

Pensieve header: Testing "PolynomialQuotient".

$$p = \text{Expand}[(t + t^{-1})^5 (a + b + c)]$$

$$\frac{a}{t^5} + \frac{b}{t^5} + \frac{c}{t^5} + \frac{5a}{t^3} + \frac{5b}{t^3} + \frac{5c}{t^3} + \frac{10a}{t} + \frac{10b}{t} + \frac{10c}{t} + 10at + 10bt + 10ct + 5at^3 + 5bt^3 + 5ct^3 + at^5 + bt^5 + ct^5$$

$$q = \text{Expand}[(t + t^{-1})^2]$$

$$2 + \frac{1}{t^2} + t^2$$

PolynomialQuotient[p, q, t]

$$\frac{1}{t^5} (at^2 + bt^2 + ct^2 + 3at^4 + 3bt^4 + 3ct^4 + 3at^6 + 3bt^6 + 3ct^6 + 5at^8 + 5bt^8 + (-4a - 4b - 4c)t^8 + 5ct^8 + 15at^{10} + 15bt^{10} + (-15a - 15b - 15c)t^{10} + 15ct^{10} + 21at^{12} + 21bt^{12} + (-21a - 21b - 21c)t^{12} + 21ct^{12} + 13at^{14} + 13bt^{14} + (-13a - 13b - 13c)t^{14} + 13ct^{14} + 3at^{16} + 3bt^{16} + (-3a - 3b - 3c)t^{16} + 3ct^{16})$$

PolynomialQuotient[p, q, t] // Expand

$$\frac{a}{t^3} + \frac{b}{t^3} + \frac{c}{t^3} + \frac{3a}{t} + \frac{3b}{t} + \frac{3c}{t} + 3at + 3bt + 3ct + at^3 + bt^3 + ct^3$$