{12}-57432T^{11}+117080T^{10}-176754T^9+150405T^8+135972T^7-928717T^6+2460642T^5-4804019T^4+7729462T^3-10672990T^2+12881566T-13703760$
	10^a_{95} $-5T^5+32T^4-114T^3+248T^2-384T+436$	$2T^3-9T^2+21T-27$	3 / ✗ 1 / ✗	$118T^{12}-1656T^{11}+11045T^{10}-44462T^9+109118T^8-104035T^7-391583T^6+2298083T^5-6804711T^4+14456709T^3-24008082T^2+32236696T-35514492$
	10^a_{96} $-7T^3+50T^2-147T+212$	$-T^3+7T^2-22T+33$	3 / ✗ 2 / ✗	$9T^{12}-203T^{11}+2156T^{10}-14060T^9+61189T^8-177034T^7+287437T^6+96689T^5-2149699T^4+7231587T^3-15228082T^2+23163354T-26546674$
	10^a_{97} $-37T^3+242T^2-603T+788$	$-5T^2+22T-33$	2 / ✗ 2 / ✗	$1061T^8-5486T^7-47090T^6+615064T^5-3157165T^4+9904926T^3-21376446T^2+33395786T-38661308$
	10^a_{98} $9T^5-60T^4+177T^3-348T^2+501T-564$	$-2T^3+9T^2-18T+23$	3 / ✗ 2 / ✗	$62T^{12}-672T^{11}+2575T^{10}+1666T^9-67602T^8+398948T^7-1483813T^6+4115776T^5-9069800T^4+16396378T^3-24767965T^2+31602148T-34255402$
	10^a_{99} 0	$T^4-4T^3+10T^2-16T+19$	4 / ✓ 2 / ✓	$16T^{16}-220T^{15}+1580T^{14}-7688T^{13}+27976T^{12}-79612T^{11}+179656T^{10}-315060T^9+386272T^8-148160T^7-792172T^6+2854748T^5-6237824T^4+10649644T^3-15214156T^2+18696608T-20003232$
	10^a_{100} $2T^7-12T^6+39T^5-80T^4+128T^3-164T^2+192T-196$	$T^4-4T^3+9T^2-12T+13$	4 / ✗ 2, 3 / ✗	$12T^{16}-156T^{15}+1019T^{14}-4340T^{13}+13189T^{12}-29012T^{11}+41715T^{10}-11232T^9-153611T^8+603116T^7-1520513T^6+3049452T^5-5190414T^4+7715304T^3-10164234T^2+11961684T-12623974$
	10^a_{101} $-129T^3+480T^2-942T+1148$	$7T^2-21T+29$	2 / ✗ 2, 3 / ✗	$-7453T^8+115979T^7-819947T^6+3586847T^5-10987573T^4+25120359T^3-44443695T^2+62133778T-69396618$
	10^a_{102} $-T^5+6T^4-19T^3+50T^2-89T+108$	$-2T^3+8T^2-16T+21$	3 / ✗ 1 / ✗	$142T^{12}-1824T^{11}+11296T^{10}-44000T^9+115984T^8-197200T^7+123203T^6+462512T^5-1996064T^4+4649298T^3-7951840T^2+10777160T-11897326$
	10^a_{103} $5T^5-30T^4+93T^3-178T^2+254T-280$	$2T^3-8T^2+17T-21$	3 / ✗ 3 / ✗	$118T^{12}-1440T^{11}+8404T^{10}-29584T^9+61863T^8-33736T^7-289763T^6+1355186T^5-3666373T^4+7367413T^3-11802974T^2+15525908T-16990056$
	10^a_{104} $T^5-2T^4+2T^3-3T+4$	$T^4-4T^3+9T^2-15T+19$	4 / ✗ 1 / ✗	$16T^{16}-220T^{15}+1535T^{14}-7197T^{13}+25227T^{12}-69332T^{11}+151513T^{10}-257279T^9+301366T^8-83393T^7-710402T^6+2409469T^5-5162297T^4+8726478T^3-12397663T^2+15191203T-16238052$
	10^a_{105} $-T^5+14T^4-71T^3+184T^2-292T+332$	$T^3-8T^2+22T-29$	3 / ✗ 2 / ✗	$8T^{12}-200T^{11}+2218T^{10}-14261T^9+57123T^8-132986T^7+65302T^6+805306T^5-3722841T^4+9784430T^3-18400587T^2+26441286T-29769592$
	10^a_{106} $-T^7+6T^6-20T^5+48T^4-82T^3+114T^2-134T+140$	$-T^4+4T^3-9T^2+15T-17$	4 / ✗ 2 / ✗	$15T^{16}-204T^{15}+1405T^{14}-6481T^{13}+22197T^{12}-58948T^{11}+122017T^{10}-186937T^9+159252T^8+161653T^7-1073190T^6+2872671T^5-5674479T^4+9221494T^3-12827310T^2+15551003T-16568312$
	10^a_{107} $2T^3-8T^2+13T-16$	$-T^3+8T^2-22T+31$	3 / ✗ 1 / ✗	$9T^{12}-232T^{11}+2674T^{10}-18155T^9+79705T^8-227986T^7+366663T^6+65430T^5-2285283T^4+7518398T^3-15408513T^2+22997470T-26180364$
	10^a_{108} $-3T^5+18T^4-41T^3+50T^2-40T+32$	$2T^3-8T^2+14T-15$	3 / ✗ 2 / ✗	$134T^{12}-1696T^{11}+10032T^{10}-36416T^9+87916T^8-133860T^7+58617T^6+353392T^5-1337642T^4+2961006T^3-4930449T^2+6594854T-7251776$
	10^a_{109} 0	$T^4-4T^3+10T^2-17T+21$	4 / ✗ 2 / ✓	$16T^{16}-220T^{15}+1580T^{14}-7719T^{13}+28318T^{12}-81525T^{11}+186591T^{10}-332351T^9+413696T^8-158284T^7-889129T^6+3239371T^5-7165411T^4+12361738T^3-17799197T^2+21979657T-23554274$
	10^a_{110} $T^5-14T^4+69T^3-160T^2+219T-236$	$T^3-8T^2+20T-25$	3 / ✗ 2 / ✗	$8T^{12}-200T^{11}+2180T^{10}-13569T^9+52114T^8-116472T^7+61616T^6+604668T^5-2747906T^4+7072274T^3-13103918T^2+18672836T-20967250$
	10^a_{111} $-9T^5+60T^4-171T^3+316T^2-436T+480$	$-2T^3+9T^2-17T+21$	3 / ✗ 2 / ✗	$62T^{12}-672T^{11}+2507T^{10}+1894T^9-64067T^8+361705T^7-1299145T^6+3506889T^5-7575591T^4+13510069T^3-20234835T^2+25700228T-27818092$
	10^a_{112} $T^7-8T^6+29T^5-68T^4+115T^3-152T^2+175T-180$	$-T^4+5T^3-11T^2+17T-19$	4 / ✗ 2 / ✗	$15T^{16}-255T^{15}+2068T^{14}-10699T^{13}+39650T^{12}-111160T^{11}+239401T^{10}-381338T^9+357595T^8+215240T^7-1900590T^6+5252099T^5-10470652T^4+17062683T^3-23747257T^2+28786648T-30666904$
	10^a_{113} $-5T^5+42T^4-167T^3+394T^2-623T+720$	$2T^3-11T^2+26T-33$	3 / ✗ 1 / ✗	$118T^{12}-2016T^{11}+15681T^{10}-71126T^9+190712T^8-187416T^7-827053T^6+4935892T^5-14986146T^4+32456282T^3-54606535T^2+73872380T-81581546$
	10^a_{114} $T^5-8T^4+30T^3-78T^2+140T-168$	$-2T^3+10T^2-21T+27$	3 / ✗ 1 / ✗	$142T^{12}-2280T^{11}+16976T^{10}-76976T^9+230999T^8-445876T^7+369450T^6+890044T^5-4554487T^4+11256519T^3-19890736T^2+27431686T-30450926$
	10^a_{115} 0	$-T^3+9T^2-26T+37$	3 / ✗ 2 / ✓	$9T^{12}-261T^{11}+3345T^{10}-24942T^9+118870T^8-365932T^7+636497T^6+31527T^5-3907730T^4+13472649T^3-28298039T^2+42798944T-48929878$

knot diag	n_k^t	Alexander's ω^+	p_1^+	p_2^+	genus / ribbon	unknotting # / amphi?
	10^a_{116}	$-T^4+5T^3-12T^2+19T-21$	$T^7-8T^6+30T^5-74T^4+132T^3-184T^2+217T-228$	$15T^{16}-255T^{15}+2111T^{14}-11302T^{13}+43668T^{12}-128023T^{11}+288575T^{10}-482307T^9+485985T^8+215018T^7-2416711T^6+6942030T^5-14142246T^4+23374622T^3-32832655T^2+40008697T-42694444$	4 / ✗	2 / ✗
	10^a_{117}	$2T^3-10T^2+24T-31$	$-5T^5+38T^4-144T^3+330T^2-522T+600$	$118T^{12}-1824T^{11}+13156T^{10}-56312T^9+143746T^8-128212T^7-648731T^6+3701012T^5-11080717T^4+238442230T^3-39994730T^2+54033352T-59650184$	3 / ✗	2 / ✗
	10^a_{118}	$T^4-5T^3+12T^2-19T+23$	0	$16T^{16}-275T^{15}+2305T^{14}-12526T^{13}+49379T^{12}-149077T^{11}+352067T^{10}-641987T^9+825146T^8-399494T^7-1458086T^6+5641784T^5-12589879T^4+21712756T^3-31187934T^2+38432195T-41152780$	4 / ✗	1 / ✓
	10^a_{119}	$-2T^3+10T^2-23T+31$	$-T^5+6T^4-26T^3+86T^2-175T+220$	$142T^{12}-2288T^{11}+17392T^{10}-81560T^9+255719T^8-521820T^7+483354T^6+990524T^5-5618050T^4+14499405T^3-26339835T^2+36916418T-41198798$	3 / ✗	1 / ✗
	10^a_{120}	$8T^2-26T+37$	$166T^3-692T^2+1433T-1788$	$-11768T^8+201320T^7-1541132T^6+7193960T^5-23193562T^4+55098408T^3-100101157T^2+142136186T-159564534$	2 / ✗	2, 3 / ✗
	10^a_{121}	$2T^3-11T^2+27T-35$	$5T^5-42T^4+167T^3-396T^2+634T-732$	$118T^{12}-2016T^{11}+15853T^{10}-73450T^9+204605T^8-232351T^7-764251T^6+5054205T^5-15890853T^4+351606633T^3-59996079T^2+81831748T-90616328$	3 / ✗	2 / ✗
	10^a_{122}	$-2T^3+11T^2-24T+31$	$-T^5+8T^4-34T^3+104T^2-211T+264$	$142T^{12}-2512T^{11}+20355T^{10}-99362T^9+318535T^8-657014T^7+617040T^6+1199636T^5-6869579T^4+17663208T^3-31953091T^2+44656222T-49787168$	3 / ✗	2 / ✗
	10^a_{123}	$T^4-6T^3+15T^2-24T+29$	0	$16T^{16}-330T^{15}+3216T^{14}-19770T^{13}+86170T^{12}-282500T^{11}+715162T^{10}-1388790T^9+1917350T^8-1169720T^7-2832520T^6+12363784T^5-28689660T^4+50560110T^3-73579700T^2+91325158T-98015944$	4 / ✓	2 / ✓
	10^n_{124}	T^4-T^3+T-1	$-4T^7-6T^4-4T^2-6T$	$9T^{15}-25T^{14}+10T^{13}+75T^{12}-177T^{11}+155T^{10}+113T^9-570T^8+850T^7-428T^6-824T^5+2167T^4-2340T^3+510T^2+2375T-3832$	4 / ✗	4 / ✗
	10^n_{125}	T^3-2T^2+2T-1	$-T^5+2T^4-2T^3+3T-4$	$8T^{12}-50T^{11}+151T^{10}-289T^9+417T^8-524T^7+536T^6-150T^5-1168T^4+3942T^3-8130T^2+12314T-14126$	3 / ✗	2 / ✗
	10^n_{126}	T^3-2T^2+4T-5	$T^5-2T^4+10T^3-12T^2+22T-20$	$8T^{12}-50T^{11}+185T^{10}-457T^9+666T^8-18T^7-3074T^6+10724T^5-24495T^4+43738T^3-64631T^2+81072T-87356$	3 / ✗	2 / ✗
	10^n_{127}	$-T^3+4T^2-6T+7$	$2T^5-14T^4+32T^3-52T^2+67T-72$	$5T^{12}-48T^{11}+128T^{10}+289T^9-3551T^8+15554T^7-46589T^6+109206T^5-211625T^4+348370T^3-494107T^2+608154T-651576$	3 / ✗	2 / ✗
	10^n_{128}	$2T^3-3T^2+T+1$	$-13T^5+12T^4-3T^3-10T^2-9T+12$	$-26T^{12}+296T^{11}-1071T^{10}+1750T^9-1107T^8+287T^7-2938T^6+7959T^5-7820T^4+3175T^3-8727T^2+28392T-40368$	3 / ✗	3 / ✗
	10^n_{129}	$2T^2-6T+9$	$-T^3-2T^2+14T-20$	$62T^8-568T^7+2280T^6-4308T^5-553T^4+25616T^3-76125T^2+132258T-157332$	2 / ✓	1 / ✗
	10^n_{130}	$2T^2-4T+5$	$T^3-2T^2+19T-24$	$62T^8-336T^7+924T^6-1568T^5+253T^4+8384T^3-28668T^2+53628T-65374$	2 / ✗	2 / ✗
	10^n_{131}	$-2T^2+8T-11$	$5T^3-38T^2+87T-112$	$38T^8-272T^7-580T^6+12792T^5-66417T^4+202096T^3-422662T^2+646440T-742870$	2 / ✗	1 / ✗
	10^n_{132}	T^2-T+1	$2T^2+5T-4$	$4T^8-7T^7+12T^6-145T^5+508T^4-631T^3-322T^2+2150T-3150$	2 / ✗	1 / ✗
	10^n_{133}	$-T^2+5T-7$	$T^3-14T^2+37T-48$	$3T^8-43T^7+16T^6+1489T^5-9322T^4+30945T^3-68047T^2+106954T-123994$	2 / ✗	1 / ✗
	10^n_{134}	$2T^3-4T^2+4T-3$	$-13T^5+24T^4-33T^3+30T^2-41T+40$	$-26T^{12}+376T^{11}-2056T^{10}+6760T^9-16248T^8+32568T^7-58951T^6+98316T^5-150194T^4+210738T^3-273246T^2+324124T-344346$	3 / ✗	3 / ✗
	10^n_{135}	$3T^2-9T+13$	$T^3-6T^2+18T-24$	$321T^8-2613T^7+8905T^6-12033T^5-19329T^4+132451T^3-337025T^2+553002T-647370$	2 / ✗	2 / ✗
	10^n_{136}	$-T^2+4T-5$	$-T^3+4T^2-2T-4$	$3T^8-36T^7+189T^6-512T^5+347T^4+2660T^3-11142T^2+22668T-28354$	2 / ✗	1 / ✗
	10^n_{137}	$T^2-6T+11$	$-4T^2+24T-44$	$4T^8-74T^7+512T^6-1420T^5-1160T^4+21074T^3-72904T^2+140922T-173900$	2 / ✓	1 / ✗
	10^n_{138}	T^3-5T^2+8T-7	$-T^5+8T^4-22T^3+24T^2-11T+8$	$8T^{12}-125T^{11}+855T^{10}-3374T^9+8458T^8-13328T^7+8173T^6+25863T^5-114602T^4+277037T^3-497313T^2+702260T-787812$	3 / ✗	2 / ✗
	10^n_{139}	T^4-T^3+2T-3	$-4T^7-12T^4+5T^3-4T^2-16T+12$	$9T^{15}-25T^{14}-3T^{13}+172T^{12}-425T^{11}+290T^{10}+924T^9-3099T^8+4327T^7-1756T^6-5200T^5+12117T^4-11846T^3+1547T^2+12451T-19002$	4 / ✗	4 / ✗
	10^n_{140}	T^2-2T+3	$8T-8$	$4T^8-22T^7+90T^6-292T^5+424T^4+430T^3-3056T^2+6470T-8104$	2 / ✓	2 / ✗
	10^n_{141}	$-T^3+3T^2-4T+5$	$T^3-8T^2+16T-20$	$9T^{12}-87T^{11}+396T^{10}-1150T^9+2382T^8-3516T^7+2746T^6+3397T^5-19148T^4+46359T^3-80476T^2+109936T-121692$	3 / ✗	1 / ✗
	10^n_{142}	$2T^3-3T^2+2T-1$	$-13T^5+12T^4-13T^3+4T^2-17T+12$	$-26T^{12}+296T^{11}-1155T^{10}+2582T^9-4276T^8+6812T^7-11749T^6+19392T^5-27878T^4+36798T^3-48891T^2+62932T-69706$	3 / ✗	3 / ✗
	10^n_{143}	T^3-3T^2+6T-7	$T^5-4T^4+15T^3-28T^2+45T-48$	$8T^{12}-75T^{11}+362T^{10}-1106T^9+2070T^8-1092T^7-7698T^6+33841T^5-86216T^4+164927T^3-254838T^2+327896T-356170$	3 / ✗	1 / ✗
	10^n_{144}	$-3T^2+10T-13$	$10T^3-44T^2+80T-96$	$222T^8-1642T^7+3140T^6+12252T^5-94326T^4+307146T^3-651636T^2+998418T-1147140$	2 / ✗	2 / ✗
	10^n_{145}	T^2+T-3	$2T^3+8T^2+6T-8$	$-5T^7+7T^6+113T^5-141T^4-465T^3+730T^2+850T-2198$	2 / ✗	2 / ✗
	10^n_{146}	$2T^2-8T+13$	$T^3-8T^2+21T-28$	$62T^8-664T^7+2844T^6-4544T^5-9663T^4+71376T^3-197106T^2+340392T-405394$	2 / ✗	1 / ✗
	10^n_{147}	$-2T^2+7T-9$	$-3T^3+12T^2-15T+12$	$54T^8-488T^7+1697T^6-1694T^5-8312T^4+42905T^3-107222T^2+177492T-208860$	2 / ✗	1 / ✗
	10^n_{148}	T^3-3T^2+7T-9	$T^5-4T^4+18T^3-36T^2+62T-68$	$8T^{12}-75T^{11}+377T^{10}-1209T^9+2330T^8-864T^7-11900T^6+51677T^5-135261T^4+266207T^3-420746T^2+549160T-599424$	3 / ✗	2 / ✗
	10^n_{149}	$-T^3+5T^2-9T+11$	$2T^5-18T^4+55T^3-104T^2+149T-164$	$5T^{12}-61T^{11}+226T^{10}+339T^9-7195T^8+38874T^7-135727T^6+357173T^5-753890T^4+1318245T^3-1945105T^2+2447584T-2640944$	3 / ✗	2 / ✗
	10^n_{150}	$-T^3+4T^2-6T+7$	$-2T^5+12T^4-26T^3+38T^2-45T+44$	$5T^{12}-52T^{11}+216T^{10}-355T^9-719T^8+6578T^7-24361T^6+64526T^5-137117T^4+243126T^3-364723T^2+464942T-504136$	3 / ✗	2 / ✗
	10^n_{151}	$T^3-4T^2+10T-13$	$-T^5+6T^4-21T^3+42T^2-66T+72$	$8T^{12}-100T^{11}+632T^{10}-2529T^9+6645T^8-9606T^7-5854T^6+80466T^5-270269T^4+605378T^3-1033839T^2+1408362T-1558600$	3 / ✗	2 / ✗
	10^n_{152}	$T^4-T^3-T^2+4T-5$	$4T^7-7T^5+18T^4-7T^3-12T^2+45T-52$	$9T^{15}-14T^{14}-92T^{13}+396T^{12}-419T^{11}-1212T^{10}+5444T^9-9692T^8+6412T^7+11488T^6-39344T^5+55244T^4-33234T^3-30168T^2+102115T-133894$	4 / ✗	4 / ✗
	10^n_{153}	T^3-T^2-T+3	$T^5-2T^4+T^3+2T^2-T$	$8T^{12}-17T^{11}-46T^{10}+231T^9-381T^8+364T^7-367T^6+157T^5+1142T^4-2815T^3+1874T^2+2128T-4572$	3 / ✓	2 / ✗

knot diag	n_k^t p_1^+	Alexander's ω^+ p_2^+	genus / ribbon unknotting # / amphi?	knot diag	n_k^t p_1^+	Alexander's ω^+ p_2^+	genus / ribbon unknotting # / amphi?
	10^n_{154} $-3T^5-6T^4+13T^3-47T+68$	T^3-4T+7 $48T^{10}-93T^9-546T^8+2396T^7-1956T^6-8376T^5+25906T^4-23802T^3-25690T^2+102540T-140874$	3 / ✘ 3 / ✘		10^n_{155} $-2T^3+12T^2-22T+28$	$-T^3+3T^2-5T+7$ $9T^{12}-87T^{11}+417T^{10}-1321T^9+3014T^8-4806T^7+3646T^6+6917T^5-34773T^4+82963T^3-142781T^2+193836T-214060$	3 / ✔ 2 / ✘
	10^n_{156} $T^5-6T^4+19T^3-30T^2+33T-32$	T^3-4T^2+8T-9 $8T^{12}-100T^{11}+594T^{10}-2165T^9+5120T^8-6852T^7-2208T^6+41208T^5-134214T^4+293026T^3-493422T^2+668112T-738218$	3 / ✘ 1 / ✘		10^n_{157} $-2T^5+22T^4-78T^3+148T^2-218T+240$	$-T^3+6T^2-11T+13$ $5T^{12}-74T^{11}+340T^{10}+321T^9-11314T^8+67637T^7-250977T^6+688036T^5-1493487T^4+2661131T^3-3974091T^2+5034465T-5444000$	3 / ✘ 2 / ✘
	10^n_{158} $2T^2-7T+12$	$-T^3+4T^2-10T+15$ $9T^{12}-116T^{11}+764T^{10}-3275T^9+9743T^8-19422T^7+18439T^6+32898T^5-196271T^4+513374T^3-940025T^2+1323614T-1479452$	3 / ✘ 2 / ✘		10^n_{159} $T^5-6T^4+26T^3-60T^2+98T-112$	$T^3-4T^2+9T-11$ $8T^{12}-100T^{11}+609T^{10}-2267T^9+5047T^8-3237T^7-23513T^6+115362T^5-318739T^4+648093T^3-1045247T^2+1379659T-1511358$	3 / ✘ 1 / ✘
	10^n_{160} $-2T^5+12T^4-20T^3+14T^2-16T+12$	$-T^3+4T^2-4T+3$ $5T^{12}-52T^{11}+198T^{10}-255T^9-522T^8+3092T^7-8443T^6+18756T^5-37588T^4+67858T^3-108568T^2+148444T-165862$	3 / ✘ 2 / ✘		10^n_{161} $3T^5+6T^4-3T^3+4T^2+14T-12$	T^3-2T+3 $30T^{10}-53T^9-145T^8+630T^7-674T^6-870T^5+3591T^4-4450T^3+581T^2+6166T-9640$	3 / ✘ 3 / ✘
	10^n_{162} $10T^3-38T^2+58T-68$	$-3T^2+9T-11$ $222T^8-1473T^7+2609T^6+8829T^5-65543T^4+206079T^3-427536T^2+647498T-741358$	2 / ✘ 2 / ✘		10^n_{163} $-T^5+8T^4-30T^3+62T^2-89T+96$	$T^3-5T^2+12T-15$ $8T^{12}-125T^{11}+923T^{10}-4154T^9+12040T^8-19732T^7-4345T^6+140575T^5-506052T^4+1171653T^3-2040193T^2+2809224T-3119648$	3 / ✘ 1, 2 / ✘
	10^n_{164} $T^3-10T^2+29T-40$	$3T^2-11T+17$ $321T^8-3179T^7+12782T^6-20103T^5-32876T^4+254013T^3-688337T^2+1170838T-1386922$	2 / ✘ 1 / ✘		10^n_{165} $-5T^3+50T^2-146T+196$	$-2T^2+10T-15$ $38T^8-344T^7-848T^6+23020T^5-137555T^4+465256T^3-1047705T^2+1673914T-1951560$	2 / ✘ 2 / ✘