

Dror Bar-Natan: Classes: 2014-15: Math 1100 Algebra I:

Running the JCF Programs

```
SetDirectory["C:\\drorbn\\AcademicPensieve\\Classes\\14-1100"];
<< JCF-Program.m
```

Matrix I - 3x3, 3 eigenvalues.

```
n = 3; AA =  $\begin{pmatrix} 3 & 0 & 0 \\ 4 & -2 & -6 \\ -2 & 0 & 1 \end{pmatrix}$ ;
PP = QQ = II = IdentityMatrix[n];
MM = x II - AA; NN = PP.MM.QQ;

SwapRows[1, 2]

SwapColumns[2, 3]

GCDTrick[{1, 2}, 1]
GCDTrick[1, {1, 2}]
GCDTrick[1, {1, 3}]
GCDTrick[{1, 3}, 1]
GCDTrick[2, {2, 3}]
GCDTrick[{2, 3}, 2]
GCDTrick[2, {2, 3}]

SplitToSum[1, 3, (-3 + x), (-2 + x + x2)]

Factor[-2 + x + x2]

SplitToSum[2, 3, (-1 + x), (2 + x)]

MatrixForm /@ {Coefficient[NN, x, 1], BB = -Coefficient[NN, x, 0]}

(CC = Sum[
  MatrixPower[BB, k].Coefficient[PP, x, k],
  {k, 0, n}
]) // MatrixForm

CC.AA.Inverse[CC] // MatrixForm
```

Matrix 2 - 3x3, one Jordan block.

$$n = 3; \mathbf{AA} = \begin{pmatrix} -\frac{5}{2} & -11 & \frac{9}{2} \\ -\frac{1}{2} & 1 & \frac{1}{2} \\ -\frac{19}{2} & -16 & \frac{21}{2} \end{pmatrix};$$

```
PP = QQ = II = IdentityMatrix[n];
```

```
MM = x II - AA; NN = PP.MM.QQ;
```

```
GCDTrick[1, {1, 2}]
```

```
GCDTrick[1, {1, 3}]
```

```
GCDTrick[{1, 2}, 1]
```

```
GCDTrick[{1, 3}, 1]
```

```
GCDTrick[2, {2, 3}]
```

```
GCDTrick[{2, 3}, 2]
```

```
JordanTrick[2, 3, x - 3, 3]
```

```
JordanTrick[1, 2, x - 3, 2]
```

```
MatrixForm /@ {Coefficient[NN, x, 1], BB = -Coefficient[NN, x, 0]}
```

```
(CC = Sum[
  MatrixPower[BB, k].Coefficient[PP, x, k],
  {k, 0, n}
]) // MatrixForm
```

```
CC.AA.Inverse[CC] // MatrixForm
```

Matrix 3 - 4x4, mixed Jordan form.

$$n = 4; \mathbf{AA} = \begin{pmatrix} 1 & -2 & 0 & -2 \\ \frac{1}{4} & \frac{5}{2} & 0 & \frac{3}{2} \\ \frac{5}{2} & 5 & 2 & 3 \\ \frac{1}{4} & \frac{1}{2} & 0 & \frac{3}{2} \end{pmatrix};$$

```
PP = QQ = II = IdentityMatrix[n];
```

```
MM = x II - AA; NN = PP.MM.QQ;
```

```
GCDTrick[{1, 2}, 1]
```

```
GCDTrick[1, {1, 2}]
```

```
GCDTrick[1, {1, 4}]
```

```
GCDTrick[{1, 3}, 1]
GCDTrick[{1, 4}, 1]
GCDTrick[2, {2, 3}]
GCDTrick[2, {2, 4}]
GCDTrick[{2, 3}, 2]
GCDTrick[{2, 4}, 2]
GCDTrick[3, {3, 4}]
SwapBoth[1, 3]
SplitToSum[2, 4, (-1 + x), (-2 + x)^2]
SwapBoth[1, 2]
JordanTrick[3, 4, x - 2, 2]
MatrixForm /@ {Coefficient[NN, x, 1], BB = -Coefficient[NN, x, 0]}
(CC = Sum[
  MatrixPower[BB, k].Coefficient[PP, x, k],
  {k, 0, n}
]) // MatrixForm
CC.AA.Inverse[CC] // MatrixForm
```