

In[\*]:= **1 + 1**

Out[\*]:= 2

In[\*]:= **K = PD[Xp[3, 1, 4, 6], Xp[1, 5, 2, 4], Xp[5, 3, 6, 2]]**

Out[\*]:= PD[Xp[3, 1, 4, 6], Xp[1, 5, 2, 4], Xp[5, 3, 6, 2]]

In[\*]:= **K**

Out[\*]:= PD[Xp[3, 1, 4, 6], Xp[1, 5, 2, 4], Xp[5, 3, 6, 2]]

In[\*]:= **t1 = K /. {Xp[i\_, j\_, k\_, L\_] => Ap[i, j] p[k, L] + A^-1 p[i, L] p[j, k]}**

Out[\*]:= PD[ $\frac{p[1, 4] p[3, 6]}{A} + Ap[3, 1] p[4, 6],$   
 $Ap[1, 5] p[2, 4] + \frac{p[1, 4] p[5, 2]}{A}, \frac{p[3, 6] p[5, 2]}{A} + Ap[5, 3] p[6, 2]$ ]

In[\*]:= **Times @@ t1**

Out[\*]:=  $\left( \frac{p[1, 4] p[3, 6]}{A} + Ap[3, 1] p[4, 6] \right)$   
 $\left( Ap[1, 5] p[2, 4] + \frac{p[1, 4] p[5, 2]}{A} \right) \left( \frac{p[3, 6] p[5, 2]}{A} + Ap[5, 3] p[6, 2] \right)$

In[\*]:= **t2 = Expand[Times @@ t1]**

Out[\*]:=  $\frac{p[1, 4] p[1, 5] p[2, 4] p[3, 6]^2 p[5, 2]}{A} +$   
 $Ap[1, 5] p[2, 4] p[3, 1] p[3, 6] p[4, 6] p[5, 2] + \frac{p[1, 4]^2 p[3, 6]^2 p[5, 2]^2}{A^3} +$   
 $\frac{p[1, 4] p[3, 1] p[3, 6] p[4, 6] p[5, 2]^2}{A} + Ap[1, 4] p[1, 5] p[2, 4] p[3, 6] p[5, 3] p[6, 2] +$   
 $A^3 p[1, 5] p[2, 4] p[3, 1] p[4, 6] p[5, 3] p[6, 2] +$   
 $\frac{p[1, 4]^2 p[3, 6] p[5, 2] p[5, 3] p[6, 2]}{A} + Ap[1, 4] p[3, 1] p[4, 6] p[5, 2] p[5, 3] p[6, 2]$

In[\*]:= **t3 = t2 //. {p[i\_, j\_] p[j\_, k\_] => p[i, k]}**

Out[\*]:=  $Ap[1, 4]^2 + A^3 p[2, 2] p[3, 3] + Ap[3, 6]^2 + \frac{p[1, 4]^2 p[3, 6]^2}{A} +$   
 $Ap[5, 2]^2 + \frac{p[1, 4]^2 p[5, 2]^2}{A} + \frac{p[3, 6]^2 p[5, 2]^2}{A} + \frac{p[1, 4]^2 p[3, 6]^2 p[5, 2]^2}{A^3}$

In[\*]:= **t4 = t3 /. {p[i\_, i\_] -> (-A^2 - A^-2), p[i\_, j\_]^2 -> (-A^2 - A^-2)}**

Out[\*]:=  $3A \left( -\frac{1}{A^2} - A^2 \right) + \frac{3 \left( -\frac{1}{A^2} - A^2 \right)^2}{A} + A^3 \left( -\frac{1}{A^2} - A^2 \right)^2 + \frac{\left( -\frac{1}{A^2} - A^2 \right)^3}{A^3}$

In[\*]:= **Expand[t4]**

Out[\*]:=  $-\frac{1}{A^9} + \frac{1}{A} + A^3 + A^7$