



$$R_{ij}^S = T^{S/2} (T^S - 1) (P_i - P_j) x_j$$

$$xP = Px - 1 \implies$$

$$G_{\alpha\beta} = \langle P_\alpha x_\beta \rangle \quad G_{\alpha, 2n+1} = 0$$

& with effort:

$$G_{1,\beta} = 0$$

$$\tilde{G}_{\alpha\beta} = \langle x_\alpha x_\beta \rangle = G_{\alpha\beta} - \delta_{\alpha\beta}$$

$X_{ij}^S$  make  $B \in M_{2n \times (2n+1)}$

$$\begin{cases} \text{row } i & \tilde{G}_{i,\beta} - G_{i+1,\beta} = 0 \iff G_{i\beta} - G_{i+1,\beta} = \delta_{i\beta} \\ \text{row } j & \tilde{G}_{j\beta} - G_{j+1,\beta} - (T^S - 1)(G_{i+1,\beta} - \tilde{G}_{i\beta}) = 0 \end{cases}$$

$$\iff T^S G_{j\beta} - G_{j+1,\beta} + (1 - T^S) G_{i+1,\beta} = T^S \delta_{j\beta}$$

$$B = (\phi | A) \quad G = \begin{pmatrix} 0 & 0 & 0 \\ D & 0 & 0 \end{pmatrix} \quad BG = \begin{pmatrix} I_{2n \times 2n} & 0 \end{pmatrix}$$

$$AD = I$$

$$[\mathcal{O}_{P\alpha}(e^{\lambda(P_i - P_j)x_j}), x_i] = \mathcal{O}_{P\alpha}(e^{\lambda(P_i - P_j)x_j} x_j)$$

$$[\mathcal{O}_{P\alpha}(e^{\lambda(P_i - P_j)x_j}), x_j] = \mathcal{O}_{P\alpha}(-\lambda e^{\lambda(P_i - P_j)x_j} x_j)$$

(agrees w/  $[P_i - P_j, x_i + x_j] = 0$ )

$$\implies -G_{\alpha,i} + \tilde{G}_{\alpha,i+1} = (T^S - 1) \tilde{G}_{\alpha,i+1} \quad \tilde{G} = G - I$$

$$-G_{\alpha,j} + \tilde{G}_{\alpha,j+1} = (1 - T^S) \tilde{G}_{\alpha,i+1} \implies -T^{-S} G_{\alpha,j} + G_{\alpha,j+1} = \delta_{\alpha,j+1}$$

$$-G_{\alpha,i} - G_{\alpha,j} + \tilde{G}_{\alpha,i+1} + \tilde{G}_{\alpha,j+1} = 0 \implies -G_{\alpha,i} - G_{\alpha,j} + G_{\alpha,i+1} + G_{\alpha,j+1} = \delta_{\alpha,i+1} + \delta_{\alpha,j+1}$$

$$GB = S \quad G = SB^{-1} = (BS^{-1})^{-1}$$







