

[Picture on page "Alekseev - Torossian"](#)

Proposition 5.1. There is a unique map $j : \text{TAut}_n \rightarrow \mathfrak{t}_n$ which satisfies the group cocycle condition

(18)
$$j(gh) = j(g) + g \cdot j(h),$$

and has the property

(19)
$$\frac{d}{ds} j(\exp(su))|_{s=0} = \text{div}(u).$$

In D-talk this is

$$j(D) = S(W(D)) \cdot D$$

added Feb 12, 2009:
I'm no longer convinced
if this is for all D
or only for exponential DS.

where $S(D)$ is the antipode of A_n^w , the anti-automorphism that turns diagrams upside down & multiplies every leg by -1 .

* $W(D)$ maps every in-leg in D to its negative.

Added Feb 13, 2009: There ought to be an even simpler, E-k-style interpretation of $j(D)$

Q What is j on $(n=2)$

$$\exp(a_1 \leftarrow + a_2 \rightarrow + H(f_1) \leftarrow + H(f_2) \leftarrow) =: \exp(u)$$

$$j(\exp(u)) = \frac{e^u - 1}{u} \cdot \text{div}(u)$$

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$$\text{div } u = (x_2 f_1 \pm x_1 f_2) w$$
 Probably (-).

$$\Rightarrow j(\exp u) = (x_2 f_1 \pm x_1 f_2) w$$

Q What's the first thing to depend on whether j is right?

what's \tilde{f} mod CC? $\text{ch}(x,y) = \log e^{xy}$

$$\tilde{f}(a) = a(x) + a(y) - a(\text{ch}(x, y))$$

mod $\mathbb{C}\langle\langle \rangle\rangle$, in \mathfrak{f}_n , this is

$$= a(x) + a(y) - a(x+y)$$