

Launch a testing program? ✓

Cheat Sheet J

<http://drorbn.net/AcademicPensieve/2013-03/>

initiated 18/3/13; completed ?; modified 21/3/13, 9:03am

With alphabet T and with $u, v, w \in T$, $\alpha, \beta, \gamma \in FL(T)$, $D \in \mathfrak{tder}(T)$, $g, h \in \exp(\mathfrak{tder}(T)) = \text{TAut}(T)$.

1. The definition of J :

$$J_u(\gamma) := \int_0^1 ds \operatorname{div}_u(\gamma \parallel RC_u^{s\gamma}) \parallel C_u^{-s\gamma}$$

2. The t equation (desired):

$$J_w(\gamma \parallel tm_w^{uv}) \parallel RC_w^{\gamma \parallel tm_w^{uv}} = J_u(\gamma) \parallel tm_w^{uv} \parallel RC_w^{\gamma \parallel tm_w^{uv}} + J_v(\gamma \parallel RC_u^\gamma) \parallel RC_v^{\gamma \parallel RC_u^\gamma} \parallel tm_w^{uv}$$

3. The h equation (desired):

$$J_u(\text{bch}(\alpha, \beta)) = J_u(\alpha) + J_u(\beta \parallel RC_u^\alpha) \parallel C_u^{-\alpha}$$

4. CRC equation t :

$$tm_w^{uv} \parallel RC_w^{\gamma \parallel tm_w^{uv}} = RC_u^\gamma \parallel RC_v^{\gamma \parallel RC_u^\gamma} \parallel tm_w^{uv}$$

5. CRC equation h :

$$RC_u^{\text{bch}(\alpha, \beta)} = RC_u^\alpha \parallel RC_u^{\beta \parallel RC_u^\alpha}$$

6. CRC equation div :

$$\operatorname{div}_u(\alpha \parallel RC_u^\gamma) \parallel C_u^\gamma = ?$$

7. div property t :

$$\operatorname{div}_w(\gamma \parallel tm_w^{uv}) = (\operatorname{div}_u(\gamma) + \operatorname{div}_v(\gamma)) \parallel tm_w^{uv}$$

8. div property h — the “cocycle condition”: with $\operatorname{ad}_u\{\gamma\} := \operatorname{der}(u \rightarrow [\gamma, u])$,

$$(\operatorname{div}_u \alpha) \parallel \operatorname{ad}_u\{\beta\} - (\operatorname{div}_u \beta) \parallel \operatorname{ad}_u\{\alpha\} = \operatorname{div}_u([\alpha, \beta] + \alpha \parallel \operatorname{ad}_u\{\beta\} - \beta \parallel \operatorname{ad}_u\{\alpha\})$$

9. div of bch :

$$\operatorname{div}_u(\text{bch}(\alpha, \beta)) = ?$$

10. The definition of JA :

$$JA_u(\gamma) := J_u(\gamma) \parallel RC_u^\gamma$$

11. The ODE for JA : with $\gamma_s = \gamma \parallel RC_u^{s\gamma}$,

$$JA(0) = 0, \quad \frac{dJA(s)}{ds} = JA(s) \parallel \operatorname{ad}_u\{\gamma_s\} + \operatorname{div}_u \gamma_s, \quad JA(1) = JA_u(\gamma)$$

12. The relation with \mathfrak{tder} :

$$e^{\operatorname{ad}_u\{\gamma\}} = C_u^\gamma \text{ and } C_u^\gamma = e^{\operatorname{ad}_u\{\gamma\}}$$

13. The definition of j (following A-T):

$$j(e^D) = \int_0^1 ds e^{sD} (\operatorname{div} D) = \frac{e^D - 1}{D} (\operatorname{div} D)$$

14. j 's cocycle property:

$$j(gh) = j(g) + g \cdot j(h)$$

15. The differential of \exp :

$$\delta e^\gamma = e^\gamma \cdot \left(\frac{1 - e^{-\operatorname{ad}_\gamma}}{\operatorname{ad}_\gamma} \right) (\delta\gamma) = \left(\frac{e^{\operatorname{ad}_\gamma} - 1}{\operatorname{ad}_\gamma} \right) (\delta\gamma) \cdot e^\gamma$$

16. The differential of $\gamma = \text{bch}(\alpha, \beta)$:

$$\left(\frac{1 - e^{-\operatorname{ad}_\gamma}}{\operatorname{ad}_\gamma} \right) (\delta\gamma) = \left(e^{-\operatorname{ad}_\beta} \frac{1 - e^{-\operatorname{ad}_\alpha}}{\operatorname{ad}_\alpha} \right) (\delta\alpha) + \left(\frac{1 - e^{-\operatorname{ad}_\beta}}{\operatorname{ad}_\beta} \right) (\delta\beta)$$

17. The differential of C (approximate):

$$\delta C_u^\gamma = \operatorname{ad}_u \left\{ \left(\frac{1 - e^{-\operatorname{ad}_\gamma}}{\operatorname{ad}_\gamma} \right) (\delta\gamma) \parallel RC_u^{-\gamma} \right\} \parallel C_u^\gamma$$

18. The differential of RC (approximate):

$$\delta RC_u^\gamma = RC_u^\gamma \parallel \operatorname{ad}_u \left\{ \left(\frac{e^{\operatorname{ad}_\gamma} - 1}{\operatorname{ad}_\gamma} \right) (\delta\gamma) \parallel RC_u^\gamma \right\}$$

19. The differential of J :

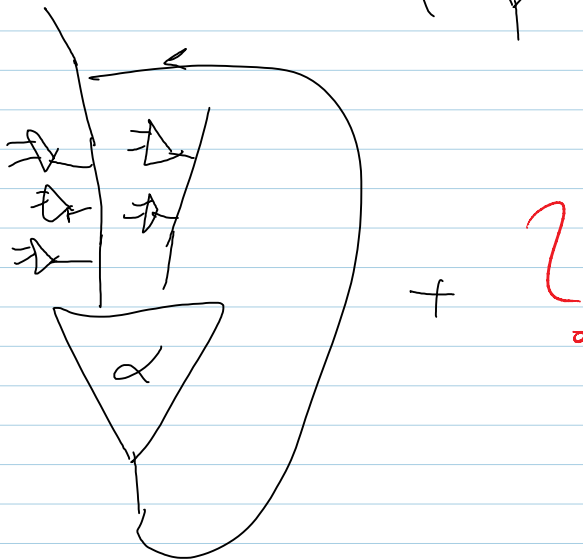
$$\delta J_u(\gamma) = ?$$

Add something about E / E_u ? seems pointless

Add something about $\mathfrak{h}, \mathfrak{tD}$ and their respective equations? ✓

$$\begin{aligned}
 t\Delta_{uv}^w // th^u // th^v &= th^w // t\Delta_{uv}^w ? \\
 h\Delta_{xy}^z // th^u // th^v &= h\Delta_{xy}^z // th^u // th^v = th^z // h\Delta_{xy}^z ?
 \end{aligned}
 \left. \vphantom{\begin{aligned} t\Delta_{uv}^w // th^u // th^v \\ h\Delta_{xy}^z // th^u // th^v \end{aligned}} \right\} \begin{array}{l} \text{Seems} \\ \text{easy} \end{array}$$

$$\text{div}_u(\alpha // C_u^\gamma) = \text{div}_u \left(\begin{array}{c} \begin{array}{|c|c|} \hline \begin{array}{c} \rightarrow \\ \rightarrow \\ \rightarrow \end{array} \\ \hline \end{array} \\ \alpha \end{array} \right) =$$



$$e^{\text{adu}\{\gamma\}} = C_u^{\beta} \text{ and } C_u^\gamma = e^{\text{adu}\{\beta\}}$$

The relation w/ A-T