

Pensieve header: Simplifying the messy functions in the symmetric dequantizer.

**FS = FullSimplify;**

$$g = \sqrt{\left( \left( \text{Cosh}\left[\frac{\hbar}{2} \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}\right] - \text{Cosh}\left[\frac{\hbar}{2} (t - (2a + \gamma) \epsilon)\right] \right) / \left( \text{Sinh}\left[\frac{\gamma \epsilon \hbar}{2}\right] (t (2a + \gamma) - 2a (a + \gamma) \epsilon + 2 \varpi) \hbar / (2 \gamma) \right) \right) \sqrt{2} \sqrt{\left( \left( \gamma \left( -\text{Cosh}\left[\frac{1}{2} (t - (2a + \gamma) \epsilon) \hbar\right] + \text{Cosh}\left[\frac{1}{2} \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi} \hbar\right] \right) \text{Csch}\left[\frac{\gamma \epsilon \hbar}{2}\right] \right) / \left( (t (2a + \gamma) - 2a (a + \gamma) \epsilon + 2 \varpi) \hbar \right) \right)}$$

$$\text{FS}\left[\sqrt{a^2 + \epsilon b} = a + \frac{\epsilon b}{a + \sqrt{a^2 + \epsilon b}}\right]$$

$$\text{FS}\left[\sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi} = t + \frac{\epsilon (4 \varpi + \epsilon \gamma^2)}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}}\right]$$

True

$$\text{FS}\left[t + \frac{\epsilon (4 \varpi + \epsilon \gamma^2)}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}}\right]$$

$$\sqrt{t^2 + \epsilon (\gamma^2 \epsilon + 4 \varpi)}$$

$$\text{FS}[g = \sqrt{\left( \left( \left( \text{Cosh}\left[\frac{\hbar}{2} \left( t + \frac{\epsilon (4 \varpi + \epsilon \gamma^2)}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}} \right) \right] - \text{Cosh}\left[\frac{\hbar}{2} (t - (2a + \gamma) \epsilon)\right] \right) / \left( \text{Sinh}\left[\frac{\gamma \epsilon \hbar}{2}\right] (t (2a + \gamma) - 2a (a + \gamma) \epsilon + 2 \varpi) \hbar / (2 \gamma) \right) \right) \right]}$$

True

$$\text{FS}[\text{Cosh}[x] - \text{Cosh}[y] = 2 \text{Sinh}\left[\frac{x+y}{2}\right] \text{Sinh}\left[\frac{x-y}{2}\right]]$$

True

$$\text{With}\left[\left\{x = \frac{\hbar}{2} \left( t + \frac{\epsilon (4 \varpi + \epsilon \gamma^2)}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}} \right), y = \frac{\hbar}{2} (t - (2a + \gamma) \epsilon) \right\},\right]$$

$$\text{Simplify} / @ \left\{ \frac{x+y}{2}, \frac{x-y}{2} \right\}$$

$$\left\{ \frac{1}{4} \left( 2t - (2a + \gamma) \epsilon + \frac{\epsilon (\gamma^2 \epsilon + 4 \varpi)}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}} \right) \hbar, \frac{1}{4} \epsilon \left( 2a + \gamma + \frac{\gamma^2 \epsilon + 4 \varpi}{t + \sqrt{t^2 + \gamma^2 \epsilon^2 + 4 \epsilon \varpi}} \right) \hbar \right\}$$

$$\text{FS}[g = 2 \sqrt{\left( \left( \gamma \text{Sinh}\left[ \frac{1}{4} \left( 2t - (2a + \gamma)\epsilon + \frac{\epsilon(\gamma^2\epsilon + 4\omega)}{t + \sqrt{t^2 + \gamma^2\epsilon^2 + 4\epsilon\omega}} \right) \right] \hbar \right) \right)} \\
 \left. \text{Sinh}\left[ \frac{1}{4} \epsilon \left( 2a + \gamma + \frac{\gamma^2\epsilon + 4\omega}{t + \sqrt{t^2 + \gamma^2\epsilon^2 + 4\epsilon\omega}} \right) \right] \hbar \right] / \\
 \left( \text{Sinh}\left[ \frac{\gamma\epsilon\hbar}{2} \right] (t(2a + \gamma) - 2a(a + \gamma)\epsilon + 2\omega)\hbar \right) \right]$$

True

$$\text{FS}\left[ - (2a + \gamma)\epsilon + \frac{\epsilon(\gamma^2\epsilon + 4\omega)}{t + \sqrt{t^2 + \gamma^2\epsilon^2 + 4\epsilon\omega}} \right] \\
 - t - (2a + \gamma)\epsilon + \sqrt{t^2 + \epsilon(\gamma^2\epsilon + 4\omega)} \\
 \text{FS}\left[ 2a + \gamma + \frac{\gamma^2\epsilon + 4\omega}{t + \sqrt{t^2 + \gamma^2\epsilon^2 + 4\epsilon\omega}} \right] \\
 \frac{-t + 2a\epsilon + \gamma\epsilon + \sqrt{t^2 + \gamma^2\epsilon^2 + 4\epsilon\omega}}{\epsilon}$$