

```

d[e[n_]] := d[e[n]] = Total[f /@ (n - Most@NestWhileList[NextPrime, 2, # < n &])]

d[e[100]]
f[3] + f[11] + f[17] + f[21] + f[27] + f[29] + f[33] +
  f[39] + f[41] + f[47] + f[53] + f[57] + f[59] + f[63] + f[69] + f[71] +
  f[77] + f[81] + f[83] + f[87] + f[89] + f[93] + f[95] + f[97] + f[98]

d/@Array[e, {1000}];

Timing[d/@Array[e, {1000}];]
{0., Null}

Timing[Total[d/@Array[e, {1000}]];]
{0.156001, Null}

Timing[t0 = Sum[Round@Log[k] e[k], {k, 1000}] /. e[n_] => d[e[n]];]
{0.062400, Null}

Timing[t0 = Expand[t0];]
{64.007210, Null}

Timing[t1 = Expand[Sum[Round@Log[k] e[k], {k, 1000}] /. e[n_] => d[e[n]]];]
{48.625512, Null}

t0 == t1
True

Timing[t2 = Sum[Expand[Round@Log[k] d[e[k]]], {k, 1000}];]
{0.499203, Null}

t1 == t2
True

Timing[
  t3 = Total[Expand /@ (Table[Round@Log[k] e[k], {k, 1000}] /. e[n_] => d[e[n]])];]
{0.436803, Null}

t2 == t3
True

```