

Pensieve Header: Verifying the "2D Lie Algebra" formula for the Alexander polynomial. Also, YAAP - Yet Another Alexander Program.

Drawing Arrow Diagrams

```
Draw[expr_] := expr /. gd_GD => Draw[gd];
Draw[gd_GD] := Module[
  {n = Length[gd], h, k = 0},
  Graphics[{
    Line[{{0, 0}, {2 n + 1, 0}}],
    Table[Text[i, {i, -0.3}], {i, 2 n}],
    (List @@ gd) /. {
      Ar[i_, j_, s_] => {
        h = Abs[i - j] / 2;
        BezierCurve[{
          {i, 0}, {i, h}, {(i + j) / 2, h}, {j, h}, {j, 0}
        }, SplineDegree -> 2],
        Text[s * (++k), {(i + j) / 2, h - 0.3}],
        Line[{{j - 0.2, 0.4}, {j, 0}, {j + 0.2, 0.4}}]
      }
    }
  ]
];
```

Main

```

GD[K_] := GD @@ PD[K] /. X[i_, j_, k_, l_] => If[PositiveQ[X[i, j, k, l]],
  Ar[l, i, +1],
  Ar[j, i, -1]
];
SL[K_] := Plus @@ (GD[K] /. Ar[t_, h_, s_] => If[h > t, s DR, s DL]);
Arcs[gd_GD] := Module[
  {n, heads, arcs, k},
  n = Length[gd];
  heads = Sort[Cases[gd, Ar[_ , h_ , _] => h]];
  arcs = Table[0, {2 n}];
  arcs[[heads]] = Range[n];
  k = 1;
  Do[If[arcs[[i]] == 0, arcs[[i]] = k, ++k], {i, 2 n}];
  arcs
];
R[gd_GD] := Module[
  {n, mat, arcs, k},
  n = Length[gd]; arcs = Arcs[gd];
  mat = Table[0, {n}, {n+1}];
  k = 0; gd /. Ar[t_, h_, s_] => {
    ++k;
    mat[[k, arcs[[h]]] += -1;
    mat[[k, arcs[[t]]] += 1 - X^s;
    mat[[k, arcs[[h]] + 1] += X^s
  };
  mat
];
e[n_, i_] := ReplacePart[Table[0, {n}], i -> 1];
EZ[gd_GD] := Module[
  {n, r, arcs, j},
  n = Length[gd];
  r = R[gd];
  arcs = Arcs[gd];
  j = 0;
  Simplify[Plus @@ (
    gd /. Ar[t_, h_, s_] => s * (
      Inverse[Append[r, e[n+1, arcs[[h]]]].Append[x e[n, ++j], DR]
    )[[arcs[[t]]]
  )]
];

```

```

];
EZ1[gd_GD] := Module[
  {n, r, arcs, j},
  n = Length[gd];
  r = R[gd];
  arcs = Arcs[gd];
  j = 0;
  Simplify[List @@ (
    gd /. Ar[t_, h_, s_] => s * (
      Inverse[Append[r, e[n+1, arcs[[h]]]].Append[x e[n, ++j], DR]
    )[[arcs[[t]]]]
  )]
];
EZ2[gd_GD] := Module[
  {n, r, arcs, j},
  n = Length[gd];
  r = R[gd];
  arcs = Arcs[gd];
  j = 0;
  Simplify[Plus @@ (
    gd /. Ar[t_, h_, s_] =>
      s * x * Inverse[Append[r, e[n+1, arcs[[h]]]]][[
        arcs[[t]], ++j
      ]]
  )]
];

```