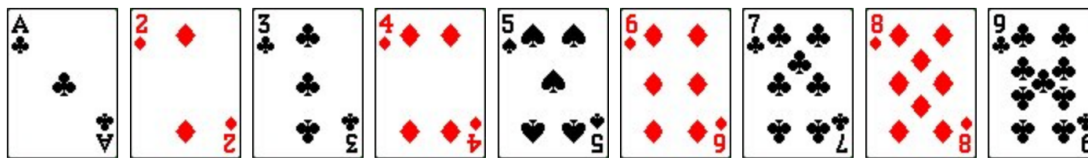


Pensieve header: Plotting a saddle and a torus for January 27.

## 1617-257 Fri Jan 27, hour 46: Manifolds and boundaries, integration on manifolds.

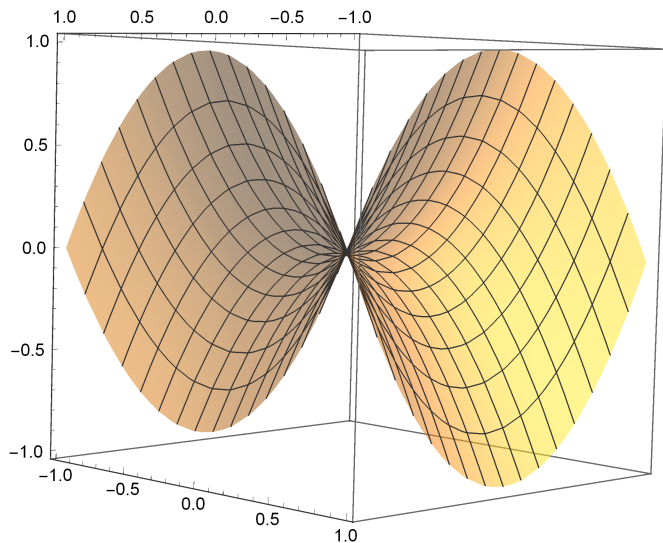
**Read Along.** Sections 24-25.

**Riddle Along.** The game of 15 is played as follows. Two players alternate choosing cards numbered between 1 and 9, with repetitions forbidden, so the game ends at most after 9 moves (or  $4\frac{1}{2}$  rounds). The first player to have within their cards a set of precisely 3 cards that add up to 15 wins. Would you rather move first or second?



Anyone looks good (from some angle)

```
ParametricPlot3D[
  {x, y, x^2 - y^2},
  {x, -1, 1}, {y, -1, 1},
  PlotStyle -> Opacity[0.5],
  ViewPoint -> {5, 5, 0}, ViewVertical -> {0, 0, 1}
]
```



```
ParametricPlot3D[  
  {Cos[α] (2 + Cos[β]), Sin[α] (2 + Cos[β]), Sin[β]},  
  {α, 0, 2 π}, {β, 0, 2 π},  
  PlotStyle -> Opacity[0.5],  
  ViewPoint -> {5, 5, 0}, ViewVertical -> {0, 0, 1}  
]
```

