The Yoga

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The "forgetful" or "fiber" functor:

$$F(V) = \mathrm{Hom}(\mathbb{Q}G, V) = \mathrm{Hom}(U(\mathfrak{g}), V)$$

(more precisely, it is called "the fiber functor" when combined w/ the tensor structure)

A "tensor structure":

Functorial isomorphisms $J_{VW} : F(V) \otimes F(W) \to F(V \otimes W)$

s.t.

$$\begin{tikzcd}
F(U)\otimes F(V)\otimes F(W) \arrow[rr, "1\otimes J_{V,W}"] \arrow[d, "J_{U,V}\otimes 1"'] & & F(U)\otimes F(V\otimes W) \arrow[dd, "J_{U,V\otimes W}"] \\
F(U\otimes V)\otimes F(W) \arrow[dr, "J_{U\otimes V,W}"'] & & \\
& F((U\otimes V)\otimes W) \arrow[r, "F(\Phi)"'] & F(U\otimes(V\otimes W))
\end{tikzcd}$$

Endomorphisms of the Fiber functor:

$H = \mathrm{End}(F)$ is a Hopf algebra.

$H^{\otimes 2} = \mathrm{End}(F^{\otimes 2} : \mathcal{M} \times \mathcal{M} \to \mathrm{Vect})$

Question. Does this yoga have a counterpart in knot theory?