

$$\overline{g} \overline{h} = w(g, h) \overline{gh} \quad \text{"twisted group algebras"}$$

Added March 24:

To thus twist a semi-direct product, it should be enough to twist the inverse map.