

A Milk (chairman -> Chair, so milkman -> Milk) has three jugs of milk, one carrying 8 liters, one 5 liters, and one 3 liters. The 8 liter jug is full, the other two are empty. Can they measure 4 liters of milk?

This program takes any number of jugs with different sizes.

```
Moves::usage =
  "Moves[pstates_List, kstates_List, fixedstate_List, output_List:{}] .\n pstates
  >> This variable is for processing the states. It grows and eventually
  becomes empty. \n kstates >> This variable helps to avoid duplicates. \n
  fixedstate >> Holds the sizes of the jugs. \n output >> The final output";
```

? Moves

```
Moves[pstates_List, kstates_List, fixedstate_List, output_List:{}] .
pstates >> This variable is for
  processing the states. It grows and eventually becomes empty.
kstates >> This variable helps to avoid duplicates.
fixedstate >> Holds the sizes of the jugs.
output >> The final output
```

```
Moves[{}, kstates_List, fixedstate_List, output_List] := Return[output];
Moves[pstates_List, kstates_List, fixedstate_List, output_List:{}] :=
Module[{n, i, j, pst, fst, kst, tmp, diff, ou, gph = {}},
  pst = pstates; kst = kstates; fst = fixedstate;
  If[Length[pst[[1]]] ≠ Length[fst],
    Print["Error"];
    Return[];
  ];
  n = Length[fst];
  For[i = 1, i ≤ n, i++,
    For[j = 1, j ≤ n, j++,
      If[i ≠ j,
        tmp = pst[[1]];
        If[pst[[1, i]] > 0,
          If[pst[[1, i]] > fst[[j]] - pst[[1, j]],
            tmp[[i]] = pst[[1, i]] + pst[[1, j]] - fst[[j]];
            tmp[[j]] = fst[[j]];
            If[MemberQ[kst, tmp] === False,
              AppendTo[kst, tmp]; AppendTo[pst, tmp]; AppendTo[gph, pst[[1] → tmp];
            ], (* Else*)
            tmp[[i]] = 0;
            tmp[[j]] = pst[[1, i]] + pst[[1, j]];
            If[MemberQ[kst, tmp] === False,
              AppendTo[kst, tmp]; AppendTo[pst, tmp];
              AppendTo[gph, pst[[1] → tmp]
            ];
          ];
        ];
      ];
    ];
  ];
```

```

];
];

(*Back tracking*)
If[pst[[1, i]] < fst[[i]],
diff = fst[[i]] - pst[[1, i]];
If[pst[[1, j]] ≤ diff,
tmp[[i]] = pst[[1, i]] + pst[[1, j]];
tmp[[j]] = 0;
If[pst[[1]] ≠ tmp,
AppendTo[gph, pst[[1]] → tmp];
]
];
If[pst[[1, j]] ≥ diff,
tmp[[j]] = pst[[1, j]] - diff;
tmp[[i]] = pst[[1, i]] + diff;
If[pst[[1]] ≠ tmp,
AppendTo[gph, pst[[1]] → tmp];
]
]
];
] (* End of second For loop*)
]; (* End of first For loop*)
ou = Union[output, gph];
Moves[Delete[pst, 1], kst, fst, ou]
]

sts1 = Moves[{{8, 0, 0}}, {{8, 0, 0}}, {8, 5, 3}];
g1 = Graph[sts1, VertexLabels → "Name", ImageSize → 450];
m1 = HighlightGraph[g1, PathGraph[FindShortestPath[sts1, {8, 0, 0}, {4, 4, 0}],
DirectedEdges → True], GraphHighlightStyle → "Thick"];

(*More jugs*)
sts2 = Moves[{{8, 0, 0, 0}}, {{8, 0, 0, 0}}, {8, 5, 3, 2}];
g2 = Graph[sts2, VertexLabels → "Name", ImageSize → 450];
m2 = HighlightGraph[g2, PathGraph[FindShortestPath[sts2, {8, 0, 0, 0}, {4, 4, 0, 0}],
DirectedEdges → True], GraphHighlightStyle → "Thick"];

```

{m1, m2}

