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Dror Bar-Natan: Classes: 2014-15: MAT 475 Problem Solving Seminar:
Quiz 1 "Search for a Pattern", January 8, 2015. You have 25 minutes to solve as much as you can of the following problem. Please write on both sides of the page.

## Good Luck!

Problem (Larson's book, problem 1.1.6, plus little). Beginning with 2 and 7, the sequence $2,7,1,4,7,4,2,8, \ldots$ is constructed by multiplying successive pairs of its members and adjoining the result as the next one or two members of the sequence, depending on whether the product is a one- or two-digit number.

1. Prove that the digit 6 appears an infinite number of times in the sequence.
2. Prove that the sequence is not periodic.
