



MakePrintable [img1]

$1 \times 0! = 1$   
 $1! = (1-1)! \cdot 1$   
 $2! = (2-1)! \cdot 2$   
 $3! = (3-1)! \cdot 3$   
 $n! = (n-1)! \cdot n$

In [ ]  
 Saw "L-shaped" → {out, ff, ...} things same  
 Saw "B-br" →

$n \rightarrow C$   
 {Tower [9, 8, 5], Tower [8, 6, 3], Tower [4, 2, 1]}  
 Tower [2, 8, 7, ...]  
 Tower [4, 9, 8, ...]  
 Tower [9, 8, ...]  
 Tower [9, 8, 7, ...]

$\{f, r, s, t, y\} \rightarrow \{r, u, s, t\} \cdot \{f, y\}$

img2 =

$e: \mathbb{R}^+ \rightarrow \mathbb{R}^+$   
 $x \mapsto e^x$   
 A miracle!!  
 $e(x) = \sum a_k x^k$   
 $e(x+y) = e(x) \cdot e(y)$   
 $x, y \geq 0$

$n^2$  eqns on  $n$  unknowns  
 $\Rightarrow$  No sol'ns.  
 Math riddle. Complete your understanding.  
 $|x| = \begin{cases} x & x > 0 \\ 0 & x = 0 \\ -x & x < 0 \end{cases}$   
 Which / Switch

$x \mid \begin{array}{l} \text{out} \\ a \mid 7 \\ 9 \mid 3 \end{array}$   
 $C \rightarrow C \xrightarrow{\perp} C \rightarrow \dots$   
 rank-nullity thm:  
 $\dim \text{Dom} = \text{rank} + \text{nullity}$

$FC_n =$  Free commutative unital algebra on  $x_1, \dots, x_n$   
 $= \langle 1, x_1, x_1 x_2, x_1^2, x_2^2, x_1 x_2^2 \rangle$   
 $=$  polynomial algebra in  $x_i$   
 $FC_0 \rightarrow FC_1 \rightarrow FC_2 \rightarrow \dots$

$FA_n =$  Free associative unital algebra on  $x_1, \dots, x_n$   
 $x_1, x_1 x_2 \neq x_2 x_1, x_1 + x_2$   
 $x_1 (7x_2 + x_3) = 7x_1 x_2 + x_1 x_3$   
 $FA_0 \rightarrow FA_1 \rightarrow FA_2 \rightarrow \dots$

MakePrintable [img2]

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 $=$  polynomial algebra in  $x_i$   
 $FC_0 \rightarrow FC_1 \rightarrow FC_2 \rightarrow \dots$

$FA_n =$  Free associative unital algebra on  $x_1, \dots, x_n$   
 $x_1, x_1 x_2 \neq x_2 x_1, x_1 + x_2 = x_2 + x_1$   
 $x_1 (7x_2 + x_3) = 7x_1 x_2 + x_1 x_3$   
 $FA_0 \rightarrow FA_1 \rightarrow FA_2 \rightarrow \dots$