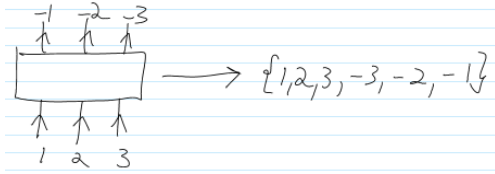


```
SetDirectory["C:\\drorbn\\AcademicPensieve\\2014-07"];
<< "MetaCalculi/MetaCalculi-Program.m"
```



```
 $\Omega_0[n\_Integer] := Table[
  Which[i < j, 0, i == j, (1 - T_i)^{-1}, i > j, 1],
  {i, n}, {j, n}];$ 
```

```
 $\Omega_0[3] // MatrixForm$ 
```

$$\begin{pmatrix} \frac{1}{1-T_1} & 0 & 0 \\ 1 & \frac{1}{1-T_2} & 0 \\ 1 & 1 & \frac{1}{1-T_3} \end{pmatrix}$$

```
 $\Omega[io\_List] := \Omega[\{io\}];$ 
```

```
 $\Omega[io\_List] /; EvenQ[Length@io] := Module[{n, \Omega_0, \Omega_0i},$ 
```

```
  n = Length[io] / 2;
```

```
  If[io == Join[Range[n], Range[-n, -1]],
```

```
     $\Omega_0 = \Omega_0[n]; \Omega_0i = Inverse[\Omega_0];$ 
```

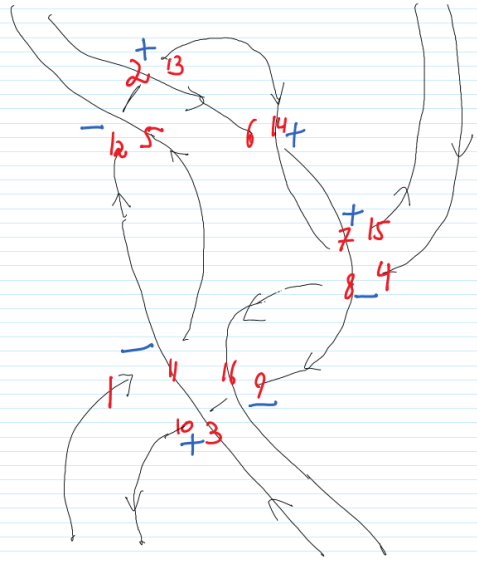
```
    Return[ $\Gamma[1, 0, \sum_{a=1}^n \sum_{b=1}^n t_a h_b \Omega_0i[[a, b]] \Gamma[1, 0, \sum_{a=1}^n \sum_{b=1}^n t_{-a} h_{-b} \Omega_0[[a, b]]]$ ]
```

```
  ]
```

```
]
```

```
 $\Omega[1, 2, -2, -1]$ 
```

$$\begin{pmatrix} 1 & s_{-2} & s_{-1} & s_1 & s_2 \\ s_{-2} & -\frac{1}{-1+T_2} & 1 & 0 & 0 \\ s_{-1} & 0 & -\frac{1}{-1+T_1} & 0 & 0 \\ s_1 & 0 & 0 & 1 - T_1 & 0 \\ s_2 & 0 & 0 & -(-1 + T_1) & (-1 + T_2) & 1 - T_2 \\ \Gamma & 0 & 0 & 0 & 0 \end{pmatrix}$$



$\gamma_0 =$

```
Xm[11, 1] Xm[5, 12] Xp[2, 13] Xp[14, 6] Xp[7, 15] Xm[8, 4] Xm[16, 9] Xp[3, 10] //  $\Gamma$  //
dm[1, 5, 1] // dm[2, 6, 2] // dm[2, 7, 2] // dm[2, 8, 2] // dm[2, 9, 2] //
dm[2, 10, 2] // dm[3, 11, 3] // dm[3, 12, 3] // dm[3, 13, 3] //
dm[3, 14, 3] // dm[3, 15, 3] // dm[4, 16, 4] // ds[2] // ds[4]
```

$$\begin{pmatrix} \frac{-1+T_2+T_3}{T_2 T_3} & S_1 & S_2 & S_3 \\ S_1 & \frac{1-T_3+T_1 T_3}{T_1 T_3} & \frac{(-1+T_1)(-1+T_3)}{T_1 T_3} & \frac{-1+T_1}{T_1} \\ S_2 & \frac{(-1+T_2)(-1+T_3)(T_2+T_3)}{T_1 T_2 T_3 (-1+T_2+T_3)} & \frac{T_1 T_2+T_2 T_4-T_1 T_2 T_4-T_2^2 T_4+T_1 T_2^2 T_4+T_3 T_4-2 T_2 T_3 T_4+T_2^2 T_3 T_4-T_3^2 T_4+T_2 T_3^2 T_4}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} & \frac{(-1+T_2)(T_2+T_3)}{T_1 T_2 (-1+T_2+T_3)} \\ S_3 & \frac{-1+T_3}{T_1 T_2 (-1+T_2+T_3)} & \frac{(-1+T_3)(T_1-T_1 T_4+T_1 T_2 T_4+T_3 T_4)}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} & \frac{T_3}{T_1 T_2 (-1+T_2+T_3)} \\ S_4 & 0 & \frac{-1+T_4}{T_2 T_3 T_4} & 0 \\ \Gamma & \frac{1}{T_3} & \frac{1}{T_3^2 T_4} & \frac{1}{T_1 T_3^2} \end{pmatrix}$$

$n = 4;$

```
 $\gamma_1 = (\gamma_0 // ds[1, 2, 3, 4]) *$ 
 $(\Omega[Join[Range[n], Range[-n, -1]]] // d\sigma@@Table[a \to \tau[a], \{a, n\}]);$ 
Do[ $\gamma_1 = \gamma_1 // dm[\tau[a], a, a], \{a, n\}$ ];
Do[ $\gamma_1 = \gamma_1 // dm[a, -a, a], \{a, n\}$ ];
 $\gamma_1$ 
```

$$\begin{pmatrix} \frac{-1+T_2+T_3}{T_2 T_3} & S_1 & S_2 & S_3 \\ S_1 & \frac{1-T_3+T_1 T_3}{T_1 T_3} & \frac{(-1+T_2)(-1+T_3)(T_2+T_3)}{T_1 T_2 T_3 (-1+T_2+T_3)} & \frac{-1+T_3}{T_1 T_2 (-1+T_2+T_3)} \\ S_2 & \frac{(-1+T_1)(-1+T_3)}{T_1 T_3} & \frac{T_1 T_2+T_2 T_4-T_1 T_2 T_4-T_2^2 T_4+T_1 T_2^2 T_4+T_3 T_4-2 T_2 T_3 T_4+T_2^2 T_3 T_4-T_3^2 T_4+T_2 T_3^2 T_4}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} & \frac{(-1+T_3)(T_1-T_1 T_4+T_1 T_2 T_4+T_3 T_4)}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} \\ S_3 & \frac{-1+T_1}{T_1} & \frac{(-1+T_2)(T_2+T_3)}{T_1 T_2 (-1+T_2+T_3)} & \frac{T_3}{T_1 T_2 (-1+T_2+T_3)} \\ S_4 & 0 & \frac{-1+T_2}{-1+T_2+T_3} & \frac{(-1+T_2)(-1+T_3)}{T_2 (-1+T_2+T_3)} \\ \Gamma & 0 & 0 & 0 \end{pmatrix}$$

**MatrixForm** /@ { $\gamma_0[A]$ ,  $\gamma_1[A]$  // **Transpose**}

$$\left\{ \begin{array}{cc} \frac{1-T_3+T_1 T_3}{T_1 T_3} & \frac{(-1+T_1) (-1+T_3)}{T_1 T_3} & \frac{-1+T_1}{T_1} & 0 \\ \frac{(-1+T_2) (-1+T_3) (T_2+T_3)}{T_1 T_2 T_3 (-1+T_2+T_3)} & \frac{T_1 T_2+T_2 T_4-T_1 T_2 T_4-T_2^2 T_4+T_1 T_2^2 T_4+T_3 T_4-2 T_2 T_3 T_4+T_2^2 T_3 T_4-T_3^2 T_4+T_2 T_3^2 T_4}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} & \frac{(-1+T_2) (T_2+T_3)}{T_1 T_2 (-1+T_2+T_3)} & \frac{-1+T_2}{-1+T_2+T_3} \\ \frac{-1+T_3}{T_1 T_2 (-1+T_2+T_3)} & \frac{(-1+T_3) (T_1-T_1 T_4+T_1 T_2 T_4+T_3 T_4)}{T_1 T_2 T_3 (-1+T_2+T_3) T_4} & \frac{T_3}{T_1 T_2 (-1+T_2+T_3)} & \frac{(-1+T_2) (-1+T_3)}{T_2 (-1+T_2+T_3)} \\ 0 & \frac{-1+T_4}{T_2 T_3 T_4} & 0 & \frac{1}{T_2} \end{array} \right.$$