

Twisting by 3-cocycles

One way that fusion categories get trickier is that a lot of information is encoded in the associator. For example, we can look at G -graded vector spaces with a nontrivial associator.

Associator

$$\omega_{\alpha,\beta,\gamma} : V_{\alpha\beta\gamma} = (V_\alpha \otimes V_\beta) \otimes V_\gamma \rightarrow V_\alpha \otimes (V_\beta \otimes V_\gamma) = V_{\alpha\beta\gamma}$$

assigns a scalar to every triple (α, β, γ) .

- Compatibility = ω is a 3-cocycle
- $\text{Vec}(G, \omega)$ up to equivalence only depends on $\omega \in H^3(G, k^\times)$.