

$$\hat{T}: \mathcal{A} \rightarrow \mathcal{A} \quad \mathcal{A} = L^2(\mathbb{R}^2)$$

Solves

$$\hat{T}_{12} \hat{T}_{13} \hat{T}_{23} = \hat{T}_{23} \hat{T}_{12} \quad \text{in } L^2(\mathbb{R}^3)$$

$$\hat{T}\psi = e^{2\pi i \hat{P}_1 \hat{Q}_2} \psi(\hat{Q}_1 - \hat{Q}_2 + \hat{P}_2)$$

$$\text{where } \hat{Q}_k F = x_k F$$

$$\hat{P}_k F = \frac{1}{2\pi i} \frac{\partial}{\partial x_k} F$$

We need to describe ψ ---

$$\psi(x) = \frac{1}{\Phi_h(x)}$$

$$\Phi_h(x) = \dots$$

Faddeev's quantum
dilogarithm.