

Dirac Structures: (V, E)

Def A Dirac structure on a vector bundle $V \rightarrow M$ is a Lagrangian subbundle $E \subset V \oplus V^*$ relative to the obvious inner product, maximally isotropic subbundle.

Examples $(V, V), (V, V^*), (V, G_{\omega})$ $\omega \in \Gamma(\wedge^2 V^*)$

$w: V \rightarrow V^*$ s.t. $w(x)(y) = -w(y)(x)$

claim $\{(x, w(x))\}$ is a Dirac structure. [obvious]

In diagrams: $w: \downarrow \quad E: \{(\downarrow, \uparrow)\}$

Def A morphism of Dirac structures

$(\oplus, w): (V, E) \rightarrow (V', E')$

s.t. \oplus is a vector bundle map $V \rightarrow V'$

w is in $\Gamma(\wedge^2 V^*)$

s.t.

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Dixmier-Douady bundles ("gerbes")

Def A DD-bundle $\mathcal{A} \rightarrow M$ is a bundle of \ast -algebras with typical fiber

$(K(H) = \overline{\text{Lin}(H)})$ ("compact operators")

Example If $V \rightarrow M$ is an even rank v.b.,

$\text{Cl}(V) \rightarrow M$ is a DD bundle.

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clifford

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