

Pensieve header: A package to manage equivalence relations.

An Equivalence Relation Object (ERO) is a symbol `er` with two internal data fields:

* `er@complexity`: A function that for any index returns a sortable object (perhaps just a number).

Lower objects are better.

* `er@down`: A list of indices; the n th entry is the index of an element with lower complexity or lower index, or 0 if the element is terminal.

Manipulators:

`EROMake[er,n,comp]`: Initiates an n -element ERO `er`, with complexity function `comp` (defaults to `Identity`).

`EROPeek[er,n]`: Returns the best equivalent of element n , and improves `er` along the way.

`EROAdjoin[er,n1 \leftrightarrow n2]`: Decreases that $n1$ is equivalent to $n2$, update `er`.

```
(Alt) In[ ]:= EROMake[er_, n_Integer] := EROMake[er, n, Identity];
EROMake[er_, n_Integer, comp_] := (
  er@complexity = comp;
  (er@down = Unique[er]) = Table[0, n];
  er)
```

```
(Alt) In[ ]:= EROPeek[er_, n_Integer] :=
  If[(er@down)[[n]] == 0, n, (er@down)[[n]] = EROPeek[er, (er@down)[[n]]];
```

```
(Alt) In[ ]:= EROAdjoin[er_, n1_Integer  $\leftrightarrow$  n2_Integer] := Module[{m1, m2},
  m1 = EROPeek[er, n1]; m2 = EROPeek[er, n2];
  Switch[Order[{(er@complexity)[m1], m1}, {(er@complexity)[m2], m2}],
    0, m1,
    1, (er@down)[[m2]] = m1; EROPeek[er, m2],
    -1, (er@down)[[m1]] = m2; EROPeek[er, m1]
  ]]
```

```
(Alt) In[ ]:= Dynamic[EROMake[er0, 10]@down]
```

```
(Alt) Out[ ]:= 
```



```
(Alt) In[ ]:= er0@down
```

```
(Alt) Out[ ]:= er0[down]
```

(Alt) In[*]:= **EROPeek**[er0, 5]

(Alt) Out[*]= 5

(Alt) In[*]:= **EROAdjoin**[er0, 3 ↔ 7]

Set: er0[down] in the part assignment is not a symbol.



(Alt) Out[*]= 7