

Pensieve header: Mathematica notebook for Talks: Beijing-2407.

Ancestors: Projects/APAI/APAI.nb, Projects/APAI/PerturbedGaussianIntegration.nb.

```
In[*]:= SetDirectory["C:\\drorbn\\AcademicPensieve\\Talks\\Beijing-2407"];
```

## The Program

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```
In[*]:= Once[<< KnotTheory` ; << Rot.m];
```

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Loading KnotTheory` version of February 2, 2020, 10:53:45.2097.  
Read more at <http://katlas.org/wiki/KnotTheory>.

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Loading Rot.m from <http://drorbn.net/icbs24> to compute rotation numbers.

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```
In[*]:= CCF[ $\mathcal{E}$ ] := ExpandDenominator@ExpandNumerator@Together[ $\mathcal{E}$ ];
CF[ $\mathcal{E}$ _List] := CF /@  $\mathcal{E}$ ;
CF[ $\mathcal{E}$ ] := Module[{vs = Cases[ $\mathcal{E}$ , (x | p)_ ,  $\infty$ ]  $\cup$  {x, p}, ps, c},
  Total[CoefficientRules[Expand[ $\mathcal{E}$ ], vs] /. (ps_  $\rightarrow$  c_)  $\Rightarrow$  CCF[c] (Times @@ vsps) ]];
CF[eqp_EQP] := CF /@ eqp
```

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```
In[*]:= EQP /. c_ * EQP[Q_, P_] := EQP[Q, CF[c P]];
```

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```
In[*]:= {p*, x*} = { $\pi$ ,  $\xi$ }; (z_{i_})^* := (z^*)_i; vs_List^* := (v  $\mapsto$  v^*) /@ vs;
Zip_{ }[ $\mathcal{E}$ ] :=  $\mathcal{E}$ ;
Zip_{z_, zs_...}[ $\mathcal{E}$ ] := (Collect[ $\mathcal{E}$  // Zip_{zs}, z] /. f_. zd_  $\Rightarrow$  (D[f, {z*, d}])) /. z*  $\rightarrow$  0
```

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```
In[*]:= FI[EQP[Q_, P_]] := FI[EQP[Q, P], Union@Cases[Q, p_,  $\infty$ ], Union@Cases[Q, x_,  $\infty$ ]];
FI[EQP[Q_, P_], ps_List, xs_List] := Module[{u, v},
  A = Table[ $\partial_{u,v} Q$ , {u, ps}, {v, xs}];
  Factor[Det[A]-1 Zip_{ps $\cup$ xs}[P e-xs*.Inverse[A].ps*]]]
```

```
In[ ]:= Unprotect[Integrate];
        
$$\int p_{-} \cdot e^{L_{-}} \, d(vs\_List) :=$$

        "Let us integrate " <> ToString[{P, L}] <> " with respect to " <> ToString[vs];
        Protect[Integrate];
        
$$\int e^{p x} \, d\{p, x\}$$

        
$$\int \text{Sin}[x] e^{p x} \, d\{p, x\}$$

```

```
Out[ ]:= Let us integrate {1, p x} with respect to {p, x}
```

```
Out[ ]:= Let us integrate {Sin[x], p x} with respect to {p, x}
```