

Pensieve header: Tbar games - $\bar{T} = (T-1)/\hbar$.

Series $\left[\frac{1 - T^2 e^{-2\epsilon a \hbar}}{\hbar}, \{a, 0, 3\} \right]$

$$\frac{1 - T^2}{\hbar} + 2 T^2 \epsilon a - 2 (T^2 \epsilon^2 \hbar) a^2 + \frac{4}{3} T^2 \epsilon^3 \hbar^2 a^3 + O[a]^4$$

Simplify $\left[\frac{1 - T^2 e^{-2\epsilon a \hbar}}{\hbar} /. T \rightarrow 1 + \hbar \bar{T} \right]$

$$\frac{1 - e^{-2\epsilon a \hbar} (1 + \hbar \bar{T})^2}{\hbar}$$

Simplify $\left[\frac{1 - T^2}{\hbar} /. T \rightarrow 1 + \hbar \bar{T} \right]$

$$-\bar{T} (2 + \hbar \bar{T})$$

Simplify $\left[\text{Series} \left[\frac{1 - T^2 e^{-2\epsilon a \hbar}}{\hbar}, \{a, 0, 3\} \right] /. T \rightarrow 1 + \hbar \bar{T} \right]$

$$-\bar{T} (2 + \hbar \bar{T}) + 2 \epsilon (1 + \hbar \bar{T})^2 a - 2 (\hbar (\epsilon + \epsilon \hbar \bar{T})^2) a^2 + O[a]^4$$

Simplify $\left[\frac{T-1}{\hbar} /. T \rightarrow T^{-1} /. T \rightarrow 1 + \hbar \bar{T} \right]$

$$-\frac{\bar{T}}{1 + \hbar \bar{T}}$$