

Pensieve header: Finding the most general R in UU notation.

```
SetDirectory@"C:\\drorbn\\AcademicPensieve\\Projects\\OneCo-1604";
<< Global.m;
Simp = Expand;
ExportButton
```

In the  $U(T) \otimes U(H)$  conventions. Internal use symbols: {rr, pp}

Export

## Finding R

```
Total[MapIndexed[ (#1 /. ff_ :> ff_#2[[1]] ) & ,
  DeleteCases[UUBasis[{j, k}, ff], UU[_β] | UU[_a] | UU[_δβ]] ] ]
UU[δa[ff1[bj, bk], ϕ, j] + δa[ff2[bj, bk], ϕ, k] + δa[ff3[bj, bk], j, j] +
  δa[ff4[bj, bk], j, k] + δa[ff5[bj, bk], k, j] + δa[ff6[bj, bk], k, k] +
  δaa[ff7[bj, bk], ϕ, j, j, j] + δaa[ff8[bj, bk], ϕ, j, j, k] + δaa[ff9[bj, bk], ϕ, k, j, j] +
  δaa[ff10[bj, bk], ϕ, k, j, k] + δaa[ff11[bj, bk], ϕ, j, k, j] +
  δaa[ff12[bj, bk], ϕ, j, k, k] + δaa[ff13[bj, bk], ϕ, k, k, j] +
  δaa[ff14[bj, bk], ϕ, k, k, k] + δaa[ff15[bj, bk], j, j, j, j] +
  δaa[ff16[bj, bk], j, j, j, k] + δaa[ff17[bj, bk], j, k, j, k] +
  δaa[ff18[bj, bk], j, j, k, j] + δaa[ff19[bj, bk], j, j, k, k] +
  δaa[ff20[bj, bk], j, k, k, k] + δaa[ff21[bj, bk], k, j, k, j] +
  δaa[ff22[bj, bk], k, j, k, k] + δaa[ff23[bj, bk], k, k, k, k] ]

ρ0[j_, k_] := UU[δa[ff1[bj, bk], ϕ, j] +
  δa[ff2[bj, bk], ϕ, k] + δa[ff3[bj, bk], j, j] + δa[ff4[bj, bk], j, k] +
  δa[ff5[bj, bk], k, j] + δa[ff6[bj, bk], k, k] + δaa[ff7[bj, bk], ϕ, j, j, j] +
  δaa[ff8[bj, bk], ϕ, j, j, k] + δaa[ff9[bj, bk], ϕ, k, j, j] +
  δaa[ff10[bj, bk], ϕ, k, j, k] + δaa[ff11[bj, bk], ϕ, j, k, j] +
  δaa[ff12[bj, bk], ϕ, j, k, k] + δaa[ff13[bj, bk], ϕ, k, k, j] +
  δaa[ff14[bj, bk], ϕ, k, k, k] + δaa[ff15[bj, bk], j, j, j, j] +
  δaa[ff16[bj, bk], j, j, j, k] + δaa[ff17[bj, bk], j, k, j, k] +
  δaa[ff18[bj, bk], j, j, k, j] + δaa[ff19[bj, bk], j, j, k, k] +
  δaa[ff20[bj, bk], j, k, k, k] + δaa[ff21[bj, bk], k, j, k, j] +
  δaa[ff22[bj, bk], k, j, k, k] + δaa[ff23[bj, bk], k, k, k, k] ]

R[j_, k_] := R[j, k] = Ea[j, k] ** TSD[{
  j → UU[a[1, j, h∞]] + bb[j, k][ρ0[j, k], UU[a[1, j, h∞]]],
  k → UU[a[1, k, h∞]] + bb[j, k][ρ0[j, k], UU[a[1, k, h∞]]]
}];
```

```
lhs = R[1, 2] ** R[1, 3] ** R[2, 3];
rhs = R[2, 3] ** R[1, 3] ** R[1, 2];
```

```
Simp = Simplify
Simplify
```

The following were obtained by watching `Dynamic[lhs1 - rhs1]` and repeatedly simplifying it:

```
Coefficient[lhs1 - rhs1, δaa[ϕ, h∞, 2, 1]]
```

$$-\frac{2(-1 + e^{2b_2}) b_1 b_3^2 \text{ff}_{21}[b_1, b_3]}{b_2}$$

```
ff21[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δa[3, h∞]]
```

$$-(-1 + e^{b_2}) b_1 \text{ff}_5[b_1, b_3]$$

```
ff5[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δaa[1, 2, 3, h∞]]
```

$$-2 e^{-b_1} (-1 + e^{b_1}) \text{ff}_{11}[b_1, b_3]$$

```
ff11[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δaa[3, 3, 3, h∞]]
```

$$-(-1 + e^{b_2}) b_1 \text{ff}_{22}[b_1, b_3]$$

```
ff22[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δaa[1, 1, 3, h∞]]
```

$$-(-1 + e^{b_2}) b_1 \text{ff}_{18}[b_1, b_3]$$

```
ff18[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δaa[2, 3, 3, h∞]] // Simplify
```

$$-\frac{(-1 + e^{b_2}) b_1 \text{ff}_{13}[b_1, b_3]}{b_2}$$

```
ff13[__] = 0;
```

```
Coefficient[lhs1 - rhs1, δaa[1, 3, 1, h∞]] // Simplify
```

$$e^{-b_2} (-1 + e^{b_2}) (\text{ff}_8[b_1, b_2] - \text{ff}_8[b_1, b_3])$$

```
ff8[x_, y_] := gg1[x];
```

The following were obtained by watching `Dynamic[lhs2 - rhs2]` and repeatedly simplifying it:

```
Coefficient[lhs2 - rhs2, δaa[1, 1, 1, h∞]] // Simplify
```

$$-\frac{(-1 + e^{b_1}) b_2 \text{ff}_7[b_1, b_3]}{b_1}$$

`ff7[_] = 0;`

`Coefficient[lhs2 - rhs2, δa[1, h∞]] // Simplify`

$$\frac{(-1 + e^{b_1}) b_2 (ff_1[b_1, b_3] - ff_1[b_2, b_3])}{b_1}$$

`ff1[x_, y_] := gg2[y];`

`Coefficient[lhs2 - rhs2, δaa[ϕ, 3, 3, h∞]] // Simplify`

$$(-1 + e^{b_1}) b_2 (ff_{12}[b_1, b_3] - ff_{12}[b_2, b_3])$$

`ff12[x_, y_] := gg3[y];`

`Coefficient[lhs2 - rhs2, δaa[2, 3, 2, h∞]] // Simplify`

$$\frac{2 e^{b_1 - b_2} (-1 + e^{b_2}) b_1 (ff_{10}[b_1, b_2] + b_1 ff_{17}[b_1, b_2])}{b_2}$$

`ff10[x_, y_] := -x ff17[x, y]`

`Coefficient[lhs2 - rhs2, δaa[ϕ, h∞, 1, 3]] // Simplify`

$$\frac{(-1 + e^{b_1}) b_2 (b_1 gg_1[b_1] - b_2 gg_1[b_2])}{b_1}$$

`gg1[x_] = cc1 / x;`

`t1 = Coefficient[lhs2 - rhs2, δaa[1, 3, 2, h∞]] // Simplify`

$$\frac{1}{b_1^2} e^{-b_2} (-1 + e^{b_2}) (2 - 2 e^{b_1} + b_1 (1 + e^{b_1} + (-1 + e^{b_1}) cc_1) + 2 e^{b_1} b_1^2 ff_{17}[b_1, b_2])$$

`Simplify[ff17[x, y] /. Solve[t1 == 0 /. {b1 -> x, b2 -> y}, ff17[x, y]]]`

$$\left\{ -\frac{e^{-x} (2 + e^x (-2 + x)) + x + (-1 + e^x) x cc_1}{2 x^3} \right\}$$

`ff17[x_, y_] := -\frac{e^{-x} (2 + e^x (-2 + x)) + x + (-1 + e^x) x cc_1}{2 x^3};`

The following were obtained by watching `Dynamic[lhs3 - rhs3]` and repeatedly simplifying it:

`Coefficient[lhs3 - rhs3, δaa[2, 2, 2, h∞]] // Simplify`

$$\frac{e^{b_1} (-1 + e^{b_2}) b_3 (ff_{14}[b_1, b_2] + b_1 ff_{20}[b_1, b_2])}{b_2}$$

`ff14[x_, y_] := -x ff20[x, y]`

`Coefficient[lhs3 - rhs3, δaa[1, 1, 1, h∞]] // Simplify`

$$e^{b_1} (-1 + e^{b_2}) b_3 (-ff_{16}[b_1, b_2] + ff_{16}[b_1, b_3])$$

`ff16[x_, y_] := gg4[x];`

**Coefficient[lhs3 - rhs3, δaa[1, 1, 2, h∞]] // Simplify**

$$\frac{e^{b_1} (-1 + e^{b_2}) b_3 (ff_9[b_1, b_2] - ff_9[b_1, b_3])}{b_2}$$

**ff9[x\_, y\_] := gg5[x];**

**Coefficient[lhs3 - rhs3, δaa[1, 3, 3, h∞]] // Simplify**

$$\frac{1}{b_1} b_3 (e^{b_1} (-1 + e^{b_2}) b_1 ff_{20}[b_1, b_3] - e^{b_2} (-1 + e^{b_1}) b_2 ff_{20}[b_2, b_3])$$

**ff20[x\_, y\_] :=  $\frac{gg_6[y] (e^x - 1)}{x e^x}$ ;**

**Coefficient[lhs3 - rhs3, δa[2, h∞]] // Simplify**

$$\frac{1}{b_2} e^{b_1} (-1 + e^{b_2}) b_3 (ff_2[b_1, b_2] - ff_2[b_1, b_3] + b_1 (ff_4[b_1, b_2] - ff_4[b_1, b_3]))$$

**(b1 ff4[b1, b2] + ff2[b1, b2] == b1 ff4[b1, b3] + ff2[b1, b3]) /. {b1 → x, b2 → y, b3 → z}**

$$ff_2[x, y] + x ff_4[x, y] == ff_2[x, z] + x ff_4[x, z]$$

**ff2[x\_, y\_] := gg7[x] - x ff4[x, y]**

**t2 = Coefficient[lhs3 - rhs3, δaa[1, 2, 2, h∞]] // Simplify**

$$\frac{1}{2 b_1 b_2^2} (-1 + e^{b_1}) b_3 (2 (-1 + e^{b_2}) + (1 + e^{b_2}) b_2 (-1 + cc_1) + 2 b_2^2 (gg_3[b_2] + e^{b_2} gg_5[b_2] - (-1 + e^{b_2}) gg_6[b_2]))$$

**Simplify[gg3[y] /. Solve[t2 == 0 /. {b1 → x, b2 → y}, gg3[y]]]**

$$\left\{ \frac{1}{2 y^2} (2 - 2 e^y + y + e^y y - (1 + e^y) y cc_1 - 2 e^y y^2 gg_5[y] - 2 y^2 gg_6[y] + 2 e^y y^2 gg_6[y]) \right\}$$

**gg3[y\_] :=  $\frac{1}{2 y^2}$**

$$(2 - 2 e^y + y + e^y y - (1 + e^y) y cc_1 - 2 e^y y^2 gg_5[y] - 2 y^2 gg_6[y] + 2 e^y y^2 gg_6[y]);$$

**t3 = Coefficient[lhs3 - rhs3, δa[1, h∞]]**

$$\frac{1}{2 b_1 b_2} b_3 (-2 (-1 + e^{b_1}) (-1 + e^{b_2}) - 2 (-1 + e^{b_1}) b_2^2 (e^{b_2} ff_4[b_2, b_3] + (-1 + e^{b_2}) gg_6[b_2]) + b_2 ((-1 + e^{b_1}) (-1 + e^{b_2}) cc_1 - 2 e^{b_1} (-1 + e^{b_2}) b_1 (ff_4[b_1, b_2] - ff_4[b_1, b_3]) + (-1 + e^{b_1}) (1 + e^{b_2} + 2 gg_2[b_2] + 2 e^{b_2} gg_7[b_2])))$$

**t4 =  $\left( 2 b_1 \frac{b_2}{b_3} t3 \right) /. \{b1 \rightarrow x, b2 \rightarrow y, b3 \rightarrow z\}$  // Simplify**

$$-2 (-1 + e^x) (-1 + e^y) - 2 (-1 + e^x) y^2 (e^y ff_4[y, z] + (-1 + e^y) gg_6[y]) + y ((-1 + e^x) (-1 + e^y) cc_1 - 2 e^x (-1 + e^y) x (ff_4[x, y] - ff_4[x, z]) + (-1 + e^x) (1 + e^y + 2 gg_2[y] + 2 e^y gg_7[y]))$$

**D[t4, z] / (2 y) // Simplify**

$$e^x (-1 + e^y) x \text{ff}_4^{(0,1)}[x, z] - e^y (-1 + e^x) y \text{ff}_4^{(0,1)}[y, z]$$

$$\text{ff}_4[x_, z_] := \text{gg}_8[x] + \frac{e^x - 1}{x e^x} \text{gg}_9[z];$$

**t5 = Coefficient[lhs3 - rhs3, da[1, hoo]] /. {b1 -> x, b2 -> y}**

$$-\frac{1}{2 x y} (-1 + e^x) b_3 (2 (-1 + e^y) + 2 y^2 ((-1 + e^y) \text{gg}_6[y] + e^y \text{gg}_8[y]) - y (1 + e^y + (-1 + e^y) c c_1 + 2 \text{gg}_2[y] + 2 e^y \text{gg}_7[y] + 2 \text{gg}_9[y] - 2 e^y \text{gg}_9[y]))$$

**Solve[t5 == 0, gg9[y]]**

$$\left\{ \left\{ \text{gg}_9[y] \rightarrow \frac{1}{2 (-1 + e^y) y} (2 - 2 e^y + y + e^y y - y c c_1 + e^y y c c_1 + 2 y \text{gg}_2[y] + 2 y^2 \text{gg}_6[y] - 2 e^y y^2 \text{gg}_6[y] + 2 e^y y \text{gg}_7[y] - 2 e^y y^2 \text{gg}_8[y]) \right\} \right\}$$

$$\text{gg}_9[y_] := \frac{1}{2 (-1 + e^y) y} (2 - 2 e^y + y + e^y y - y c c_1 + e^y y c c_1 + 2 y \text{gg}_2[y] + 2 y^2 \text{gg}_6[y] - 2 e^y y^2 \text{gg}_6[y] + 2 e^y y \text{gg}_7[y] - 2 e^y y^2 \text{gg}_8[y]);$$

**Table[lhs\_i - rhs\_i, {i, 3}]**

$$\{\text{UU}[0], \text{UU}[0], \text{UU}[0]\}$$

**UU@beta[f[b1, b2, b3]] // R[1, 2] // R[1, 3] // R[2, 3]**

$$\begin{aligned} & \text{UU}[\beta[f[b_1, b_2, b_3]]] + \delta a \left[ -\frac{1}{b_2} e^{-b_2} (-1 + e^{b_2}) (f^{(0,0,1)}[b_1, b_2, b_3] - f^{(0,1,0)}[b_1, b_2, b_3]), 2, 3 \right] + \\ & \delta a [e^{-b_1} (-1 + e^{b_1}) (f^{(0,1,0)}[b_1, b_2, b_3] - f^{(1,0,0)}[b_1, b_2, b_3]), \zeta, 2] + \\ & \delta a \left[ -\frac{1}{b_1} e^{-b_1} (-1 + e^{b_1}) (f^{(0,1,0)}[b_1, b_2, b_3] - f^{(1,0,0)}[b_1, b_2, b_3]), 1, 2 \right] + \\ & \delta a \left[ -\frac{1}{b_1} e^{-b_1 - b_2} (-1 + e^{b_1}) (f^{(0,0,1)}[b_1, b_2, b_3] + (-1 + e^{b_2}) f^{(0,1,0)}[b_1, b_2, b_3] - e^{b_2} f^{(1,0,0)}[b_1, b_2, b_3]), 1, 3 \right] + \\ & \delta a [e^{-b_1 - b_2} ((-1 + e^{b_1 + b_2}) f^{(0,0,1)}[b_1, b_2, b_3] - (-1 + e^{b_2}) f^{(0,1,0)}[b_1, b_2, b_3] - e^{b_2} (-1 + e^{b_1}) f^{(1,0,0)}[b_1, b_2, b_3]), \zeta, 3] \end{aligned}$$

**UU@beta[f[b1, b2, b3]] // R[2, 3] // R[1, 3] // R[1, 2]**

$$\begin{aligned} & \text{UU}[\beta[f[b_1, b_2, b_3]]] + \delta a \left[ -\frac{1}{b_2} e^{-b_2} (-1 + e^{b_2}) (f^{(0,0,1)}[b_1, b_2, b_3] - f^{(0,1,0)}[b_1, b_2, b_3]), 2, 3 \right] + \\ & \delta a [e^{-b_1} (-1 + e^{b_1}) (f^{(0,1,0)}[b_1, b_2, b_3] - f^{(1,0,0)}[b_1, b_2, b_3]), \zeta, 2] + \\ & \delta a \left[ -\frac{1}{b_1} e^{-b_1} (-1 + e^{b_1}) (f^{(0,1,0)}[b_1, b_2, b_3] - f^{(1,0,0)}[b_1, b_2, b_3]), 1, 2 \right] + \\ & \delta a \left[ -\frac{1}{b_1} e^{-b_1 - b_2} (-1 + e^{b_1}) (f^{(0,0,1)}[b_1, b_2, b_3] + (-1 + e^{b_2}) f^{(0,1,0)}[b_1, b_2, b_3] - e^{b_2} f^{(1,0,0)}[b_1, b_2, b_3]), 1, 3 \right] + \\ & \delta a [e^{-b_1 - b_2} ((-1 + e^{b_1 + b_2}) f^{(0,0,1)}[b_1, b_2, b_3] - (-1 + e^{b_2}) f^{(0,1,0)}[b_1, b_2, b_3] - e^{b_2} (-1 + e^{b_1}) f^{(1,0,0)}[b_1, b_2, b_3]), \zeta, 3] \end{aligned}$$

$(\text{UU}@\beta[\mathbf{f}[\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3]] // \mathbf{R}[1, 2] // \mathbf{R}[1, 3] // \mathbf{R}[2, 3]) -$   
 $(\text{UU}@\beta[\mathbf{f}[\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3]] // \mathbf{R}[2, 3] // \mathbf{R}[1, 3] // \mathbf{R}[1, 2])$   
 $\text{UU}[0]$

**Table**[( $\text{UU}@\mathbf{a}[\mathbf{f}[\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3], \mathbf{i}, \text{h}\infty] // \mathbf{R}[1, 2] // \mathbf{R}[1, 3] // \mathbf{R}[2, 3]$ ) -  
 $(\text{UU}@\mathbf{a}[\mathbf{f}[\mathbf{b}_1, \mathbf{b}_2, \mathbf{b}_3], \mathbf{i}, \text{h}\infty] // \mathbf{R}[2, 3] // \mathbf{R}[1, 3] // \mathbf{R}[1, 2])$ , { $\mathbf{i}, 3$ }]  
 $\{\text{UU}[0], \text{UU}[0], \text{UU}[0]\}$

**Table**[ $\text{CF}[\mathbf{A}\text{Form}[(\mathbf{R}[1, 2] ** \mathbf{R}[1, 3])_{\mathbf{i}} - (\mathbf{R}[1, 3] ** \mathbf{R}[1, 2])_{\mathbf{i}}]]$ , { $\mathbf{i}, 3$ }]

$\{\text{UU}[0], \text{UU}[\text{aao}[-\frac{(-1 + e^{b_1}) (-1 + cc_1)}{b_1}, 1, 3, 2, \text{h}\infty] + \text{aao}[\frac{1}{2 b_1 b_3^2}$   
 $(-1 + e^{b_1}) b_2 (2 (-1 + e^{b_3}) + (1 + e^{b_3}) b_3 (-1 + cc_1) + 2 b_3^2 (e^{b_3} \text{gg}_5[b_3] - (-1 + e^{b_3}) \text{gg}_6[b_3]))$ ,  
 $1, 3, 3, \text{h}\infty] + \text{ao}[-\frac{(-1 + e^{b_1}) b_2 \text{gg}_2[b_3]}{b_1}, 1, \text{h}\infty] +$   
 $\text{ca}[\frac{1}{2 b_1 b_3} (-1 + e^{b_1}) b_2 (2 (-1 + e^{b_3}) + (-1 + e^{b_3}) b_3 (-1 + cc_1) +$   
 $2 b_3^2 (e^{b_3} \text{gg}_5[b_3] - (-1 + e^{b_3}) \text{gg}_6[b_3]))$ , 3, 1,  $\text{h}\infty]$ ],  
 $\text{UU}[\text{aao}[\frac{(-1 + e^{b_1}) (-1 + cc_1)}{b_1}, 1, 2, 3, \text{h}\infty] + \text{aao}[-\frac{1}{2 b_1 b_2^2} (-1 + e^{b_1}) b_3$   
 $(2 (-1 + e^{b_2}) + (1 + e^{b_2}) b_2 (-1 + cc_1) + 2 b_2^2 (e^{b_2} \text{gg}_5[b_2] - (-1 + e^{b_2}) \text{gg}_6[b_2]))$ ,  
 $1, 2, 2, \text{h}\infty] + \text{ao}[\frac{(-1 + e^{b_1}) b_3 \text{gg}_2[b_2]}{b_1}, 1, \text{h}\infty] +$   
 $\text{ca}[-\frac{1}{2 b_1 b_2} (-1 + e^{b_1}) b_3 (2 (-1 + e^{b_2}) + (-1 + e^{b_2}) b_2 (-1 + cc_1) +$   
 $2 b_2^2 (e^{b_2} \text{gg}_5[b_2] - (-1 + e^{b_2}) \text{gg}_6[b_2]))$ , 2, 1,  $\text{h}\infty]$ ]]}

**Table**[ $\text{CF}[\mathbf{A}\text{Form}[(\mathbf{R}[1, 2] ** \mathbf{R}[1, 3])_{\mathbf{i}} - (\mathbf{R}[1, 3] ** \mathbf{R}[1, 2])_{\mathbf{i}}] /.$

$\{\text{gg}_{2|4|5|7}[_] \rightarrow 0, \text{gg}_6[\mathbf{x}_] \rightarrow \frac{2 - \mathbf{x}}{2 \mathbf{x}^2}, \text{gg}_8[\mathbf{x}_] \rightarrow 1/\mathbf{x}, \text{cc}_1 \rightarrow 0\}]$ , { $\mathbf{i}, 3$ }]

$\{\text{UU}[0], \text{UU}[\text{aao}[\frac{-1 + e^{b_1}}{b_1}, 1, 3, 2, \text{h}\infty] + \text{aao}[-\frac{(-1 + e^{b_1}) b_2}{b_1 b_3}, 1, 3, 3, \text{h}\infty]]$ ,  
 $\text{UU}[\text{aao}[\frac{1 - e^{b_1}}{b_1}, 1, 2, 3, \text{h}\infty] + \text{aao}[\frac{(-1 + e^{b_1}) b_3}{b_1 b_2}, 1, 2, 2, \text{h}\infty]]\}$

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$\rho_0[1, 2]$ 

$$\begin{aligned}
& UU[\delta a[\text{ff}_3[b_1, b_2], 1, 1] + \delta a[\text{ff}_6[b_1, b_2], 2, 2] + \\
& \delta a[\text{gg}_2[b_2], \zeta, 1] + \delta a[\text{gg}_8[b_1] + \frac{1}{2(-1 + e^{b_2}) b_1 b_2} \\
& e^{-b_1}(-1 + e^{b_1})(2 - 2e^{b_2} + b_2 + e^{b_2} b_2 - b_2 c c_1 + e^{b_2} b_2 c c_1 + 2 b_2 \text{gg}_2[b_2] + 2 b_2^2 \text{gg}_6[b_2] - \\
& 2 e^{b_2} b_2^2 \text{gg}_6[b_2] + 2 e^{b_2} b_2 \text{gg}_7[b_2] - 2 e^{b_2} b_2^2 \text{gg}_8[b_2]), 1, 2] + \delta a[\text{gg}_7[b_1] - \\
& b_1 \left( \text{gg}_8[b_1] + \frac{1}{2(-1 + e^{b_2}) b_1 b_2} e^{-b_1}(-1 + e^{b_1})(2 - 2e^{b_2} + b_2 + e^{b_2} b_2 - b_2 c c_1 + e^{b_2} b_2 c c_1 + \right. \\
& \left. 2 b_2 \text{gg}_2[b_2] + 2 b_2^2 \text{gg}_6[b_2] - 2 e^{b_2} b_2^2 \text{gg}_6[b_2] + 2 e^{b_2} b_2 \text{gg}_7[b_2] - 2 e^{b_2} b_2^2 \text{gg}_8[b_2] \right) \Big), \\
& \zeta, 2] + \delta aa\left[\frac{c c_1}{b_1}, \zeta, 1, 1, 2\right] + \delta aa\left[-\frac{e^{-b_1}(2 + e^{b_1}(-2 + b_1) + b_1 + (-1 + e^{b_1}) b_1 c c_1)}{2 b_1^3}, \right. \\
& \left. 1, 2, 1, 2\right] + \\
& \delta aa\left[\frac{e^{-b_1}(2 + e^{b_1}(-2 + b_1) + b_1 + (-1 + e^{b_1}) b_1 c c_1)}{2 b_1^2}, \zeta, 2, 1, 2\right] + \\
& \delta aa[\text{ff}_{15}[b_1, b_2], 1, 1, 1, 1] + \\
& \delta aa[\text{ff}_{19}[b_1, b_2], 1, 1, 2, 2] + \\
& \delta aa[\text{ff}_{23}[b_1, b_2], 2, 2, 2, 2] + \\
& \delta aa[\text{gg}_4[b_1], 1, 1, 1, 2] + \\
& \delta aa[\text{gg}_5[b_1], \zeta, 2, 1, 1] + \\
& \delta aa[-e^{-b_1}(-1 + e^{b_1}) \text{gg}_6[b_2], \zeta, 2, 2, 2] + \\
& \delta aa\left[\frac{e^{-b_1}(-1 + e^{b_1}) \text{gg}_6[b_2]}{b_1}, 1, 2, 2, 2\right] + \delta aa\left[\frac{1}{2 b_2^2} \right. \\
& \left. (2 - 2e^{b_2} + b_2 + e^{b_2} b_2 - (1 + e^{b_2}) b_2 c c_1 - 2 e^{b_2} b_2^2 \text{gg}_5[b_2] - 2 b_2^2 \text{gg}_6[b_2] + 2 e^{b_2} b_2^2 \text{gg}_6[b_2]), \right. \\
& \left. \zeta, 1, 2, 2\right]
\end{aligned}$$

**Table**[CF@R[1, 2]<sub>i</sub>, {i, 2}]

$$\begin{aligned}
& \{UU[a[1, 1, h\infty] + \delta a[gg_2[b_2], 1, h\infty] + \\
& \delta a[-b_1 gg_2[b_2], \zeta, h\infty] + \delta aa\left[\frac{1 - e^{-b_1} + b_1(-1 + cc_1)}{b_1^2}, 1, 2, 1, h\infty\right] + \delta aa\left[\frac{1}{2 b_2}\right. \\
& \left.(2(-1 + e^{b_2}) + (-1 + e^{b_2}) b_2(-1 + cc_1) + 2 b_2^2(e^{b_2} gg_5[b_2] - (-1 + e^{b_2}) gg_6[b_2])\right), \zeta, h\infty, 1, \\
& 2] + \delta aa\left[-\frac{1}{2 b_2^2}(-2 + 2 e^{b_2} + (1 + e^{b_2}) b_2(-1 + cc_1) + 2 b_2^2(e^{b_2} gg_5[b_2] - (-1 + e^{b_2}) gg_6[b_2]))\right), \\
& 1, 2, 2, h\infty] + \\
& \delta aa\left[\frac{1}{2 b_2^2} b_1(2(-1 + e^{b_2}) + (1 + e^{b_2}) b_2(-1 + cc_1) + 2 b_2^2(e^{b_2} gg_5[b_2] - (-1 + e^{b_2}) gg_6[b_2]))\right), \\
& \zeta, 2, 2, h\infty] + \delta aa\left[\frac{1}{2 b_1 b_2} e^{-b_1}(-2(-1 + e^{b_1}) b_2 - \right. \\
& \left. e^{b_1} b_1(2(-1 + e^{b_2}) + (1 + e^{b_2}) b_2(-1 + cc_1) + 2 b_2^2(e^{b_2} gg_5[b_2] - (-1 + e^{b_2}) gg_6[b_2]))\right), \\
& \zeta, 2, 1, h\infty], UU[a[e^{b_1}, 2, h\infty] + a\left[-\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty\right] + \\
& \delta a[e^{b_1} gg_7[b_1], 2, h\infty] + \delta a\left[\frac{1}{-1 + e^{b_2}}(-(-1 + e^{b_1})(-1 + e^{b_2}) + \right. \\
& \left. b_2(-e^{b_2} + e^{b_1+b_2} + e^{b_2}(-1 + e^{b_1}) gg_2[b_2] - e^{b_1}(-1 + e^{b_2}) gg_7[b_1] - e^{b_2} gg_7[b_2] + e^{b_1+b_2} \right. \\
& \left. gg_7[b_2] - e^{b_1} b_1 gg_8[b_1] + e^{b_1+b_2} b_1 gg_8[b_1]) - e^{b_2}(-1 + e^{b_1}) b_2^2 gg_8[b_2]\right), \zeta, h\infty] + \\
& \delta a\left[\frac{1}{(-1 + e^{b_2}) b_1}(((-1 + e^{b_1})(-1 + e^{b_2}) + b_2(e^{b_2} - e^{b_1+b_2} - e^{b_2}(-1 + e^{b_1}) gg_2[b_2] - \right. \\
& \left. e^{b_2}(-1 + e^{b_1}) gg_7[b_2] + e^{b_1} b_1 gg_8[b_1] - e^{b_1+b_2} b_1 gg_8[b_1]) + e^{b_2}(-1 + e^{b_1}) b_2^2 gg_8[b_2])\right), \\
& 1, h\infty] + \delta aa\left[\frac{e^{-b_1}(-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty\right] + \delta aa[e^{b_1} cc_1, \zeta, 1, 2, h\infty] + \\
& \delta aa\left[-\frac{e^{b_1} b_2 cc_1}{b_1}, \zeta, 1, 1, h\infty\right] + \delta aa[-e^{b_1} b_2 gg_4[b_1], 1, 1, 1, h\infty] + \\
& \delta aa[-e^{b_1} b_2 gg_5[b_1], \zeta, h\infty, 1, 1] + \\
& \delta aa[e^{b_1}(b_1 gg_4[b_1] + gg_5[b_1]), 1, 1, 2, h\infty] + \\
& \delta aa\left[-\frac{1}{2 b_1} e^{b_2}(-1 + e^{b_1})(2 + b_2(-1 + cc_1) + 2 b_2^2(gg_5[b_2] - gg_6[b_2]))\right), \zeta, h\infty, 1, 2] + \\
& \delta aa\left[-\frac{1}{2 b_2}(-1 + e^{b_1})(2(-1 + e^{b_2}) + e^{b_2} b_2(-1 + cc_1) + 2 e^{b_2} b_2^2(gg_5[b_2] - gg_6[b_2]))\right), \zeta, 2, 2, \\
& h\infty] + \delta aa\left[\frac{1}{2 b_1 b_2}(-1 + e^{b_1})(2(-1 + e^{b_2}) + e^{b_2} b_2(-1 + cc_1) + 2 e^{b_2} b_2^2(gg_5[b_2] - gg_6[b_2]))\right), \\
& 1, 2, 2, h\infty] + \delta aa\left[\frac{1}{2 b_1} e^{-b_1}(-1 + e^{b_1}) \right. \\
& \left. (2(1 - e^{b_1} + e^{b_1+b_2}) + e^{b_1+b_2} b_2(-1 + cc_1) + 2 e^{b_1+b_2} b_2^2(gg_5[b_2] - gg_6[b_2]))\right), \zeta, 2, 1, h\infty]\}
\end{aligned}$$



**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|6|7|8</sub>[\_] → 0}], {i, 2}]

$$\begin{aligned}
& \{UU[a[1, 1, h\infty] + \delta aa \left[ \frac{-1 + e^{-b_1}}{b_1} - \frac{-2 + 2 e^{b_2} + (1 + e^{b_2}) b_2 (-1 + c c_1)}{2 b_2}, \zeta, 2, 1, h\infty \right] + \\
& \delta aa \left[ \frac{1 - e^{-b_1} + b_1 (-1 + c c_1)}{b_1^2}, 1, 2, 1, h\infty \right] + \delta aa \left[ \frac{(-1 + e^{b_2}) (2 + b_2 (-1 + c c_1))}{2 b_2}, \zeta, h\infty, 1, 2 \right] + \\
& \delta aa \left[ -\frac{-2 + 2 e^{b_2} + (1 + e^{b_2}) b_2 (-1 + c c_1)}{2 b_2^2}, 1, 2, 2, h\infty \right] + \\
& \delta aa \left[ \frac{b_1 (2 (-1 + e^{b_2}) + (1 + e^{b_2}) b_2 (-1 + c c_1))}{2 b_2^2}, \zeta, 2, 2, h\infty \right] \}, \\
& UU[a[e^{b_1}, 2, h\infty] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty \right] + \delta a \left[ \frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{-1 + e^{b_2}}, \zeta, h\infty \right] + \\
& \delta a \left[ -\frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{(-1 + e^{b_2}) b_1}, 1, h\infty \right] + \delta aa \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty \right] + \\
& \delta aa \left[ -\frac{e^{b_2} (-1 + e^{b_1}) (2 + b_2 (-1 + c c_1))}{2 b_1}, \zeta, h\infty, 1, 2 \right] + \\
& \delta aa \left[ -\frac{(-1 + e^{b_1}) (2 (-1 + e^{b_2}) + e^{b_2} b_2 (-1 + c c_1))}{2 b_2}, \zeta, 2, 2, h\infty \right] + \\
& \delta aa \left[ \frac{(-1 + e^{b_1}) (2 (-1 + e^{b_2}) + e^{b_2} b_2 (-1 + c c_1))}{2 b_1 b_2}, 1, 2, 2, h\infty \right] + \\
& \delta aa \left[ \frac{e^{-b_1} (-1 + e^{b_1}) (2 (1 - e^{b_1} + e^{b_1+b_2}) + e^{b_1+b_2} b_2 (-1 + c c_1))}{2 b_1}, \zeta, 2, 1, h\infty \right] + \\
& \delta aa [e^{b_1} c c_1, \zeta, 1, 2, h\infty] + \delta aa \left[ -\frac{e^{b_1} b_2 c c_1}{b_1}, \zeta, 1, 1, h\infty \right] \}
\end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg2|4|5|6|7|8[\_] → 0}], {i, 2}] // ÅForm

$$\begin{aligned}
& \{ \text{UU} [ a [ 1, 1, \text{h}\infty ] + \text{aa} \left[ \frac{1 - e^{-b_1} + b_1 (-1 + \text{cc}_1)}{b_1^2}, 1, 2, 1, \text{h}\infty \right] + \\
& \quad \text{aa} \left[ -\frac{-2 + 2 e^{b_2} + (1 + e^{b_2}) b_2 (-1 + \text{cc}_1)}{2 b_2^2}, 1, 2, 2, \text{h}\infty \right] + \\
& \quad \text{ca} \left[ \frac{1 - e^{-b_1}}{b_1}, \text{h}\infty, 1, 2 \right] + \text{ca} \left[ -\frac{(-1 + e^{b_2}) (2 + b_2 (-1 + \text{cc}_1))}{2 b_2}, 2, 1, \text{h}\infty \right] \}, \\
& \text{UU} [ a [ e^{b_1}, 2, \text{h}\infty ] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, \text{h}\infty \right] + \text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, \text{h}\infty \right] + \\
& \quad \text{aa} \left[ \frac{(-1 + e^{b_1}) (2 (-1 + e^{b_2}) + e^{b_2} b_2 (-1 + \text{cc}_1))}{2 b_1 b_2}, 1, 2, 2, \text{h}\infty \right] + \\
& \quad \text{ao} \left[ -\frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{(-1 + e^{b_2}) b_1}, 1, \text{h}\infty \right] + \text{ca} \left[ -\frac{1 - e^{-b_1}}{b_1}, \text{h}\infty, 1, 2 \right] + \\
& \quad \text{ca} \left[ \frac{e^{b_2} (-1 + e^{b_1}) (2 + b_2 (-1 + \text{cc}_1))}{2 b_1}, 2, 1, \text{h}\infty \right] + \\
& \quad \text{ca} [ e^{b_1} \text{cc}_1, 1, 2, \text{h}\infty ] + \text{ca} \left[ -\frac{e^{b_1} b_2 \text{cc}_1}{b_1}, 1, 1, \text{h}\infty \right] \}
\end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg2|4|5|6|7|8[\_] → 0, cc1 → 1}], {i, 2}]

$$\begin{aligned}
& \{ \text{UU} [ a [ 1, 1, \text{h}\infty ] + \delta \text{aa} \left[ \frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, \text{h}\infty \right] + \delta \text{aa} \left[ \frac{-1 + e^{-b_1}}{b_1} + \frac{1 - e^{b_2}}{b_2}, \zeta, 2, 1, \text{h}\infty \right] + \\
& \quad \delta \text{aa} \left[ \frac{1 - e^{b_2}}{b_2^2}, 1, 2, 2, \text{h}\infty \right] + \delta \text{aa} \left[ \frac{(-1 + e^{b_2}) b_1}{b_2^2}, \zeta, 2, 2, \text{h}\infty \right] + \delta \text{aa} \left[ \frac{-1 + e^{b_2}}{b_2}, \zeta, \text{h}\infty, 1, 2 \right] \}, \\
& \text{UU} [ a [ e^{b_1}, 2, \text{h}\infty ] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, \text{h}\infty \right] + \delta a \left[ \frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{-1 + e^{b_2}}, \zeta, \text{h}\infty \right] + \\
& \quad \delta a \left[ -\frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{(-1 + e^{b_2}) b_1}, 1, \text{h}\infty \right] + \delta \text{aa} [ e^{b_1}, \zeta, 1, 2, \text{h}\infty ] + \\
& \quad \delta \text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, \text{h}\infty \right] + \delta \text{aa} \left[ -\frac{e^{b_2} (-1 + e^{b_1})}{b_1}, \zeta, \text{h}\infty, 1, 2 \right] + \\
& \quad \delta \text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1}) (1 - e^{b_1} + e^{b_1+b_2})}{b_1}, \zeta, 2, 1, \text{h}\infty \right] + \delta \text{aa} \left[ -\frac{(-1 + e^{b_1}) (-1 + e^{b_2})}{b_2}, \zeta, \right. \\
& \quad \left. 2, 2, \text{h}\infty \right] + \delta \text{aa} \left[ \frac{(-1 + e^{b_1}) (-1 + e^{b_2})}{b_1 b_2}, 1, 2, 2, \text{h}\infty \right] + \delta \text{aa} \left[ -\frac{e^{b_1} b_2}{b_1}, \zeta, 1, 1, \text{h}\infty \right] \}
\end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|6|7|8</sub>[\_] → 0, cc<sub>1</sub> → 1}], {i, 2}] // **ÅForm**

$$\begin{aligned} & \{UU[a[1, 1, h\infty] + aao[\frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, h\infty] + \\ & \quad aao[\frac{1 - e^{b_2}}{b_2^2}, 1, 2, 2, h\infty] + ca[\frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2] + ca[\frac{1 - e^{b_2}}{b_2}, 2, 1, h\infty]], \\ & UU[a[e^{b_1}, 2, h\infty] + a[-\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty] + aao[\frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty] + \\ & \quad aao[\frac{(-1 + e^{b_1}) (-1 + e^{b_2})}{b_1 b_2}, 1, 2, 2, h\infty] + ao[-\frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2)}{(-1 + e^{b_2}) b_1}, 1, h\infty] + \\ & \quad ca[e^{b_1}, 1, 2, h\infty] + ca[-\frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2] + \\ & \quad ca[\frac{e^{b_2} (-1 + e^{b_1})}{b_1}, 2, 1, h\infty] + ca[-\frac{e^{b_1} b_2}{b_1}, 1, 1, h\infty]]\} \end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|7</sub>[\_] → 0}], {i, 2}]

$$\begin{aligned}
& \{ \text{UU}[a[1, 1, h\infty] + \delta_{aa} \left[ \frac{1 - e^{-b_1} + b_1 (-1 + cc_1)}{b_1^2}, 1, 2, 1, h\infty \right] + \\
& \quad \delta_{aa} \left[ -\frac{(-1 + e^{b_2}) (-2 - b_2 (-1 + cc_1) + 2 b_2^2 gg_6[b_2])}{2 b_2}, \zeta, h\infty, 1, 2 \right] + \\
& \quad \delta_{aa} \left[ \frac{2 - 2 e^{b_2} - (1 + e^{b_2}) b_2 (-1 + cc_1) + 2 (-1 + e^{b_2}) b_2^2 gg_6[b_2]}{2 b_2^2}, 1, 2, 2, h\infty \right] + \\
& \quad \delta_{aa} \left[ -\frac{1}{2 b_2^2} b_1 (2 - 2 e^{b_2} - (1 + e^{b_2}) b_2 (-1 + cc_1) + 2 (-1 + e^{b_2}) b_2^2 gg_6[b_2]), \zeta, 2, 2, h\infty \right] + \\
& \quad \delta_{aa} \left[ \frac{1}{2 b_1 b_2} \right. \\
& \quad \left. e^{-b_1} (-2 (-1 + e^{b_1}) b_2 + e^{b_1} b_1 (2 - 2 e^{b_2} - (1 + e^{b_2}) b_2 (-1 + cc_1) + 2 (-1 + e^{b_2}) b_2^2 gg_6[b_2])) \right], \\
& \quad \zeta, 2, 1, h\infty \left. \right], \\
& \text{UU}[a[e^{b_1}, 2, h\infty] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty \right] + \delta_a \left[ \frac{1}{-1 + e^{b_2}} (-(-1 + e^{b_1}) (-1 + e^{b_2}) + \right. \\
& \quad \left. b_2 (e^{b_2} (-1 + e^{b_1}) + e^{b_1} (-1 + e^{b_2}) b_1 gg_8[b_1]) - e^{b_2} (-1 + e^{b_1}) b_2^2 gg_8[b_2]), \zeta, h\infty \right] + \\
& \quad \delta_a \left[ \frac{1}{(-1 + e^{b_2}) b_1} ((-1 + e^{b_1}) (-1 + e^{b_2}) + b_2 (-e^{b_2} (-1 + e^{b_1}) - e^{b_1} (-1 + e^{b_2}) b_1 gg_8[b_1]) + \right. \\
& \quad \left. e^{b_2} (-1 + e^{b_1}) b_2^2 gg_8[b_2]), 1, h\infty \right] + \delta_{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty \right] + \\
& \quad \delta_{aa} [e^{b_1} cc_1, \zeta, 1, 2, h\infty] + \delta_{aa} \left[ -\frac{e^{b_1} b_2 cc_1}{b_1}, \zeta, 1, 1, h\infty \right] + \\
& \quad \delta_{aa} \left[ \frac{e^{b_2} (-1 + e^{b_1}) (-2 - b_2 (-1 + cc_1) + 2 b_2^2 gg_6[b_2])}{2 b_1}, \zeta, h\infty, 1, 2 \right] + \\
& \quad \delta_{aa} \left[ \frac{1}{2 b_2} (-1 + e^{b_1}) (2 - 2 e^{b_2} - e^{b_2} b_2 (-1 + cc_1) + 2 e^{b_2} b_2^2 gg_6[b_2]), \zeta, 2, 2, h\infty \right] + \\
& \quad \delta_{aa} \left[ -\frac{1}{2 b_1 b_2} (-1 + e^{b_1}) (2 - 2 e^{b_2} - e^{b_2} b_2 (-1 + cc_1) + 2 e^{b_2} b_2^2 gg_6[b_2]), 1, 2, 2, h\infty \right] + \\
& \quad \delta_{aa} \left[ -\frac{1}{2 b_1} e^{-b_1} (-1 + e^{b_1}) (-2 (1 - e^{b_1} + e^{b_1+b_2}) - e^{b_1+b_2} b_2 (-1 + cc_1) + 2 e^{b_1+b_2} b_2^2 gg_6[b_2]), \right. \\
& \quad \left. \zeta, 2, 1, h\infty \right] \left. \right\}
\end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|7</sub>[\_] → 0, cc<sub>1</sub> → 1}], {i, 2}]

$$\begin{aligned}
& \{UU[a[1, 1, h\infty] + \delta aa \left[ \frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, h\infty \right] + \delta aa \left[ \frac{(-1 + e^{b_2}) (-1 + b_2^2 gg_6[b_2])}{b_2^2}, 1, 2, 2, h\infty \right] + \\
& \delta aa \left[ -\frac{(-1 + e^{b_2}) b_1 (-1 + b_2^2 gg_6[b_2])}{b_2^2}, \zeta, 2, 2, h\infty \right] + \\
& \delta aa \left[ -\frac{(-1 + e^{b_2}) (-1 + b_2^2 gg_6[b_2])}{b_2}, \zeta, h\infty, 1, 2 \right] + \\
& \delta aa \left[ \frac{e^{-b_1} (-(-1 + e^{b_1}) b_2 + e^{b_1} (-1 + e^{b_2}) b_1 (-1 + b_2^2 gg_6[b_2]))}{b_1 b_2}, \zeta, 2, 1, h\infty \right] \}, \\
& UU[a[e^{b_1}, 2, h\infty] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty \right] + \delta a \left[ \frac{1}{-1 + e^{b_2}} (-(-1 + e^{b_1}) (-1 + e^{b_2}) + \right. \\
& \left. b_2 (e^{b_2} (-1 + e^{b_1}) + e^{b_1} (-1 + e^{b_2}) b_1 gg_8[b_1]) - e^{b_2} (-1 + e^{b_1}) b_2^2 gg_8[b_2]), \zeta, h\infty \right] + \\
& \delta a \left[ \frac{1}{(-1 + e^{b_2}) b_1} ((-1 + e^{b_1}) (-1 + e^{b_2}) + b_2 (-e^{b_2} (-1 + e^{b_1}) - e^{b_1} (-1 + e^{b_2}) b_1 gg_8[b_1]) + \right. \\
& \left. e^{b_2} (-1 + e^{b_1}) b_2^2 gg_8[b_2]), 1, h\infty \right] + \delta aa[e^{b_1}, \zeta, 1, 2, h\infty] + \\
& \delta aa \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty \right] + \delta aa \left[ -\frac{e^{b_1} b_2}{b_1}, \zeta, 1, 1, h\infty \right] + \\
& \delta aa \left[ \frac{e^{b_2} (-1 + e^{b_1}) (-1 + b_2^2 gg_6[b_2])}{b_1}, \zeta, h\infty, 1, 2 \right] + \\
& \delta aa \left[ \frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2^2 gg_6[b_2])}{b_2}, \zeta, 2, 2, h\infty \right] + \\
& \delta aa \left[ -\frac{(-1 + e^{b_1}) (1 - e^{b_2} + e^{b_2} b_2^2 gg_6[b_2])}{b_1 b_2}, 1, 2, 2, h\infty \right] + \\
& \delta aa \left[ -\frac{e^{-b_1} (-1 + e^{b_1}) (-1 + e^{b_1} - e^{b_1+b_2} + e^{b_1+b_2} b_2^2 gg_6[b_2])}{b_1}, \zeta, 2, 1, h\infty \right] \}
\end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|7</sub>[\_] → 0, cc<sub>1</sub> → 1, gg<sub>6</sub>[x\_] :=  $\frac{1}{2 x^2}$ }], {i, 2}]

$$\begin{aligned} & \{ \text{UU} [a [1, 1, h\infty] + \delta\text{aa} \left[ \frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, h\infty \right] + \\ & \delta\text{aa} \left[ \frac{1}{2} \left( \frac{-2 + 2 e^{-b_1}}{b_1} + \frac{1 - e^{b_2}}{b_2} \right), \zeta, 2, 1, h\infty \right] + \delta\text{aa} \left[ -\frac{-1 + e^{b_2}}{2 b_2^2}, 1, 2, 2, h\infty \right] + \\ & \delta\text{aa} \left[ \frac{(-1 + e^{b_2}) b_1}{2 b_2^2}, \zeta, 2, 2, h\infty \right] + \delta\text{aa} \left[ \frac{-1 + e^{b_2}}{2 b_2}, \zeta, h\infty, 1, 2 \right] ], \\ & \text{UU} [a [e^{b_1}, 2, h\infty] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty \right] + \delta a \left[ \frac{1}{-1 + e^{b_2}} (-(-1 + e^{b_1}) (-1 + e^{b_2}) + \right. \\ & \left. b_2 (e^{b_2} (-1 + e^{b_1}) + e^{b_1} (-1 + e^{b_2}) b_1 \text{gg}_8[b_1]) - e^{b_2} (-1 + e^{b_1}) b_2^2 \text{gg}_8[b_2] \right), \zeta, h\infty] + \\ & \delta a \left[ \frac{1}{(-1 + e^{b_2}) b_1} ((-1 + e^{b_1}) (-1 + e^{b_2}) + b_2 (-e^{b_2} (-1 + e^{b_1}) - e^{b_1} (-1 + e^{b_2}) b_1 \text{gg}_8[b_1]) + \right. \\ & \left. e^{b_2} (-1 + e^{b_1}) b_2^2 \text{gg}_8[b_2]) \right), 1, h\infty] + \delta\text{aa} [e^{b_1}, \zeta, 1, 2, h\infty] + \\ & \delta\text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty \right] + \delta\text{aa} \left[ -\frac{e^{b_2} (-1 + e^{b_1})}{2 b_1}, \zeta, h\infty, 1, 2 \right] + \\ & \delta\text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1}) (2 - 2 e^{b_1} + e^{b_1+b_2})}{2 b_1}, \zeta, 2, 1, h\infty \right] + \\ & \delta\text{aa} \left[ -\frac{(-1 + e^{b_1}) (-2 + e^{b_2})}{2 b_2}, \zeta, 2, 2, h\infty \right] + \\ & \delta\text{aa} \left[ \frac{(-1 + e^{b_1}) (-2 + e^{b_2})}{2 b_1 b_2}, 1, 2, 2, h\infty \right] + \delta\text{aa} \left[ -\frac{e^{b_1} b_2}{b_1}, \zeta, 1, 1, h\infty \right] ] \} \end{aligned}$$

**Table**[CF[R[1, 2]<sub>i</sub> /. {gg<sub>2|4|5|7</sub>[\_] → 0, gg<sub>6</sub>[x\_] :=  $\frac{2-x}{2 x^2}$ , cc<sub>1</sub> → 0}], {i, 2}]

$$\begin{aligned} & \{ \text{UU} [a [1, 1, h\infty] + \delta\text{aa} \left[ 1 + \frac{-1 + e^{-b_1}}{b_1}, \zeta, 2, 1, h\infty \right] + \\ & \delta\text{aa} \left[ -\frac{-1 + e^{-b_1} + b_1}{b_1^2}, 1, 2, 1, h\infty \right] + \delta\text{aa} \left[ \frac{1}{b_2}, 1, 2, 2, h\infty \right] + \delta\text{aa} \left[ -\frac{b_1}{b_2}, \zeta, 2, 2, h\infty \right] ], \\ & \text{UU} [a [e^{b_1}, 2, h\infty] + a \left[ -\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty \right] + \\ & \delta a \left[ \frac{1}{-1 + e^{b_2}} (-(-1 + e^{b_1}) (-1 + e^{b_2}) + b_2 (e^{b_2} (-1 + e^{b_1}) + e^{b_1} (-1 + e^{b_2}) b_1 \text{gg}_8[b_1]) - \right. \\ & \left. e^{b_2} (-1 + e^{b_1}) b_2^2 \text{gg}_8[b_2]) \right), \zeta, h\infty] + \delta a \left[ \frac{1}{(-1 + e^{b_2}) b_1} ((-1 + e^{b_1}) (-1 + e^{b_2}) + \right. \\ & \left. b_2 (-e^{b_2} (-1 + e^{b_1}) - e^{b_1} (-1 + e^{b_2}) b_1 \text{gg}_8[b_1]) + e^{b_2} (-1 + e^{b_1}) b_2^2 \text{gg}_8[b_2]) \right), 1, h\infty] + \\ & \delta\text{aa} \left[ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty \right] + \delta\text{aa} \left[ -\frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1}, \zeta, 2, 1, h\infty \right] + \\ & \delta\text{aa} \left[ \frac{-1 + e^{b_1}}{b_2}, \zeta, 2, 2, h\infty \right] + \delta\text{aa} \left[ \frac{1 - e^{b_1}}{b_1 b_2}, 1, 2, 2, h\infty \right] ] \} \end{aligned}$$

BestR

**Table**[**CF**[**R**[1, 2]<sub>i</sub> /. {**gg**<sub>2|4|5|7</sub>[\_] → 0, **gg**<sub>6</sub>[**x**\_] ⇒  $\frac{2-x}{2x^2}$ , **gg**<sub>8</sub>[**x**\_] ⇒ 1/**x**, **cc**<sub>1</sub> → 0}],  
 {**i**, 2}] // **AForm**

BestR

$$\begin{aligned} & \{ \text{UU} [ a [ 1, 1, h\infty ] + \text{aao} [ - \frac{-1 + e^{-b_1} + b_1}{b_1^2}, 1, 2, 1, h\infty ] + \\ & \quad \text{aao} [ \frac{1}{b_2}, 1, 2, 2, h\infty ] + \text{ca} [ \frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2 ] ], \\ & \text{UU} [ a [ e^{b_1}, 2, h\infty ] + a [ - \frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty ] + \text{aao} [ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty ] + \\ & \quad \text{aao} [ \frac{1 - e^{b_1}}{b_1 b_2}, 1, 2, 2, h\infty ] + \text{ao} [ \frac{-1 + e^{b_1} - e^{b_1} b_2}{b_1}, 1, h\infty ] + \text{ca} [ - \frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2 ] ] \} \end{aligned}$$

**Table**[

$$\begin{aligned} & \text{CF} [ \text{R} [ 1, 2 ]_i /. \{ \text{gg}_{2|4|5|7} [ ] \rightarrow 0, \text{gg}_6 [ \mathbf{x}_- ] \Rightarrow \frac{1}{2x^2}, \text{gg}_8 [ \mathbf{x}_- ] \Rightarrow 1/x, \text{cc}_1 \rightarrow 1 \} ], \{ \mathbf{i}, 2 \} ] \\ & \{ \text{UU} [ a [ 1, 1, h\infty ] + \delta \text{aa} [ \frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, h\infty ] + \\ & \quad \delta \text{aa} [ \frac{1}{2} \left( \frac{-2 + 2 e^{-b_1}}{b_1} + \frac{1 - e^{b_2}}{b_2} \right), \zeta, 2, 1, h\infty ] + \delta \text{aa} [ - \frac{-1 + e^{b_2}}{2 b_2^2}, 1, 2, 2, h\infty ] + \\ & \quad \delta \text{aa} [ \frac{(-1 + e^{b_2}) b_1}{2 b_2^2}, \zeta, 2, 2, h\infty ] + \delta \text{aa} [ \frac{-1 + e^{b_2}}{2 b_2}, \zeta, h\infty, 1, 2 ] ], \\ & \text{UU} [ a [ e^{b_1}, 2, h\infty ] + a [ - \frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty ] + \delta a [ \frac{-1 + e^{b_1} - e^{b_1} b_2}{b_1}, 1, h\infty ] + \\ & \quad \delta a [ 1 - e^{b_1} + e^{b_1} b_2, \zeta, h\infty ] + \delta \text{aa} [ e^{b_1}, \zeta, 1, 2, h\infty ] + \delta \text{aa} [ \frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty ] + \\ & \quad \delta \text{aa} [ - \frac{e^{b_2} (-1 + e^{b_1})}{2 b_1}, \zeta, h\infty, 1, 2 ] + \delta \text{aa} [ \frac{e^{-b_1} (-1 + e^{b_1}) (2 - 2 e^{b_1} + e^{b_1+b_2})}{2 b_1}, \zeta, 2, 1, h\infty ] + \\ & \quad \delta \text{aa} [ - \frac{(-1 + e^{b_1}) (-2 + e^{b_2})}{2 b_2}, \zeta, 2, 2, h\infty ] + \\ & \quad \delta \text{aa} [ \frac{(-1 + e^{b_1}) (-2 + e^{b_2})}{2 b_1 b_2}, 1, 2, 2, h\infty ] + \delta \text{aa} [ - \frac{e^{b_1} b_2}{b_1}, \zeta, 1, 1, h\infty ] ] \} \end{aligned}$$

**Table**[**CF**[**R**[1, 2]<sub>i</sub> /. {**gg**<sub>2|4|5|7</sub>[\_] → 0, **gg**<sub>6</sub>[**x**\_] :=  $\frac{1}{2 x^2}$ , **gg**<sub>8</sub>[**x**\_] := 1/**x**, **cc**<sub>1</sub> → 1}],  
**{i, 2}] //  $\hat{A}$ Form**

$$\begin{aligned} & \{UU[a[1, 1, h\infty] + aao[\frac{1 - e^{-b_1}}{b_1^2}, 1, 2, 1, h\infty] + \\ & aao[-\frac{-1 + e^{b_2}}{2 b_2^2}, 1, 2, 2, h\infty] + ca[\frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2] + ca[-\frac{-1 + e^{b_2}}{2 b_2}, 2, 1, h\infty]], \\ & UU[a[e^{b_1}, 2, h\infty] + a[-\frac{(-1 + e^{b_1}) b_2}{b_1}, 1, h\infty] + aao[\frac{e^{-b_1} (-1 + e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty] + \\ & aao[\frac{(-1 + e^{b_1}) (-2 + e^{b_2})}{2 b_1 b_2}, 1, 2, 2, h\infty] + ao[\frac{-1 + e^{b_1} - e^{b_1} b_2}{b_1}, 1, h\infty] + ca[e^{b_1}, 1, 2, h\infty] + \\ & ca[-\frac{1 - e^{-b_1}}{b_1}, h\infty, 1, 2] + ca[\frac{e^{b_2} (-1 + e^{b_1})}{2 b_1}, 2, 1, h\infty] + ca[-\frac{e^{b_1} b_2}{b_1}, 1, 1, h\infty]] \} \end{aligned}$$

**Column@Table**[**x** → **CF**[ $\hat{A}$ Form[( $\delta$ aForm@UU@**x**) // **R**[1, 2] // **R**[2, 3] // **R**[2, 1]]] /.  
**{gg**<sub>2|4|5|7</sub>[\_] → 0, **gg**<sub>6</sub>[**x**\_] :=  $\frac{2 - x}{2 x^2}$ , **gg**<sub>8</sub>[**x**\_] := 1/**x**, **cc**<sub>1</sub> → 0}],

**{x, { $\beta$ [f[b<sub>1</sub>, b<sub>2</sub>]], a[1, 1, h $\infty$ ], a[1, 2, h $\infty$ ], ao[1, 1, h $\infty$ ],  
ao[1, 2, h $\infty$ ], ca[1, h $\infty$ , 1, 3], ca[1, h $\infty$ , 2, 3], ca[1, h $\infty$ , 0, 1],  
ca[1, h $\infty$ , 0, 2], aao[1, 1, 3, 1, h $\infty$ ], aao[1, 3, 4, 2, h $\infty$ ]]}**

$\beta$ [f[b<sub>1</sub>, b<sub>2</sub>]] →

$$\begin{aligned} & UU[ao[-\frac{e^{-b_1+b_2} (-1+e^{b_1}) (f^{(0,1)}[b_1, b_2] - f^{(1,0)}[b_1, b_2])}{b_1}, 1, 2] + ao[-\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2}) (f^{(0,1)}[b_1, b_2] - f^{(1,0)}[b_1, b_2])}{b_1}, \\ & 1, 1] + ao[-\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2}) (f^{(0,1)}[b_1, b_2] - f^{(1,0)}[b_1, b_2])}{b_1}, 1, 3] + \\ & ao[\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2}) (f^{(0,1)}[b_1, b_2] - f^{(1,0)}[b_1, b_2])}{b_2}, 2, 2] + \\ & ao[\frac{e^{-b_1-b_2} (-1+e^{b_2}) (1-e^{b_2}+e^{b_1+b_2}) (f^{(0,1)}[b_1, b_2] - f^{(1,0)}[b_1, b_2])}{b_2}, 2, 1] + \\ & ao[\frac{1}{b_2} e^{-b_1-b_2} (-1 + e^{b_2}) ((1 - e^{b_2} + e^{b_1+b_2}) f^{(0,1)}[b_1, b_2] - (-1 + e^{b_1}) (-1 + e^{b_2}) f^{(1,0)}[b_1, b_2]), \\ & 2, 3] + \beta[f[b_1, b_2]]] \\ & a[1, 1, h\infty] \rightarrow UU[a[e^{b_2}, 1, h\infty] + a[-\frac{(-1+e^{b_2}) b_1}{b_2}, 2, h\infty] + aao[\frac{e^2 b_2 (1-e^{-b_1}-b_1)}{b_1^2}, 1, 2, 1, h\infty] + \\ & aao[\frac{e^{-b_1+b_2} (-1+e^{b_2}) (-1+e^{b_1}-e^{b_1} b_1)}{b_1^2}, 1, 1, 1, h\infty] + aao[\frac{e^{-b_1+b_2} (-1+e^{b_2}) (-1+e^{b_1}-e^{b_1} b_1)}{b_1^2}, 1, 3, 1, h\infty] + \\ & aao[\frac{e^{-b_1-b_2} (-1+e^{b_2})^2 (1-e^{b_2}+e^{b_1+b_2}-e^{b_1+b_2} b_1)}{b_2^2}, 2, 1, 2, h\infty] + \\ & aao[\frac{e^{-b_1-b_2} (-1+e^{b_2})^2 ((-1+e^{b_1}) (-1+e^{b_2}) - e^{b_1+b_2} b_1)}{b_2^2}, 2, 3, 2, h\infty] + \\ & aao[-\frac{e^{-b_1} (-1+e^{b_2}) (-(-1+e^{b_1}) (-1+e^{b_2}) + e^{b_1+b_2} b_1)}{b_2^2}, 2, 2, 2, h\infty] + \\ & aao[\frac{e^{-b_1} (-1+e^{b_2}) (-2+e^{b_1}+2 e^{b_2}-2 e^{b_1+b_2}+e^{b_1} (-1+2 e^{b_2}) b_1)}{b_1 b_2}, 1, 1, 2, h\infty] + \\ & aao[\frac{e^{-b_1+b_2} (-2 (-1+e^{b_1}) (-1+e^{b_2}) + e^{b_1} (-1+2 e^{b_2}) b_1)}{b_1 b_2}, 1, 2, 2, h\infty] + \\ & aao[\frac{e^{-b_1} (-1+e^{b_2}) (-2 (-1+e^{b_1}) (-1+e^{b_2}) + e^{b_1} (-1+2 e^{b_2}) b_1)}{b_1 b_2}, 1, 3, 2, h\infty] + ao[\frac{-1+e^{b_2}-e^{b_2} b_1}{b_2}, 2, h\infty] + \\ & ca[\frac{e^{-b_1+b_2} (-1+e^{b_1})}{b_1}, h\infty, 1, 2] + ca[\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2})}{b_1}, h\infty, 1, 1] + \\ & ca[\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2})}{b_1}, h\infty, 1, 3] + ca[-\frac{e^{-b_1} (-1+e^{b_1}) (-1+e^{b_2})}{b_2}, h\infty, 2, 2] + \\ & ca[-\frac{e^{-b_1-b_2} (-1+e^{b_1}) (-1+e^{b_2})^2}{b_2}, h\infty, 2, 3] + ca[-\frac{e^{-b_1-b_2} (-1+e^{b_2}) (1-e^{b_2}+e^{b_1+b_2})}{b_2}, h\infty, 2, 1]] \end{aligned}$$



a[1, 2, h∞] →

$$\begin{aligned} & \text{UU}\left[a\left[1 - e^{b_2} + e^{b_1+b_2}, 2, h\infty\right] + a\left[-\frac{e^{b_2}(-1+e^{b_1})b_2}{b_1}, 1, h\infty\right] + \text{aao}\left[\frac{e^{-b_1+2b_2}(-1+e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty\right] + \right. \\ & \text{aao}\left[\frac{e^{-b_1+b_2}(-1+e^{b_1})^2(-1+e^{b_2})}{b_1^2}, 1, 1, 1, h\infty\right] + \text{aao}\left[\frac{e^{-b_1+b_2}(-1+e^{b_1})^2(-1+e^{b_2})}{b_1^2}, 1, 3, 1, h\infty\right] + \\ & \text{aao}\left[\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})}{b_1^2}, 2, 2, 2, h\infty\right] + \text{aao}\left[-\frac{2e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})}{b_1 b_2}, \right. \\ & \left. 1, 3, 2, h\infty\right] + \text{aao}\left[-\frac{e^{-b_1+b_2}(-1+e^{b_1})(2-e^{b_1}-2e^{b_2}+2e^{b_1+b_2})}{b_1 b_2}, 1, 2, 2, h\infty\right] + \\ & \text{aao}\left[\frac{e^{-b_1-b_2}((-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})^2-e^{2(b_1+b_2)}b_2)}{b_1^2}, 2, 1, 2, h\infty\right] + \\ & \text{aao}\left[\frac{e^{-b_1-b_2}((-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})^2-e^{2b_1+b_2}b_2)}{b_1^2}, 2, 3, 2, h\infty\right] + \\ & \text{aao}\left[\frac{e^{-b_1}(-2(-1+e^{b_1})(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})+e^{2b_1+b_2}b_2)}{b_1 b_2}, 1, 1, 2, h\infty\right] + \\ & \text{aao}\left[\frac{e^{b_1}}{b_3}, 2, 3, 3, h\infty\right] + \text{ao}\left[e^{b_2}(-1+e^{b_1}), 2, h\infty\right] + \text{ao}\left[\frac{e^{b_2}(-1+e^{b_1}-e^{b_1}b_2)}{b_1}, 1, h\infty\right] + \\ & \text{ca}\left[-\frac{e^{-b_1+b_2}(-1+e^{b_1})}{b_1}, h\infty, 1, 2\right] + \text{ca}\left[-\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})}{b_1}, h\infty, 1, 1\right] + \\ & \text{ca}\left[-\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})}{b_1}, h\infty, 1, 3\right] + \text{ca}\left[\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})}{b_2}, h\infty, 2, 2\right] + \\ & \text{ca}\left[\frac{e^{-b_1-b_2}(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})}{b_2}, h\infty, 2, 1\right] + \text{ca}\left[\frac{e^{-b_1-b_2}(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})}{b_2}, h\infty, 2, 3\right] \end{aligned}$$

$$\text{ao}[1, 1, h\infty] \rightarrow \text{UU}\left[\text{ao}\left[e^{b_2}, 1, h\infty\right] + \text{ao}\left[-\frac{(-1+e^{b_2})b_1}{b_2}, 2, h\infty\right]\right]$$

$$\text{ao}[1, 2, h\infty] \rightarrow \text{UU}\left[\text{ao}\left[1 - e^{b_2} + e^{b_1+b_2}, 2, h\infty\right] + \text{ao}\left[-\frac{e^{b_2}(-1+e^{b_1})b_2}{b_1}, 1, h\infty\right]\right]$$

$$\text{ca}[1, h\infty, 1, 3] \rightarrow \text{UU}\left[\text{ca}\left[1, h\infty, 1, 3\right]\right]$$

$$\text{ca}[1, h\infty, 2, 3] \rightarrow \text{UU}\left[\text{ca}\left[e^{b_1}, h\infty, 2, 3\right] + \text{ca}\left[-\frac{(-1+e^{b_1})b_2}{b_1}, h\infty, 1, 3\right]\right]$$

ca[1, h∞, 0, 1] →

$$\begin{aligned} & \text{UU}\left[\text{ca}\left[1 - e^{-b_1}, h\infty, 0, 2\right] + \text{ca}\left[1 - e^{-b_1} + e^{-b_1-b_2}, h\infty, 0, 1\right] + \text{ca}\left[\left(1 - e^{-b_1}\right)\left(1 - e^{-b_2}\right), h\infty, 0, 3\right] + \right. \\ & \text{ca}\left[-\frac{e^{b_2}(1-e^{-b_1})b_0}{b_1}, h\infty, 1, 2\right] + \text{ca}\left[-\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})b_0}{b_1}, h\infty, 1, 1\right] + \\ & \text{ca}\left[-\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})b_0}{b_1}, h\infty, 1, 3\right] + \text{ca}\left[\frac{(1-e^{-b_1})(-1+e^{b_2})b_0}{b_2}, h\infty, 2, 2\right] + \\ & \left. \text{ca}\left[\frac{e^{-b_1-b_2}(-1+e^{b_1})(-1+e^{b_2})^2b_0}{b_2}, h\infty, 2, 3\right] + \text{ca}\left[\frac{e^{-b_1-b_2}(-1+e^{b_1})(1-e^{b_2}+e^{b_1+b_2})b_0}{b_2}, h\infty, 2, 1\right]\right] \end{aligned}$$

ca[1, h∞, 0, 2] →

$$\begin{aligned} & \text{UU}\left[\text{ca}\left[e^{-b_1}, h\infty, 0, 2\right] + \text{ca}\left[e^{-b_1}\left(1 - e^{-b_2}\right), h\infty, 0, 1\right] + \text{ca}\left[e^{-b_1}\left(1 - e^{-b_2}\right), h\infty, 0, 3\right] + \right. \\ & \text{ca}\left[\frac{e^{b_2}(1-e^{-b_1})b_0}{b_1}, h\infty, 1, 2\right] + \text{ca}\left[\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})b_0}{b_1}, h\infty, 1, 1\right] + \\ & \text{ca}\left[\frac{e^{-b_1}(-1+e^{b_1})(-1+e^{b_2})b_0}{b_1}, h\infty, 1, 3\right] + \text{ca}\left[-\frac{(1-e^{-b_1})(-1+e^{b_2})b_0}{b_2}, h\infty, 2, 2\right] + \\ & \left. \text{ca}\left[-\frac{e^{-b_1-b_2}(-1+e^{b_1})(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})b_0}{b_2}, h\infty, 2, 1\right] + \text{ca}\left[-\frac{e^{-b_1-b_2}(-1+e^{b_1})(1-e^{b_2}+e^{b_1+b_2})b_0}{b_2}, h\infty, 2, 3\right]\right] \end{aligned}$$

$$\text{aao}[1, 1, 3, 1, h\infty] \rightarrow \text{UU}\left[\text{aao}\left[e^{b_2}, 1, 3, 1, h\infty\right] + \text{aao}\left[\frac{e^{-b_2}(-1+e^{b_2})^2b_1^2}{b_2^2}, 2, 3, 2, h\infty\right] + \right.$$

$$\left. \text{aao}\left[-\frac{2(-1+e^{b_2})b_1}{b_2}, 1, 3, 2, h\infty\right] + \text{ca}\left[-\frac{e^{-b_2}(-1+e^{b_2})b_1^2}{b_2}, h\infty, 2, 3\right]\right]$$

aao[1, 3, 4, 2, h∞] →

$$\begin{aligned} & \text{UU}\left[\text{aao}\left[e^{b_2}\left(1 - e^{b_2} + e^{b_1+b_2}\right), 2, 4, 3, h\infty\right] + \text{aao}\left[-\frac{e^{2b_2}(-1+e^{b_1})b_2}{b_1}, 1, 4, 3, h\infty\right] + \right. \\ & \left. \text{aao}\left[\frac{e^{b_2}(-1+e^{b_1})(-1+e^{b_2})b_3}{b_1}, 1, 4, 2, h\infty\right] + \text{aao}\left[-\frac{(-1+e^{b_2})(1-e^{b_2}+e^{b_1+b_2})b_3}{b_2}, 2, 4, 2, h\infty\right]\right] \end{aligned}$$

Column@Table[x → CF[ÅForm[(δaForm@UU@x) // R[1, 2]] /.

$$\left\{\text{gg}_2|4|5|7[_] \rightarrow 0, \text{gg}_6[\mathbf{x}_-] \Rightarrow \frac{2-\mathbf{x}}{2\mathbf{x}^2}, \text{gg}_8[\mathbf{x}_-] \Rightarrow 1/\mathbf{x}, \text{cc}_1 \rightarrow 0\right\},$$

{**x**, {β[f[b<sub>1</sub>, b<sub>2</sub>]], a[1, 1, h∞], a[1, 2, h∞], a[f[b<sub>1</sub>, b<sub>2</sub>], 1, h∞],  
a[f[b<sub>1</sub>, b<sub>2</sub>], 2, h∞], c[1, h∞], ao[1, 1, h∞], ao[1, 2, h∞], ca[1, 1, 1, h∞],  
ca[1, 2, 1, h∞], ca[1, h∞, 1, 1], ca[1, h∞, 1, 2], ca[1, 1, 2, h∞], ca[1, 2, 2, h∞],  
ca[1, h∞, 2, 1], ca[1, h∞, 2, 2], aao[1, 1, 1, 1, h∞], aao[1, 1, 2, 1, h∞],  
aao[1, 1, 1, 2, h∞], aao[1, 1, 2, 2, h∞], aao[1, 2, 1, 2, h∞], aao[1, 2, 2, 2, h∞]}}

$$\beta[f[b_1, b_2]] \rightarrow UU\left[ao\left[-\frac{e^{-b_1}(-1+e^{b_1})(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2])}{b_1}, 1, 2\right] + \beta[f[b_1, b_2]]\right]$$

$$a[1, 1, h\infty] \rightarrow$$

$$UU\left[a[1, 1, h\infty] + aao\left[-\frac{-1+e^{-b_1}+b_1}{b_1^2}, 1, 2, 1, h\infty\right] + aao\left[\frac{1}{b_2}, 1, 2, 2, h\infty\right] + ca\left[\frac{1-e^{-b_1}}{b_1}, h\infty, 1, 2\right]\right]$$

$$a[1, 2, h\infty] \rightarrow UU\left[a\left[e^{b_1}, 2, h\infty\right] + a\left[-\frac{(-1+e^{b_1})b_2}{b_1}, 1, h\infty\right] + aao\left[\frac{e^{-b_1}(-1+e^{b_1})^2}{b_1^2}, 1, 2, 1, h\infty\right] +\right.$$

$$aao\left[\frac{1-e^{-b_1}}{b_1 b_2}, 1, 2, 2, h\infty\right] + ao\left[\frac{-1+e^{b_1}-e^{b_1}b_2}{b_1}, 1, h\infty\right] + ca\left[-\frac{1-e^{-b_1}}{b_1}, h\infty, 1, 2\right]\left.] \right.$$

$$a[f[b_1, b_2], 1, h\infty] \rightarrow UU\left[a[f[b_1, b_2], 1, h\infty] + aao\left[\frac{f[b_1, b_2]}{b_2}, 1, 2, 2, h\infty\right] +\right.$$

$$aao\left[\frac{e^{-b_1}(f[b_1, b_2](-1+e^{b_1}-e^{b_1}b_1)-(-1+e^{b_1})b_1(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2]))}{b_1^2}, 1, 2, 1, h\infty\right] +$$

$$ca\left[\frac{e^{-b_1}(-1+e^{b_1})(f[b_1, b_2]+b_1(-f^{(0,1)}[b_1, b_2]+f^{(1,0)}[b_1, b_2]))}{b_1}, h\infty, 1, 2\right]\left.] \right.$$

$$a[f[b_1, b_2], 2, h\infty] \rightarrow UU\left[a\left[e^{b_1}f[b_1, b_2], 2, h\infty\right] + a\left[-\frac{(-1+e^{b_1})f[b_1, b_2]b_2}{b_1}, 1, h\infty\right] +\right.$$

$$aao\left[\frac{e^{-b_1}(-1+e^{b_1})^2(f[b_1, b_2]+b_2(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2]))}{b_1^2}, 1, 2, 1, h\infty\right] +$$

$$aao\left[-\frac{(-1+e^{b_1})(f[b_1, b_2]+b_2(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2]))}{b_1 b_2}, 1, 2, 2, h\infty\right] +$$

$$ao\left[\frac{f[b_1, b_2](-1+e^{b_1}-e^{b_1}b_2)+(-1+e^{b_1})b_2(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2])}{b_1}, 1, h\infty\right] +$$

$$ca\left[-\frac{e^{-b_1}(-1+e^{b_1})(f[b_1, b_2]+b_2(f^{(0,1)}[b_1, b_2]-f^{(1,0)}[b_1, b_2]))}{b_1}, h\infty, 1, 2\right]\left.] \right.$$

$$c[1, h\infty] \rightarrow UU[c[1, h\infty]]$$

$$ao[1, 1, h\infty] \rightarrow UU[ao[1, 1, h\infty]]$$

$$ao[1, 2, h\infty] \rightarrow UU\left[ao\left[e^{b_1}, 2, h\infty\right] + ao\left[-\frac{(-1+e^{b_1})b_2}{b_1}, 1, h\infty\right]\right]$$

$$ca[1, 1, 1, h\infty] \rightarrow UU\left[aao\left[-\frac{1-e^{-b_1}}{b_1}, 1, 2, 1, h\infty\right] + ca[1, 1, 1, h\infty] + ca[-1+e^{-b_1}, h\infty, 1, 2]\right]$$

$$ca[1, 2, 1, h\infty] \rightarrow UU\left[aao\left[\frac{1-e^{-b_1}}{b_1}, 1, 2, 1, h\infty\right] + ca[1, 2, 1, h\infty] + ca[1-e^{-b_1}, h\infty, 1, 2]\right]$$

$$ca[1, h\infty, 1, 1] \rightarrow UU[ca[1, h\infty, 1, 1]]$$

$$ca[1, h\infty, 1, 2] \rightarrow UU[ca[1, h\infty, 1, 2]]$$

$$ca[1, 1, 2, h\infty] \rightarrow UU\left[aao\left[\frac{1-e^{-b_1}}{b_1}, 1, 2, 2, h\infty\right] + aao\left[\frac{e^{-b_1}(-1+e^{b_1})^2 b_2}{b_1^2}, 1, 2, 1, h\infty\right] +\right.$$

$$ca\left[e^{b_1}, 1, 2, h\infty\right] + ca\left[-\frac{(1-e^{-b_1})b_2}{b_1}, h\infty, 1, 2\right] + ca\left[-\frac{(-1+e^{b_1})b_2}{b_1}, 1, 1, h\infty\right]\left.] \right.$$

$$ca[1, 2, 2, h\infty] \rightarrow UU\left[aao\left[\frac{-1+e^{b_1}}{b_1}, 1, 2, 2, h\infty\right] + aao\left[-\frac{e^{-b_1}(-1+e^{b_1})^2 b_2}{b_1^2}, 1, 2, 1, h\infty\right] +\right.$$

$$ca\left[e^{b_1}, 2, 2, h\infty\right] + ca\left[\frac{(1-e^{-b_1})b_2}{b_1}, h\infty, 1, 2\right] + ca\left[-\frac{(-1+e^{b_1})b_2}{b_1}, 2, 1, h\infty\right]\left.] \right.$$

$$ca[1, h\infty, 2, 1] \rightarrow UU\left[ca\left[e^{b_1}, h\infty, 2, 1\right] +\right.$$

$$ca[-1+e^{b_1}, h\infty, 2, 2] + ca\left[-\frac{(-1+e^{b_1})b_2}{b_1}, h\infty, 1, 1\right] + ca\left[-\frac{(-1+e^{b_1})b_2}{b_1}, h\infty, 1, 2\right]\left.] \right.$$

$$ca[1, h\infty, 2, 2] \rightarrow UU[ca[1, h\infty, 2, 2]]$$

$$aao[1, 1, 1, 1, h\infty] \rightarrow$$

$$UU\left[aao[1, 1, 1, 1, h\infty] + aao[1-e^{-b_1}, 1, 2, 1, h\infty] + ca\left[(1-e^{-b_1})b_1, h\infty, 1, 2\right]\right]$$

$$aao[1, 1, 2, 1, h\infty] \rightarrow UU\left[aao\left[e^{-b_1}, 1, 2, 1, h\infty\right] + ca\left[(-1+e^{-b_1})b_1, h\infty, 1, 2\right]\right]$$

$$aao[1, 1, 1, 2, h\infty] \rightarrow$$

$$UU\left[aao\left[e^{b_1}, 1, 1, 2, h\infty\right] + aao[-1+e^{b_1}, 1, 2, 2, h\infty] + aao\left[-\frac{(-1+e^{b_1})b_2}{b_1}, 1, 1, 1, h\infty\right] +\right.$$

$$aao\left[-\frac{e^{-b_1}(-1+e^{b_1})^2 b_2}{b_1}, 1, 2, 1, h\infty\right] + ca\left[(1-e^{-b_1})b_2, h\infty, 1, 2\right]\left.] \right.$$

$$aao[1, 1, 2, 2, h\infty] \rightarrow$$

$$UU\left[aao[1, 1, 2, 2, h\infty] + aao\left[-\frac{(1-e^{-b_1})b_2}{b_1}, 1, 2, 1, h\infty\right] + ca\left[-(1-e^{-b_1})b_2, h\infty, 1, 2\right]\right]$$

$$aao[1, 2, 1, 2, h\infty] \rightarrow UU\left[aao\left[e^{2b_1}, 2, 1, 2, h\infty\right] + aao\left[e^{b_1}(-1+e^{b_1}), 2, 2, 2, h\infty\right] +\right.$$

$$aao\left[-\frac{2e^{b_1}(-1+e^{b_1})b_2}{b_1}, 1, 1, 2, h\infty\right] + aao\left[-\frac{2(-1+e^{b_1})^2 b_2}{b_1}, 1, 2, 2, h\infty\right] +$$

$$aao\left[\frac{(-1+e^{b_1})^2 b_2^2}{b_1^2}, 1, 1, 1, h\infty\right] + aao\left[\frac{e^{-b_1}(-1+e^{b_1})^3 b_2^2}{b_1^2}, 1, 2, 1, h\infty\right] + ca\left[\frac{e^{-b_1}(-1+e^{b_1})b_2^2}{b_1}, h\infty, 1, 2\right]\left.] \right.$$

$$aao[1, 2, 2, 2, h\infty] \rightarrow UU\left[aao\left[e^{b_1}, 2, 2, 2, h\infty\right] + aao\left[-\frac{2(-1+e^{b_1})b_2}{b_1}, 1, 2, 2, h\infty\right] +\right.$$

$$aao\left[\frac{e^{-b_1}(-1+e^{b_1})^2 b_2^2}{b_1^2}, 1, 2, 1, h\infty\right] + ca\left[-\frac{e^{-b_1}(-1+e^{b_1})b_2^2}{b_1}, h\infty, 1, 2\right]\left.] \right.$$