Four Hard Things

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1. The precise equality with Alekseev-Torrosian- in the Montpellier handout:

Alekseev-Torossian statement. There are elements $F \in \text{TAut}_2$ and $a \in \mathfrak{tr}_1$ such that $F(x+y) = \log e^x e^y$ and $jF = a(x) + a(y) - a(\log e^x e^y)$. Theorem. The Alekseev-Torossian statement is equivalent to the knot-theoretic statement. Proof. Write $V = e^c e^{uD}$ with $c \in \mathfrak{tr}_2$, $D \in \mathfrak{tder}_2$, and $\omega = e^b$ with $b \in \mathfrak{tr}_1$. Then $(1) \Leftrightarrow e^{uD}(x+y)e^{-uD} = \log e^x e^y$, $(2) \Leftrightarrow I = e^c e^{uD}(e^{uD})^* e^c = e^{2c} e^{jD}$, and $(3) \Leftrightarrow e^c e^{uD} e^{b(x+y)} = e^{b(x)+b(y)} \Leftrightarrow e^c e^{b(\log e^x e^y)} = e^{b(x)+b(y)}$ $\Leftrightarrow c = b(x) + b(y) - b(\log e^x e^y)$.

Note that A-T also have an additional equation, as in my MSRI handout:

$$RF^{2}(e(-t)) = F \iff \overrightarrow{f_1} = \overrightarrow{f_1}$$

2. Phi is in sder as in Montpellier:

and therefore it is a sum of (undirected!) chord trees. See http://katlas.math.toronto.edu/drorbn/bbs/show?shot=Moskovich-110223-173549.jpg and the following ones.

3. The Alekseev-Enriquez-Torrosian story: The "sled" of SwissKnots:



4. Do we do the 6-step derivation of the "equivalence" of the existence of Z and the convolutions statement? See Bonn:

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 $\dot{\Phi}(f) \star \dot{\Phi}(g) - \dot{\Phi}(f \star g).$