

```

In[9]:= {b = B[ω, α t[1] h[1] + β t[1] h[2] + γ t[2] h[1]],
        b // thswap[1, 1],
        b // J // thswap[1, 1] // K
        }

```

$$\text{Out[9]} = \left\{ \begin{pmatrix} \omega & h[1] & h[2] \\ t[1] & \alpha & \beta \\ t[2] & \gamma & 0 \end{pmatrix}, \begin{pmatrix} \omega + \alpha \omega c_1 & h[1] & h[2] \\ t[1] & \alpha + \frac{\alpha \gamma c_2}{1 + \alpha c_1} & \beta + \frac{\beta \gamma c_2}{1 + \alpha c_1} \\ t[2] & \frac{\gamma}{1 + \alpha c_1} & -\frac{\beta \gamma c_1}{1 + \alpha c_1} \end{pmatrix}, \right.$$

$$\left. \begin{pmatrix} \omega \left(1 + \frac{(-1 + e^{\alpha c_1 + \gamma c_2}) \alpha c_1}{\alpha c_1 + \gamma c_2} \right) & h[1] & h[2] \\ t[1] & \frac{e^{\alpha c_1 + \gamma c_2} \alpha (\alpha c_1 + \gamma c_2)}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} & \frac{e^{\alpha c_1 + \gamma c_2} \beta (\alpha c_1 + \gamma c_2)}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} \\ t[2] & \frac{\gamma (\alpha c_1 + \gamma c_2)}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} & -\frac{(-1 + e^{\alpha c_1 + \gamma c_2}) \beta \gamma c_1}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} \end{pmatrix} \right\}$$

```

In[10]:= {b = B[ω, α t[1] h[1]],
         b // thswap[1, 1],
         b // J // thswap[1, 1] // K
         }

```

$$\text{Out[10]} = \left\{ \begin{pmatrix} \omega & h[1] \\ t[1] & \alpha \end{pmatrix}, \begin{pmatrix} \omega + \alpha \omega c_1 & h[1] \\ t[1] & \alpha \end{pmatrix}, \begin{pmatrix} e^{\alpha c_1} \omega & h[1] \\ t[1] & \alpha \end{pmatrix} \right\}$$

```

In[11]:= {b = B[ω, β t[1] h[2]],
         b // thswap[1, 1],
         b // J // thswap[1, 1] // K
         }

```

$$\text{Out[11]} = \left\{ \begin{pmatrix} \omega & h[2] \\ t[1] & \beta \end{pmatrix}, \begin{pmatrix} \omega & h[2] \\ t[1] & \beta \end{pmatrix}, \begin{pmatrix} \omega & h[2] \\ t[1] & \beta \end{pmatrix} \right\}$$

```

In[12]:= {b = B[ω, γ t[2] h[1]],
         b // thswap[1, 1],
         b // J // thswap[1, 1] // K
         }

```

$$\text{Out[12]} = \left\{ \begin{pmatrix} \omega & h[1] \\ t[2] & \gamma \end{pmatrix}, \begin{pmatrix} \omega & h[1] \\ t[2] & \gamma \end{pmatrix}, \begin{pmatrix} \omega & h[1] \\ t[2] & \gamma \end{pmatrix} \right\}$$

```

In[13]:= {b = B[ω, δ t[2] h[2]],
         b // thswap[1, 1],
         b // J // thswap[1, 1] // K
         }

```

$$\text{Out[13]} = \left\{ \begin{pmatrix} \omega & h[2] \\ t[2] & \delta \end{pmatrix}, \begin{pmatrix} \omega & h[2] \\ t[2] & \delta \end{pmatrix}, \begin{pmatrix} \omega & h[2] \\ t[2] & \delta \end{pmatrix} \right\}$$

```

In[14]:= {b = B[ω, α t[1] h[1] + β t[2] h[2] + γ t[3] h[1]],
  b // tm[1, 2, 1],
  b // tm[1, 2, 1] // thswap[1, 1],
  b // thswap[2, 1] // thswap[1, 1] // tm[1, 2, 1],
  b // thswap[2, 1]
}

```

$$\text{Out[14]} = \left\{ \begin{pmatrix} \omega & h[1] & h[2] \\ t[1] & \alpha & 0 \\ t[2] & 0 & \beta \\ t[3] & \gamma & 0 \end{pmatrix}, \begin{pmatrix} \omega & h[1] & h[2] \\ t[1] & \alpha & \beta \\ t[3] & \gamma & 0 \end{pmatrix}, \begin{pmatrix} \omega + \alpha \omega c_1 & h[1] & h[2] \\ t[1] & \alpha + \frac{\alpha \gamma c_3}{1 + \alpha c_1} & \beta + \frac{\beta \gamma c_3}{1 + \alpha c_1} \\ t[3] & \frac{\gamma}{1 + \alpha c_1} & -\frac{\beta \gamma c_1}{1 + \alpha c_1} \end{pmatrix}, \right.$$

$$\left. \begin{pmatrix} \omega + \alpha \omega c_1 & h[1] & h[2] \\ t[1] & \alpha + \frac{\alpha \gamma c_3}{1 + \alpha c_1} & \beta + \frac{\beta \gamma c_3}{1 + \alpha c_1} \\ t[3] & \frac{\gamma}{1 + \alpha c_1} & -\frac{\beta \gamma c_1}{1 + \alpha c_1} \end{pmatrix}, \begin{pmatrix} \omega & h[1] & h[2] \\ t[1] & \alpha & -\alpha \beta c_2 \\ t[2] & 0 & \beta (1 + \alpha c_1 + \gamma c_3) \\ t[3] & \gamma & -\beta \gamma c_2 \end{pmatrix} \right\}$$

```

In[16]:= {b = B[ω, α t[1] h[1] + γ t[2] h[1] + δ t[2] h[2]],
  b // thswap[1, 1],
  b // J // thswap[1, 1] // K
}

```

$$\text{Out[16]} = \left\{ \begin{pmatrix} \omega & h[1] & h[2] \\ t[1] & \alpha & 0 \\ t[2] & \gamma & \delta \end{pmatrix}, \begin{pmatrix} \omega + \alpha \omega c_1 & h[1] & h[2] \\ t[1] & \alpha + \frac{\alpha \gamma c_2}{1 + \alpha c_1} & 0 \\ t[2] & \frac{\gamma}{1 + \alpha c_1} & \delta \end{pmatrix}, \right.$$

$$\left. \begin{pmatrix} \omega \left(1 + \frac{(-1 + e^{\alpha c_1 + \gamma c_2}) \alpha c_1}{\alpha c_1 + \gamma c_2} \right) & h[1] & h[2] \\ t[1] & \frac{e^{\alpha c_1 + \gamma c_2} \alpha (\alpha c_1 + \gamma c_2)}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} & 0 \\ t[2] & \frac{\gamma (\alpha c_1 + \gamma c_2)}{e^{\alpha c_1 + \gamma c_2} \alpha c_1 + \gamma c_2} & \delta \end{pmatrix} \right\}$$