

$\delta_{aa}$  relations, 2

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The Task: in  $\delta_{aa}$ , reduce  $V^{\otimes 2} \otimes V^{\otimes 2}$  to  $S^2 V \otimes S^2 V$ .

The tasks: locality:  $\delta[a_{ij}, a_{kl}] = 0$

Swinging:  $\delta a_{ij} a_{kl} \sim \delta a_{ik} a_{jl}$

Tails commute:  $\delta[a_{ij}, a_{ik}] = 0$

Commute heads:  $\delta[a_{ik}, a_{ij}] = 0$

Commute T/H:  $\delta[a_{ij}, a_{jk}] \sim 0$

Actions: \* IF  $\delta a_{ij} a_{kl}$ ,  $|\{i, j, k, l\}| = 4$ ,

Use locality to get  $i < k$ , then swing to  $j < l$ ;

No issues.

\* IF one chord is a selfie & other is on

other strands: use locality; swinging

can be used to reduce to T/H  $\delta$

\* IF  $|\text{support}| = 3$ :

- shared tails:  $i = k$ ; use TC/swinging to  $j < l$

TC & swinging are compatible.

- shared heads:  $j = l$ ; use CH/swinging

to  $i < k$ .

$$CH: \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} = \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} - \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array}$$

Swinging:  $\delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} = \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} - \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array}$

They are compatible!

- T/H: target is  $\delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array}$ , start is  $\delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array}$

use T/H:  $\rightarrow \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} + \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} - \delta \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \begin{array}{|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array}$

$1223$ 
 $1323$ 
 $2313$