

Pensieve header: The $k=3$ building micro-blocks and gradings to cancel \hbar and γ .

Warning. To test degree rules, use versions of SL2Invariant.m from before July 5, 2018, and unset $\hbar = \gamma = 1$.

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In[ ]:= SetDirectory["C:\\drorbn\\AcademicPensieve\\Projects\\SL2Invariant"];
<< SL2Invariant.m
Block[{$k = 3}, quarks = {
  am → ami,j→k, bm → bmi,j→k, R → Ri,j, P → Pi,j, aS → aSi, CC → CCi, b2t → b2ti, t2b → t2bi
}] // Column

This is Profile.m of http://www.drorbn.net/AcademicPensieve/Projects/Profile/.
This version: June 2018. Original version: July 1994.

am → E[ak (αi + αj), xk (e-γ αj ξi + ξj), 1]
bm → E[bk (βi + βj), yk (ηi + ηj),
  1 - yk βi ηj ∈ +  $\frac{1}{2}$  (yk βi2 ηj + yk2 βi2 ηj2) ε2 +  $\frac{1}{6}$  (-yk βi3 ηj - 3 yk2 βi3 ηj2 - yk3 βi3 ηj3) ε3 + 0[ε]4]
R → E[ħ aj bi, ħ xj yi, 1 -  $\frac{1}{4}$  (γ ħ3 xj2 yi2) ε + ( $\frac{1}{9}$  γ2 ħ5 xj3 yi3 +  $\frac{1}{32}$  γ2 ħ6 xj4 yi4) ε2 +
   $\frac{1}{1152}$  (24 γ3 ħ5 xj5 yi2 - 72 γ3 ħ7 xj4 yi4 - 32 γ3 ħ8 xj5 yi5 - 3 γ3 ħ9 xj6 yi6) ε3 + 0[ε]4]
P → E[ $\frac{\alpha_j \beta_i}{\hbar}$ ,  $\frac{\eta_i \xi_j}{\hbar}$ , 1 +  $\frac{\gamma \eta_i^2 \xi_j^2 \epsilon}{4 \hbar}$  +  $\frac{(36 \gamma^2 \hbar^2 \eta_i^2 \xi_j^2 + 40 \gamma^2 \hbar \eta_i^3 \xi_j^3 + 9 \gamma^2 \eta_i^4 \xi_j^4) \epsilon^2}{288 \hbar^2}$  +  $\frac{1}{1152 \hbar^3}$ 
  (48 γ3 ħ4 ηi2 ξj2 + 192 γ3 ħ3 ηi3 ξj3 + 156 γ3 ħ2 ηi4 ξj4 + 40 γ3 ħ ηi5 ξj5 + 3 γ3 ηi6 ξj6) ε3 + 0[ε]4]
aS → E[-ai αi, -xi Ai ξi,
Out[ ]:= 1 +  $\frac{1}{2}$  (-2 ħ ai xi Ai ξi - γ ħ xi2 Ai2 ξi2) ε +  $\frac{1}{8}$  (-4 ħ2 ai2 xi Ai ξi + 2 γ2 ħ2 xi2 Ai2 ξi2 - 8 γ ħ2 ai xi2 Ai2 ξi2 +
  4 ħ2 ai2 xi2 Ai2 ξi2 - 4 γ2 ħ2 xi3 Ai3 ξi3 + 4 γ ħ2 ai xi3 Ai3 ξi3 + γ2 ħ2 xi4 Ai4 ξi4) ε2 +
   $\frac{1}{48}$  (-8 ħ3 ai3 xi Ai ξi - 4 γ3 ħ3 xi2 Ai2 ξi2 + 24 γ2 ħ3 ai xi2 Ai2 ξi2 - 48 γ ħ3 ai2 xi2 Ai2 ξi2 +
  24 ħ3 ai3 xi2 Ai2 ξi2 + 32 γ3 ħ3 xi3 Ai3 ξi3 - 84 γ2 ħ3 ai xi3 Ai3 ξi3 + 60 γ ħ3 ai2 xi3 Ai3 ξi3 -
  8 ħ3 ai3 xi3 Ai3 ξi3 - 38 γ3 ħ3 xi4 Ai4 ξi4 + 48 γ2 ħ3 ai xi4 Ai4 ξi4 - 12 γ ħ3 ai2 xi4 Ai4 ξi4 +
  12 γ3 ħ3 xi5 Ai5 ξi5 - 6 γ2 ħ3 ai xi5 Ai5 ξi5 - γ3 ħ3 xi6 Ai6 ξi6) ε3 + 0[ε]4]
CC → E[0, 0, √Bi -  $\frac{1}{2}$  (ħ ai √Bi) ε +  $\frac{1}{8}$  ħ2 ai2 √Bi ε2 -  $\frac{1}{48}$  (ħ3 ai3 √Bi) ε3 + 0[ε]4]
b2t → E[ai αi -  $\frac{t_i \beta_i}{\gamma}$ , yi ηi + xi ξi, 1 +  $\frac{a_i \beta_i \epsilon}{\gamma}$  +  $\frac{a_i^2 \beta_i^2 \epsilon^2}{2 \gamma^2}$  +  $\frac{a_i^3 \beta_i^3 \epsilon^3}{6 \gamma^3}$  + 0[ε]4]
t2b → E[aj αi - γ bj τi, yj ηi + xj ξi, 1 + aj τi ∈ +  $\frac{1}{2}$  aj2 τi2 ε2 +  $\frac{1}{6}$  aj3 τi3 ε3 + 0[ε]4]

In[ ]:= Print[degrule = Thread[{a, b, α, β, ξ, η, x, y, ħ, γ, ε, t, τ, T, B, A} →
  {1, 1, -1, -1, -1, -1, 1, 1, -2, 1, 1, 2, -2, 0, 0, 0}]];
quarks /. E[L_, Q_, P_] := (E[L, Q, P] ≡ (E[L, Q, Normal@P] /.
  {v-i → sv/.degrule vi, (v : ħ | ε | γ) → sv/.degrule v}))

{a → 1, b → 1, α → -1, β → -1, ξ → -1, η → -1, x → 1,
  y → 1, ħ → -2, γ → 1, ε → 1, t → 2, τ → -2, T → 0, B → 0, A → 0}

Out[ ]:= {am → True, bm → True, R → True, P → True, aS → True, CC → True, b2t → True, t2b → True}

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In[*]:= Print[degrule = Thread[{a, b,  $\alpha$ ,  $\beta$ ,  $\xi$ ,  $\eta$ , x, y,  $\hbar$ ,  $\gamma$ ,  $\epsilon$ , t,  $\tau$ , T, B,  $\mathcal{A}$ }  $\rightarrow$ 
  {0, 1, 0, -1, 0, -1, 0, 1, -1, 0, 1, 1, -1, 0, 0, 0}]];
quarks /.  $\mathbb{E}[L_, Q_, P_] \mapsto (\mathbb{E}[L, Q, P] \equiv (\mathbb{E}[L, Q, \text{Normal}@P] /.
  \{v_{-i} \mapsto s^{v/.degrule} v_i, (v : \hbar | \epsilon | \gamma) \mapsto s^{v/.degrule} v\}))$ 
{a  $\rightarrow$  0, b  $\rightarrow$  1,  $\alpha \rightarrow$  0,  $\beta \rightarrow$  -1,  $\xi \rightarrow$  0,  $\eta \rightarrow$  -1, x  $\rightarrow$  0,
  y  $\rightarrow$  1,  $\hbar \rightarrow$  -1,  $\gamma \rightarrow$  0,  $\epsilon \rightarrow$  1, t  $\rightarrow$  1,  $\tau \rightarrow$  -1, T  $\rightarrow$  0, B  $\rightarrow$  0,  $\mathcal{A} \rightarrow$  0}
Out[*]:= {am  $\rightarrow$  True, bm  $\rightarrow$  True, R  $\rightarrow$  True, P  $\rightarrow$  True, aS  $\rightarrow$  True, CC  $\rightarrow$  True, b2t  $\rightarrow$  True, t2b  $\rightarrow$  True}
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In[*]:= Print[degrule = Thread[{a, b,  $\alpha$ ,  $\beta$ ,  $\xi$ ,  $\eta$ , x, y,  $\hbar$ ,  $\gamma$ ,  $\epsilon$ , t,  $\tau$ , T, B,  $\mathcal{A}$ }  $\rightarrow$ 
  {1, 0, -1, 0, -1, 0, 1, 0, -1, 1, 0, 1, -1, 0, 0, 0}]];
quarks /.  $\mathbb{E}[L_, Q_, P_] \mapsto (\mathbb{E}[L, Q, P] \equiv (\mathbb{E}[L, Q, \text{Normal}@P] /.
  \{v_{-i} \mapsto s^{v/.degrule} v_i, (v : \hbar | \epsilon | \gamma) \mapsto s^{v/.degrule} v\}))$ 
{a  $\rightarrow$  1, b  $\rightarrow$  0,  $\alpha \rightarrow$  -1,  $\beta \rightarrow$  0,  $\xi \rightarrow$  -1,  $\eta \rightarrow$  0, x  $\rightarrow$  1,
  y  $\rightarrow$  0,  $\hbar \rightarrow$  -1,  $\gamma \rightarrow$  1,  $\epsilon \rightarrow$  0, t  $\rightarrow$  1,  $\tau \rightarrow$  -1, T  $\rightarrow$  0, B  $\rightarrow$  0,  $\mathcal{A} \rightarrow$  0}
Out[*]:= {am  $\rightarrow$  True, bm  $\rightarrow$  True, R  $\rightarrow$  True, P  $\rightarrow$  True, aS  $\rightarrow$  True, CC  $\rightarrow$  True, b2t  $\rightarrow$  True, t2b  $\rightarrow$  True}
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