Mixing Weyl and Gauss

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$$\mathbb{O}(e^{\delta ef}|fe) = \mathbb{O}\left(e^{\delta\partial_\alpha\partial_\beta} e^{\beta e} e^{\alpha f}\Big|_{\alpha=\beta=0} \Big| fe\right) = e^{\delta\partial_\alpha\partial_\beta}\mathbb{O}(e^{\beta e}e^{\alpha f}|fe)\Big|_{\alpha=\beta=0}$$

$$= e^{\delta\partial_\alpha\partial_\beta}\mathbb{O}(e^{-\alpha\beta h+\beta e+\alpha f}|ef)\Big|_{\alpha=\beta=0} = \mathbb{O}\left(e^{\delta\partial_\alpha\partial_\beta}e^{-\alpha\beta h+\beta e+\alpha f}\Big|_{\alpha=\beta=0}\Big| ef\right)$$

$$= \mathbb{O}($$

The g1 version, from 2017-02/g1.nb:

```
In[34]:= $TD = 8;
Simp[ 𝕆[e^(ħ (α f1+β e1)), {f1, e1} → 1] -
  𝕆[(1 - 1/2 α β ϵ ħ^2 (-2 β ħ e1 - 2 α ħ f1 + α β ħ^2 h1 - 4 l1))
    e^(ħ (-ħ h1 α β+α f1+β e1)), {e1, l1, f1} → 1]]
Out[34]= 0
```

The corresponding logos:

$$\frac{1}{2\mu^4}\Big(-h\alpha^2\beta^2 + e^2\beta^2\delta(2+h\delta) + f^2\delta(\alpha+e\delta)(\alpha(2+h\delta)+e\delta(4+3h\delta)) - 4h\alpha\beta\delta\mu + 4l\alpha\beta\mu^2 - 2h\delta^2\mu^2 + 4l\delta\mu^3 + 2e\beta(\alpha\beta+2\delta\mu(1+l\mu)) + 2f\big(\alpha^2\beta + 2\alpha\delta(e\beta(2+h\delta)+\mu(1+l\mu)) + e\delta^2(e\beta(3+2h\delta)+2\mu(2+h\delta+l\mu))\big)\Big)$$

The core logos:

$$\frac{1}{2\mu^4}\delta\left(e^2f^2\delta^2(4+3h\delta) + 4ef\delta\mu(2+h\delta+l\mu) + 2\mu^2(-h\delta+2l\mu)\right)$$

Aside. Compute $e^{\delta\partial_\alpha\partial_\beta}e^{-h\alpha\beta}\Big|_{\alpha,\beta=0}$

$$\partial_\alpha\partial_\beta e^{-h\alpha\beta} = \partial_\alpha(-h\alpha e^{-h\alpha\beta}) = (-h+h^2\alpha\beta)e^{-h\alpha\beta}$$
$$= (-h-h^2\partial_h)e^{-h\alpha\beta}$$