

## Proofs

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10:30 AM

Proof of 1. Trivial for  $I^{ss}$ , easy for  $I^\beta$ .

Proof of 0.

$$J_y = \frac{\log \left( 1 + C_x \frac{e^{\pm C_x} - 1}{C_x} \right)}{C_x \frac{e^{\pm C_x} - 1}{C_x}} = \frac{\pm C_x}{e^{\pm C_x} - 1}$$

$$\begin{aligned} \text{So } \frac{1}{x} \left( \frac{y}{e^{\pm C_x} - 1} \right) &\mapsto \chi^{ss} \left( \exp \frac{\pm C_x}{e^{\pm C_x} - 1} \cdot \frac{e^{\pm C_x} - 1}{C_x} a_{xy} \right) \\ &= \chi^{ss} \left( \exp \pm a_{xy} \right) = \begin{array}{c} \uparrow e^{\pm a} \uparrow \\ \xrightarrow{\quad} \\ x \qquad y \end{array} \end{aligned}$$

Proof of 2.

$$\begin{aligned} I^\beta \left( \frac{1}{\langle \beta \rangle} \left( \frac{y}{x} \right) \right) &= \chi^{ss} \left( \exp \frac{\log \langle \alpha \rangle}{\langle \alpha \rangle} \sum \alpha_{ix} a_{ix} \right. \\ &\quad \left. + \frac{\log \langle \beta \rangle}{\langle \beta \rangle} \sum \beta_{iy} a_{iy} \right) \end{aligned}$$

Claim  $I \cap L^\beta = \text{Lie} \langle x, y : [x, y] = C_x y - C_y x \rangle$   
( $\deg x, y, C_x, C_y = 1$ )...