

```
In[ ]:= PD[GST48] = PD[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3],
  X[4, 44, 5, 43], X[5, 26, 6, 27], X[95, 7, 96, 6], X[7, 1, 8, 96], X[8, 14, 9, 13],
  X[28, 9, 29, 10], X[41, 11, 42, 10], X[11, 43, 12, 42], X[12, 27, 13, 28],
  X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18], X[83, 18, 84, 19],
  X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80],
  X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62],
  X[32, 74, 33, 73], X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36],
  X[70, 38, 71, 37], X[59, 39, 60, 38], X[54, 39, 55, 40], X[55, 45, 56, 44],
  X[45, 59, 46, 58], X[46, 70, 47, 69], X[47, 81, 48, 80], X[91, 49, 92, 48],
  X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52], X[60, 54, 61, 53],
  X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77], X[66, 87, 67, 88],
  X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]];
```

```
In[ ]:= GST48 // PD
```

```
Out[ ]:= PD[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3], X[4, 44, 5, 43], X[5, 26, 6, 27],
  X[95, 7, 96, 6], X[7, 1, 8, 96], X[8, 14, 9, 13], X[28, 9, 29, 10], X[41, 11, 42, 10],
  X[11, 43, 12, 42], X[12, 27, 13, 28], X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18],
  X[83, 18, 84, 19], X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80],
  X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62], X[32, 74, 33, 73],
  X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36], X[70, 38, 71, 37], X[59, 39, 60, 38],
  X[54, 39, 55, 40], X[55, 45, 56, 44], X[45, 59, 46, 58], X[46, 70, 47, 69],
  X[47, 81, 48, 80], X[91, 49, 92, 48], X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52],
  X[60, 54, 61, 53], X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77],
  X[66, 87, 67, 88], X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]]
```

```
In[ ]:= EPD[K_] := EPD@@PD[K] /. {x : X[i_, j_, k_, l_] => If[PositiveQ[x], X[i, j, k, l], X[i, j, k, l]]}
EPD[GST48]
```

```
Out[ ]:= EPD[X14,1, X2,29, X3,40, X43,4, X26,5, X6,95, X96,7, X13,8, X9,28, X10,41, X42,11, X27,12,
  X30,15, X16,61, X17,72, X18,83, X19,34, X89,20, X21,92, X79,22, X68,23, X57,24, X25,56, X62,31,
  X73,32, X84,33, X50,35, X36,81, X37,70, X38,59, X39,54, X44,55, X58,45, X69,46, X80,47, X48,91,
  X90,49, X51,82, X52,71, X53,60, X63,74, X64,85, X76,65, X87,66, X67,94, X75,86, X88,77, X78,93]
```

```
In[ ]:= PD@@EPD[GST48] /. {X[i_, j_] => X[j, i+1, j+1, i], X[i_, j_] => X[j, i, j+1, i+1]}
```

```
Out[ ]:= PD[X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3], X[4, 44, 5, 43], X[5, 26, 6, 27],
  X[95, 7, 96, 6], X[7, 97, 8, 96], X[8, 14, 9, 13], X[28, 9, 29, 10], X[41, 11, 42, 10],
  X[11, 43, 12, 42], X[12, 27, 13, 28], X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18],
  X[83, 18, 84, 19], X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80],
  X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62], X[32, 74, 33, 73],
  X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36], X[70, 38, 71, 37], X[59, 39, 60, 38],
  X[54, 39, 55, 40], X[55, 45, 56, 44], X[45, 59, 46, 58], X[46, 70, 47, 69],
  X[47, 81, 48, 80], X[91, 49, 92, 48], X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52],
  X[60, 54, 61, 53], X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77],
  X[66, 87, 67, 88], X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79]]
```

```
In[ ]:= PD [EPD [X14,1, X̄2,29, X3,40, X43,4, X̄26,5, X6,95, X96,7, X13,8, X̄9,28, X10,41, X42,11, X̄27,12,
X30,15, X̄16,61, X̄17,72, X̄18,83, X19,34, X̄89,20, X̄21,92, X̄79,22, X̄68,23, X̄57,24, X̄25,56, X62,31,
X73,32, X84,33, X̄50,35, X36,81, X37,70, X38,59, X̄39,54, X44,55, X58,45, X69,46, X80,47, X48,91,
X90,49, X51,82, X52,71, X53,60, X̄63,74, X̄64,85, X̄76,65, X̄87,66, X̄67,94, X̄75,86, X̄88,77, X̄78,93 ] ]
```

```
Out[ ]:= PD [X[1, 15, 2, 14], X[29, 2, 30, 3], X[40, 4, 41, 3], X[4, 44, 5, 43], X[5, 26, 6, 27],
X[95, 7, 96, 6], X[7, 97, 8, 96], X[8, 14, 9, 13], X[28, 9, 29, 10], X[41, 11, 42, 10],
X[11, 43, 12, 42], X[12, 27, 13, 28], X[15, 31, 16, 30], X[61, 16, 62, 17], X[72, 17, 73, 18],
X[83, 18, 84, 19], X[34, 20, 35, 19], X[20, 89, 21, 90], X[92, 21, 93, 22], X[22, 79, 23, 80],
X[23, 68, 24, 69], X[24, 57, 25, 58], X[56, 25, 57, 26], X[31, 63, 32, 62], X[32, 74, 33, 73],
X[33, 85, 34, 84], X[35, 50, 36, 51], X[81, 37, 82, 36], X[70, 38, 71, 37], X[59, 39, 60, 38],
X[54, 39, 55, 40], X[55, 45, 56, 44], X[45, 59, 46, 58], X[46, 70, 47, 69],
X[47, 81, 48, 80], X[91, 49, 92, 48], X[49, 91, 50, 90], X[82, 52, 83, 51], X[71, 53, 72, 52],
X[60, 54, 61, 53], X[74, 63, 75, 64], X[85, 64, 86, 65], X[65, 76, 66, 77],
X[66, 87, 67, 88], X[94, 67, 95, 68], X[86, 75, 87, 76], X[77, 88, 78, 89], X[93, 78, 94, 79] ]
```

```
In[ ]:= Ks = ReadList["C:\\drorbn\\AcademicPensieve\\People\\Dunfield\\nmd_random_knots"] /.
i_Integer -> i + 1;
```

```
In[ ]:= Crossings[Ks[[46]]]
```

```
Out[ ]:= 48
```

```
In[ ]:= Ks[[46]] // EPD
```

```
Out[ ]:= EPD [X72,11, X2,83, X33,20, X̄14,7, X30,27, X74,57, X21,34, X6,19, X60,29, X̄89,92, X87,50, X̄18,13,
X12,73, X5,94, X̄8,17, X55,48, X46,75, X̄91,52, X71,68, X69,66, X58,61, X49,54, X76,47, X̄81,40,
X95,4, X63,24, X28,59, X39,42, X̄65,62, X43,84, X67,70, X̄16,9, X̄77,56, X82,1, X23,64, X̄41,80,
X93,78, X̄51,90, X26,31, X35,32, X36,3, X45,86, X79,38, X̄37,96, X85,44, X̄10,15, X̄25,22, X53,88 ]
```